

Asymptotic Cones and Functions in Optimization and Variational Inequalities
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Errata as of September 2006

- p.8, l.2: $C_1 \cap \text{ri } C_2 = \emptyset$.
- p.9, l.7: $\alpha \cdot \infty = 0$.
- p.10, l.7: replace 'epi($\inf_{i \in I} f_i$) = $\cup_{i \in I} \text{epi } f_i$ ' by 'epi($\inf_{i \in I} f_i$) $\subset \cup_{i \in I} \text{epi } f_i$ '.
- p.11, l.9: replace ' $x, y \in \mathbb{R}^n$ ' by ' $x, y \in \text{dom } f$ '.
- p.13, In Proposition 1.2.9, l.17: replace $t_i f_i(x)$ by $t_i f_i(x_i)$.
- p.16, l.13: replace 'max' by 'sup'.
- p.17, l.-7: replace ' $x \in \text{ri}(\text{dom } f)$ ' by ' $x \in \text{int}(\text{dom } f)$ '.
- p.19, l.12: replace $\{C\}_{i \in I}$ by $\{C_i\}_{i \in I}$.
- p.19, l.24: $\text{dom } \sigma_C \subset \cap_{i \in I} \text{dom } \sigma_{C_i}$.
- p.22, l.17: after 'at every point $\bar{x} \in \mathbb{R}^n$,' insert '(and $S(\bar{x})$ is a compact set for each \bar{x})'.
- p.43, l.14: add the assumption ' C is semibounded'; l.19 (b): remove 'If in addition C is semibounded then'.
- p.44, Just after Definition 2.4.1, the sentence "We recall...for all $y \in V$ " should be removed. The continuity of σ_C at x means that for each sequence $\{x_k\}$ converging to x the sequence $\{\sigma_C(x_k)\}$ converges to $\sigma_C(x)$.
- p.49, l.18: denotes
- p.53, l.3: replace ' $f(t) = t \sin t^{-1}$ ' by ' $f(t) = t \sin t$ '.
- p.55, l.4: in the second expression for \mathcal{K}_f , replace ' $(\text{epi } f)_\infty \cap \{(d, 0) | d \in \mathbb{R}^n\}$ ' by ' $L((\text{epi } f)_\infty \cap \{(d, 0) | d \in \mathbb{R}^n\})$, where L is the projection map on \mathbb{R}^n '.
- p.59, l.2: replace p_f by p .
- p.59, l.11: y, x should be ' d ' in the formula of $\text{cl } p$.
- p.62, In Proposition 2.6.4, replace ' $\psi : (-\infty, b) \rightarrow \mathbb{R}$ with $0 \leq b \leq \infty$ be a convex' by ' $\psi : \mathbb{R} \cup \{+\infty\}$ with $\text{dom } \psi = (-\infty, b), 0 \leq b \leq +\infty$ be a lsc convex'.
- p.65, l.-2: in the right hand side of (c), replace ' $\psi(s^{-1})$ ' by ' $\psi^*(s^{-1})$ '.
- p.67,l.17: replace ' $\text{tr}(AB)$ ' by ' $\text{tr } A^t B$ '.
- p.79, l.-18: after by Zalinescu [135], add 'see also C. Zalinescu, Stability for a class of nonlinear optimization problems and applications, in *Nonsmooth Optimization and Related Topics*, F. H. Clarke, V. F. Dem'yanov, F. Gianessi (eds.), Plenum Press, New York, 1989, pp. 437-458.'
- p.82, l. -16: change 'on the level set' by 'on the nonempty level set'.
- p.83, l.-7: d_k converging to x .
- p.91, l.15: add after 'convex' 'and with $\inf f > -\infty$ '.
- p.92, l.9: after ' $f := \sup_k f_k$ ' insert 'a proper function,'.
- p.100, l.-3: replace 'Then since' by 'Then since whenever $C(y) \neq \emptyset$, one has'.
- p.111, l.11: remove the extra +.
- p.112, l. -8: after image add: of such a set under a linear map is closed.
- p.113; l.18: replace ε_1 by λ_1 .
- p.120, l. -11: after ' $i = 1, \dots, r$ ' add ' and ' $f_i(\hat{x}) \leq 0, i = r + 1, \dots, m$ '.
- p.121, l.7: To apply Proposition 1.2.22, one needs to change 'ri dom f_0 ' by 'int dom f_0 ' in the

hypothesis (ii), (p.120, l,-11). However, a different proof of Theorem 4.1.2 would allow to keep the hypothesis (ii) as stated with the relative interior assumption on $\text{dom } f_0$.

p.125, l.-11: should be ' $(f(x) - \lambda)^+$ ' instead of ' $(f(x))^+$ '.

p.126, In Lemma 4.2.2 (b): replace $y \in \text{ri dom } f$ by $y \in \text{int dom } f$.

p.127, l.4, l. -4, l. -7; p.128, l.11 and p.131 l. -12: replace $x \in \text{ri dom } f$ by $x \in \text{int dom } f$.

p.127, l.-4; p.128, l.11, and p.131, l. -12: insert after that ' $\infty > f(x) > \inf f$ '.

p.130, l.-3: last term should be $s(f^*(y/s) + \lambda)$.

p.131, l.13: replace Proposition 3.6.1 by Proposition 3.6.2

p.133, l.-2: replace 'norm on \mathbb{R}^n ' by 'norm on \mathbb{R}^m '.

p.140, l.17: replace the letter ' m ' in (P) by ' m_* ', as well in the corresponding places in Theorem 4.1.1 and its proof in p. 141.

p.141, l.12: replace Definition 4.3.1(c) by Definition 4.4.1(c), and in l.19: Theorem 4.1.1 by Theorem 3.6.3.

p.150, l.19: Without additional assumptions on Φ , the implication (b) \implies (c) is incorrect.

p.156, l.2: after Theorem 5.1.4(a) add: and Corollary 5.1.1(a) applied...

p.156, in Corollary 5.2.2: remove: and $g : \mathbb{R}^n \rightarrow \mathbb{R} \cup +\infty$, and add: be a proper lsc convex function, and let A:...

p.160, In Proposition 5.3.2, the statement (b) should be replaced by 'Under assumption (R), if $0 \in \text{ri dom } \varphi$, then assumption (S) holds, and $\text{ri dom } \varphi = \text{int dom } \varphi$ '.

p.160, l.-9: replace the letter '(L)' by '(R)'.

p.161, l.2: replace the letter '(L)' by '(R)'.

p.163, l.-10: remove the example of the log-sum-exp function which is not strictly convex.

p.164, l.-2: add for 'every k ' after $C_1(u^k)$.

p.178, in formula (5.8) replace: $\sup_{y \in D} K(\cdot, y)_\infty > 0, \forall w \neq 0$.

p.179, l.17: replace $S_P(v)$ by $S_P(u)$.

p.192, l.3: replace 'is then' by 'and then δ_C '.

p.194, l.-3: replace (y, w) by (z, w) , and $y \in \partial f_0(x) + \dots$ by $z \in \partial f_0(x) \dots$

p.210, l.8: replace $\forall v \in \text{dom } T$ by $\forall w \in \text{dom } T$.

p.215, l.-5 and last line: replace Proposition 6.6.4(v) by Proposition 6.6.4(e) and Proposition 6.6.4(iv) by Proposition 6.6.4(d).

p.217, l.-7: add 'if' after we assume.

p.219, l.18: replace 'using Corollary 6.8.2' by 'using Corollary 6.8.2'.

p.220, l.1: replace 'enssure' by 'ensure'.

p.226, In statement of Theorem 6.9.2: add after exists x^* , 'in $M(u^*)$ ' and replace ' $u^* + F(x^*) = 0$ ' with ' $F(x^*) \leq 0$ '. In the proof of that Theorem: add 'in $M(u^*)$ ' after there exists x^* .

p.229, l.8: remove the '(i)' in Proposition 6.8.1.

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