

# Ray Tracing



MIT EECS 6.837

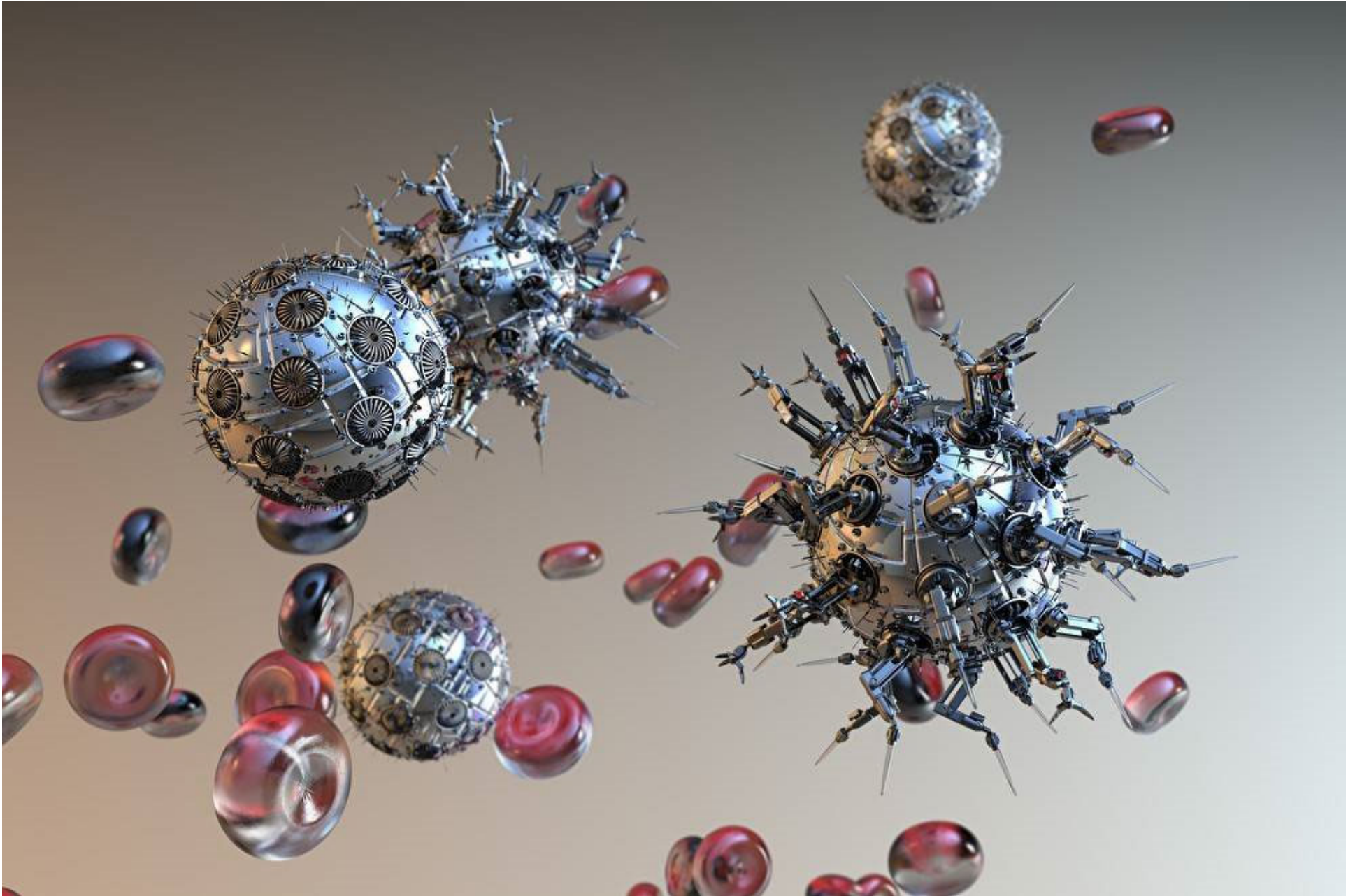
Most slides are taken from Frédo Durand and Barb Cutler

Some slides courtesy of Leonard McMillan









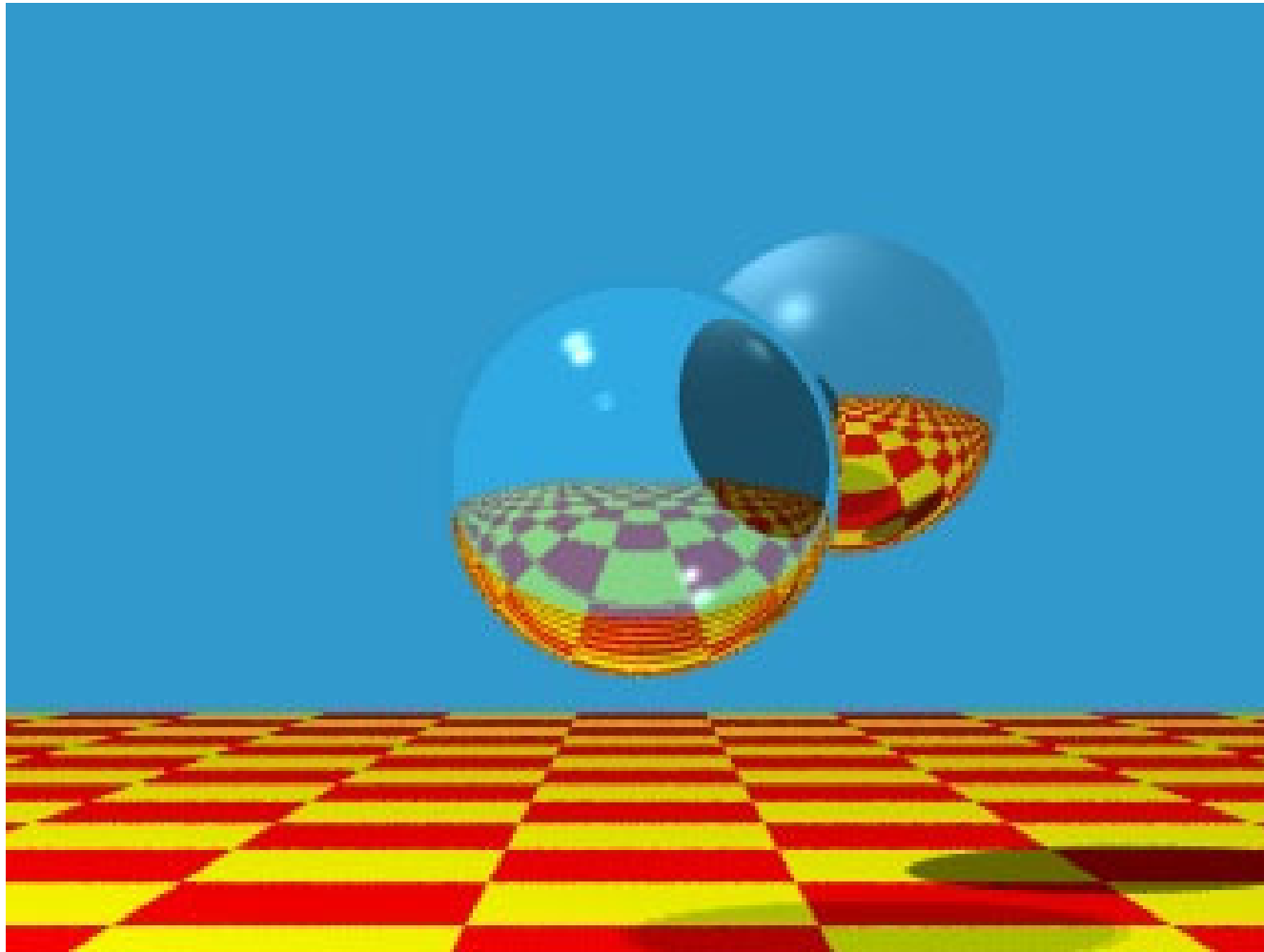
# Ray Tracing

---

- Ray Tracing kills two birds with one stone:
  - Solves the Hidden Surface Removal problem
  - Evaluates an improved **global** illumination model
    - shadows
    - ideal specular reflections
    - ideal specular refractions
  - Enables direct rendering of a large variety of geometric primitives
- Book: A. Glassner, An Introduction to Ray Tracing
- Web: <http://www.cs.cf.ac.uk/Ray.Tracing>

# Ray Tracing

---



Recursive ray tracing: Turner Whitted, 1980



# Backward Tracing

---

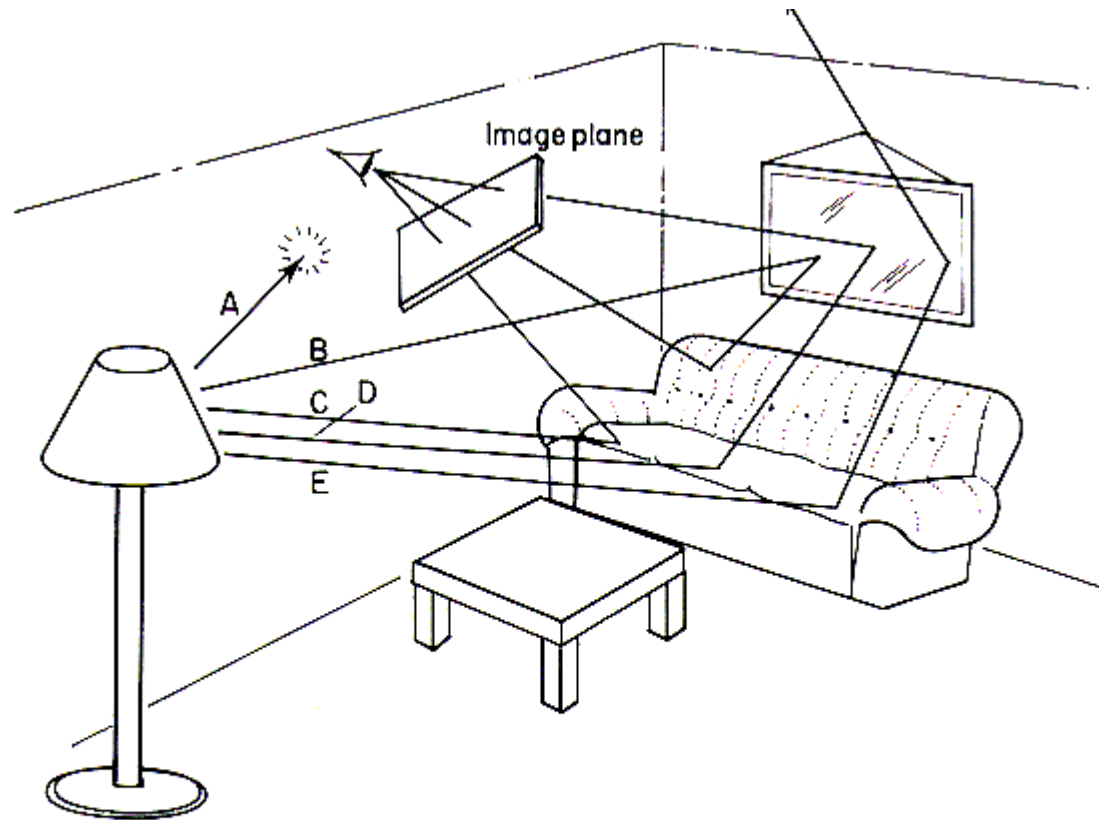
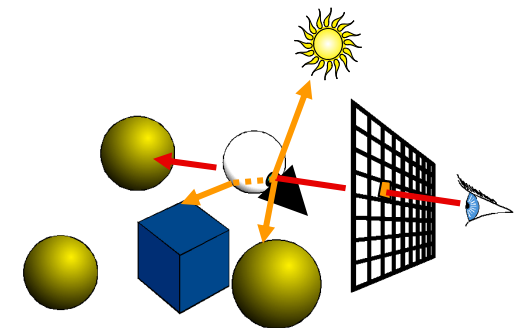
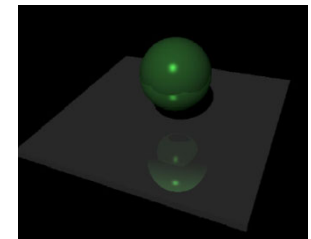
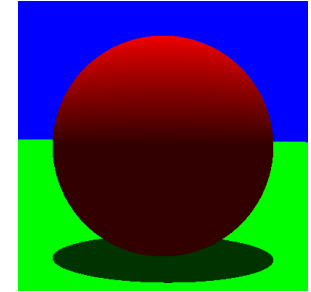


Fig. 5. Some light rays (like A and E) never reach the image plane at all. Others follow simple or complicated routes.

# Overview of today

---

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing



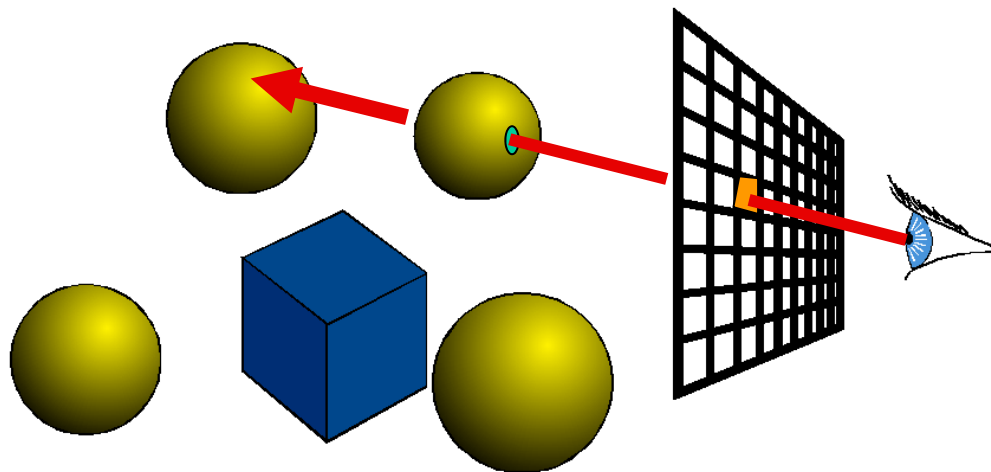


# Ray Casting (a.k.a. Ray Shooting)

---

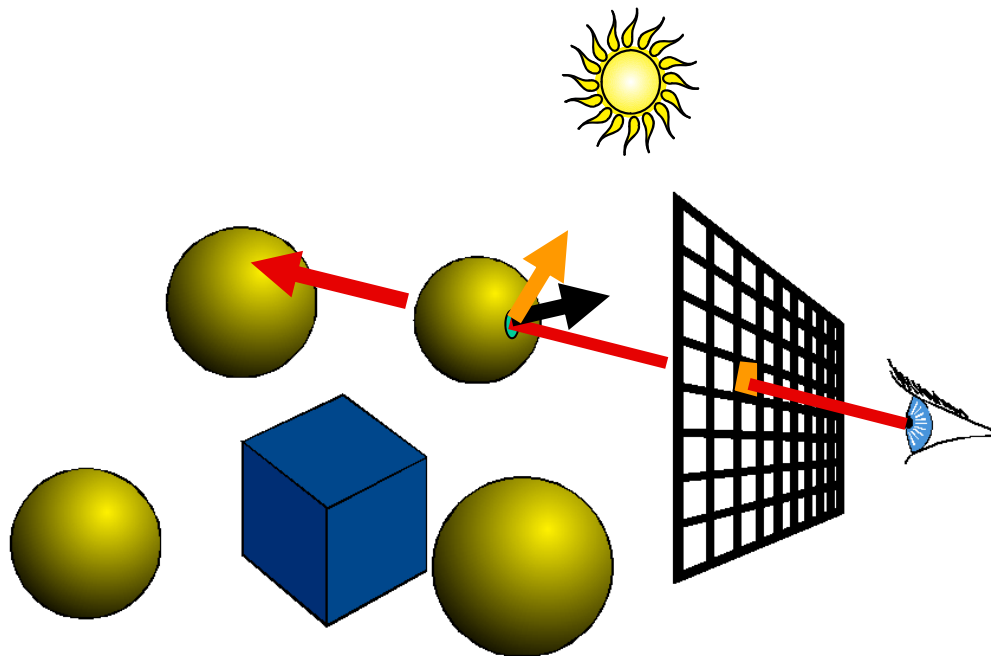
For every pixel  $(x, y)$   
Construct a ray from the eye  
 $color[x, y] = \text{castRay}(\text{ray})$

- Complexity?
  - $O(n * m)$
  - $n$ : number of objects,  $m$ : number of pixels



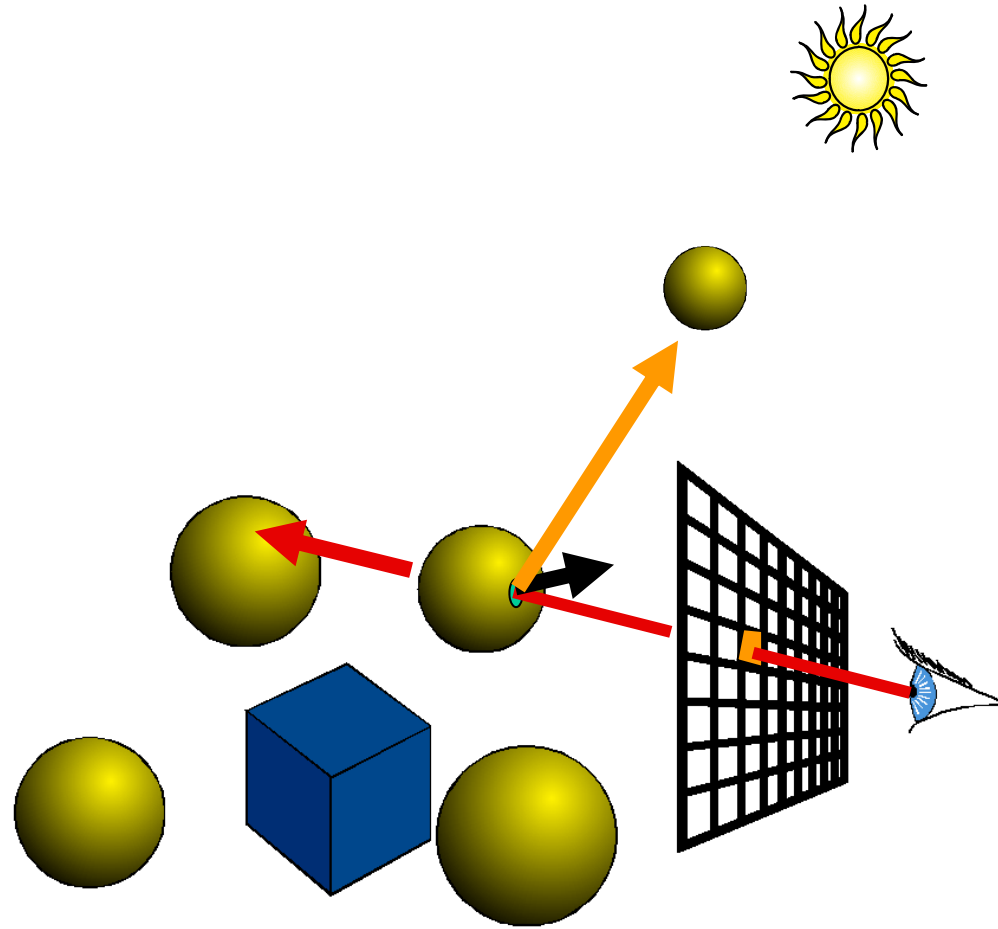
# Ray Casting with diffuse shading

---



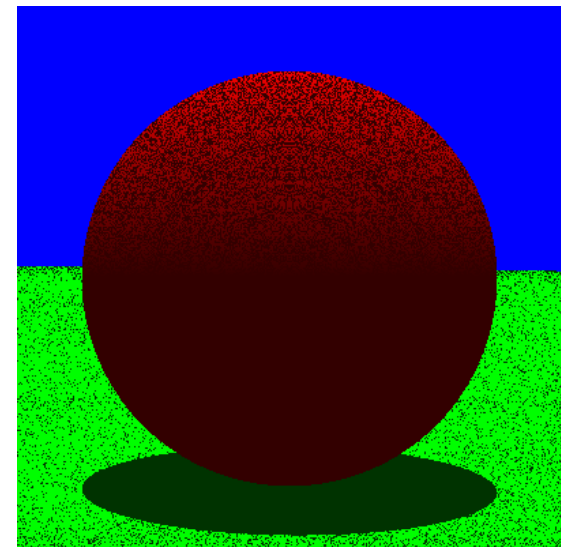
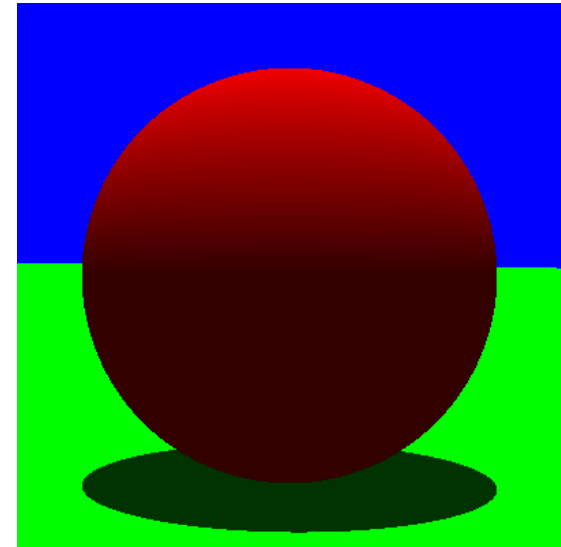
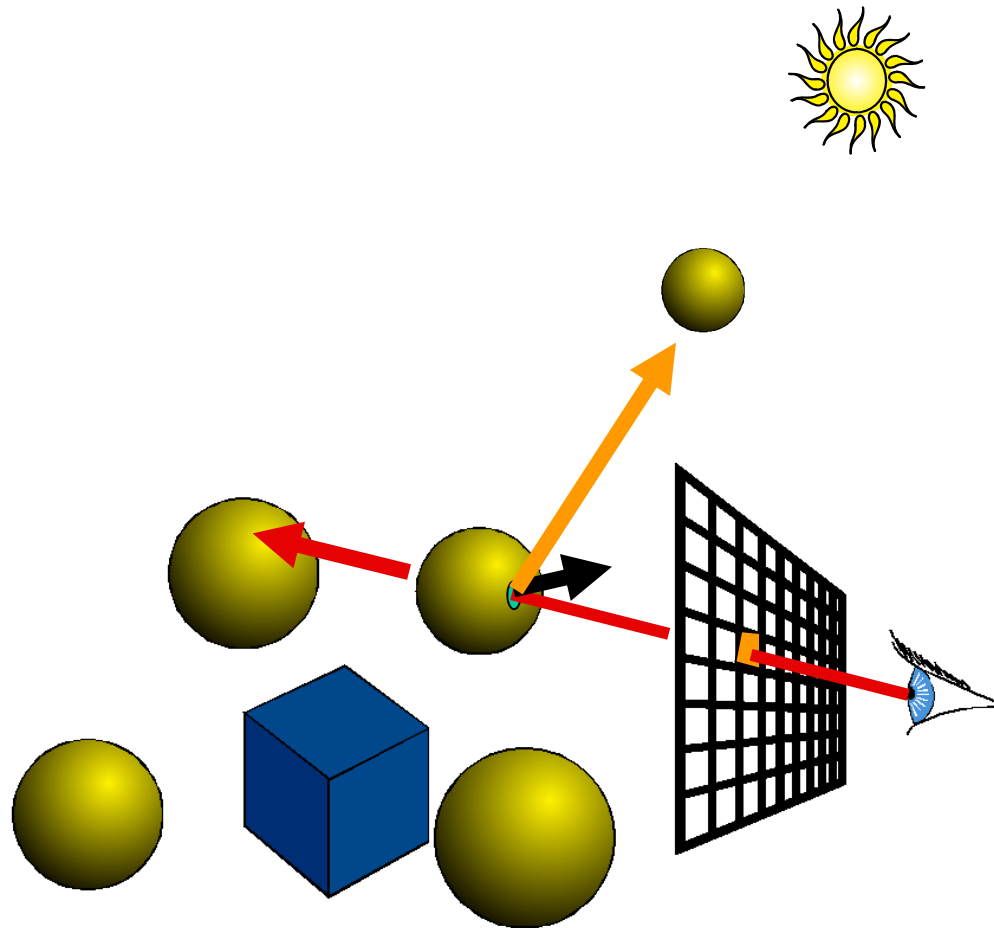
# Shadows

---



# Shadows

---

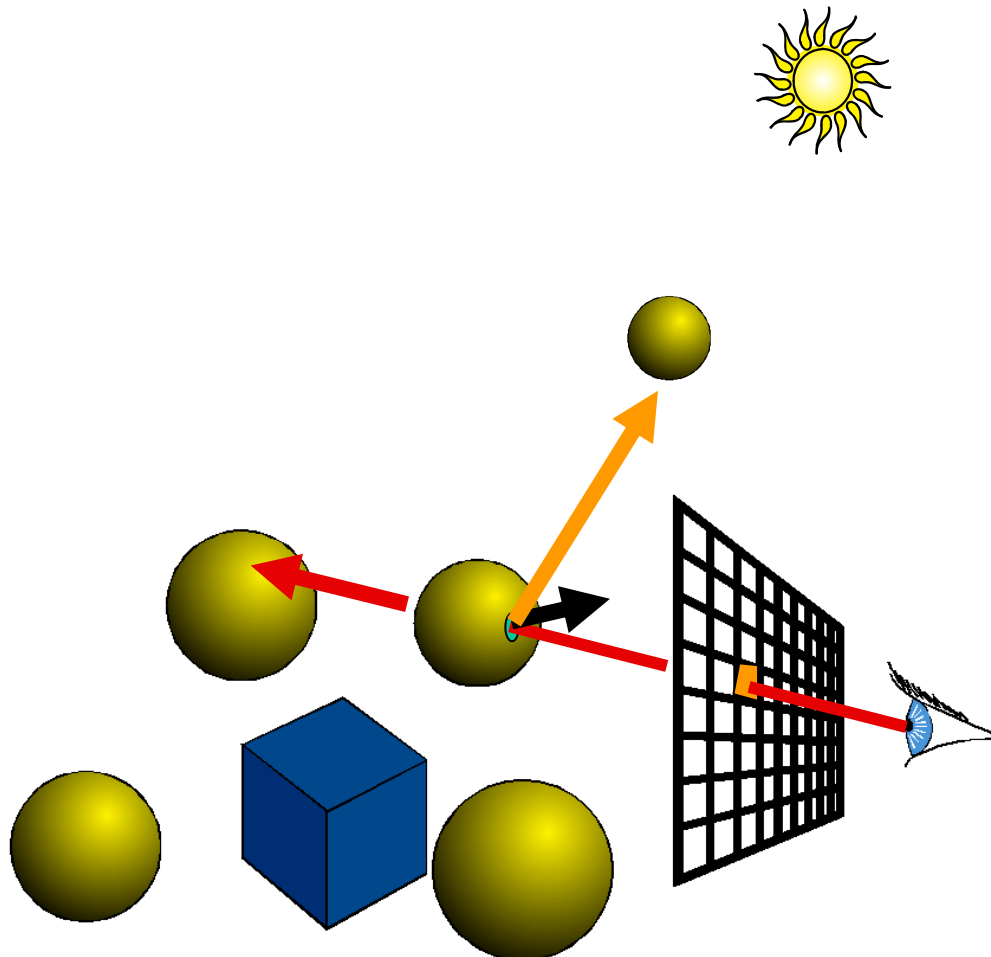




# Shadow optimization

---

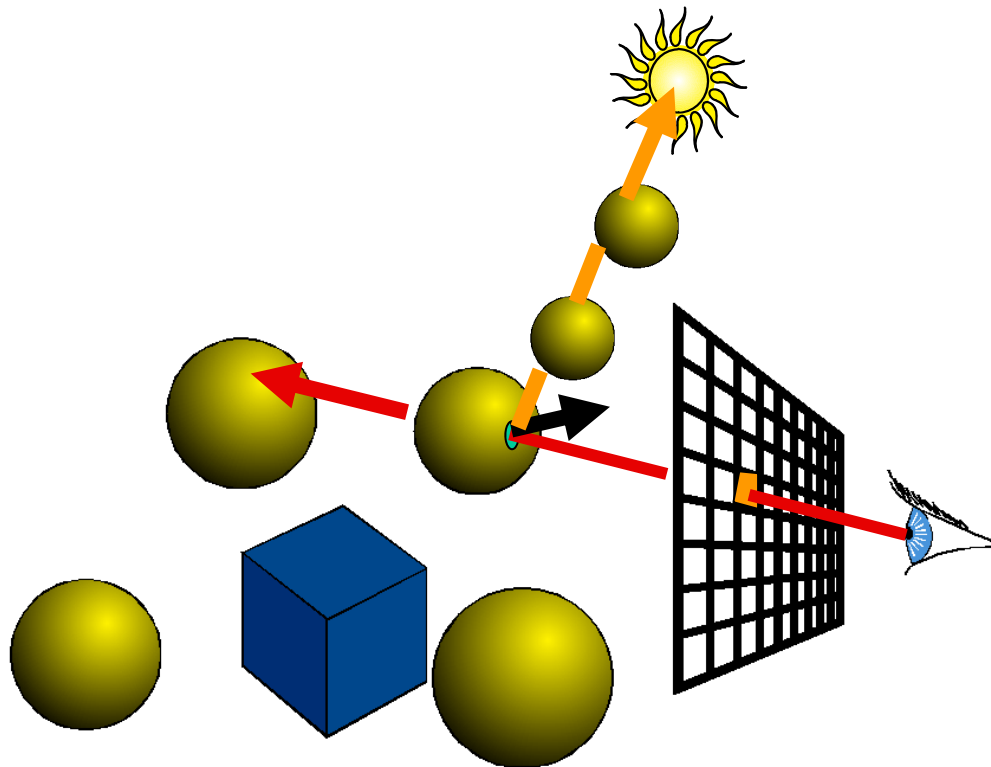
- Shadow rays are special
- How can we accelerate our code?



# Shadow optimization

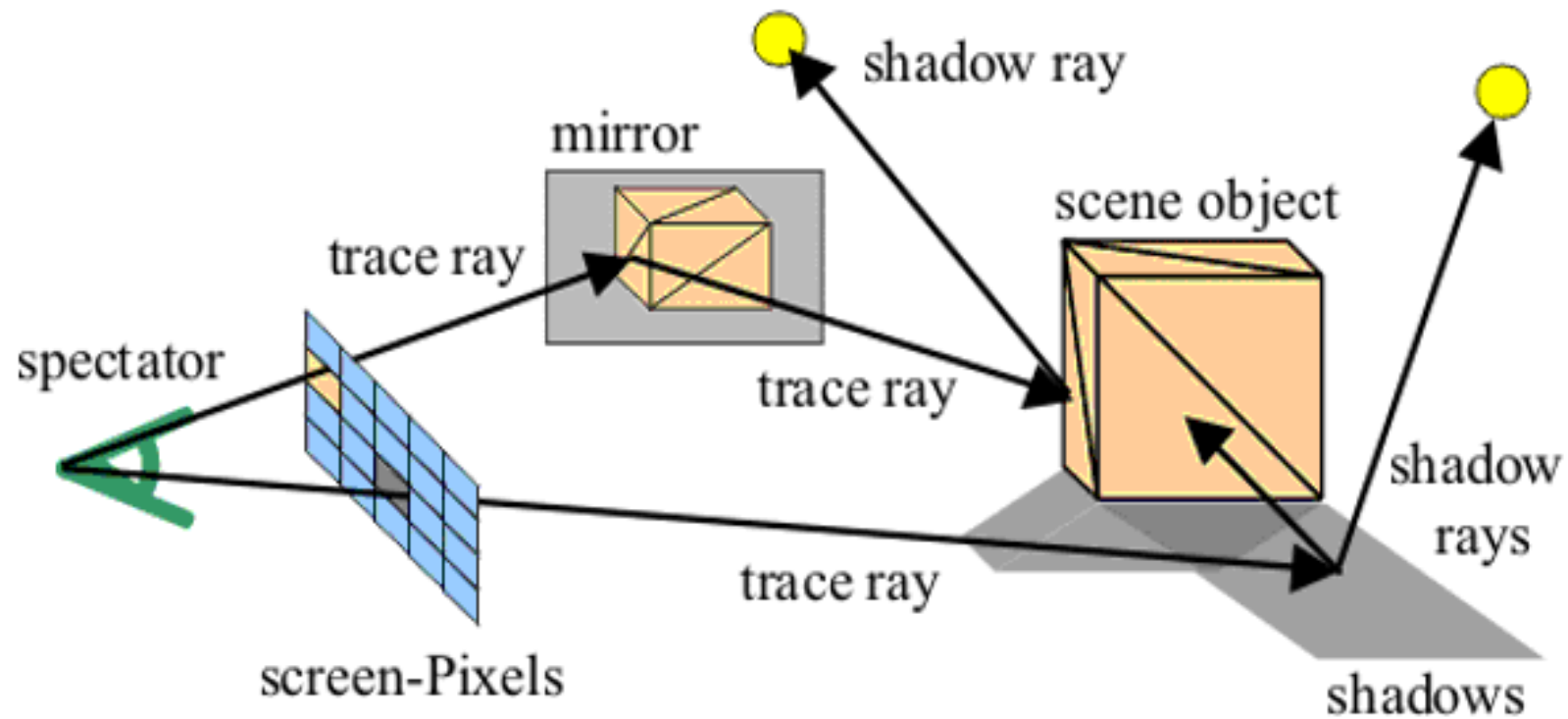
---

- We only want to know whether there is an intersection, not which one is closest
  - Stops at first intersection



# Recursive Ray Tracing

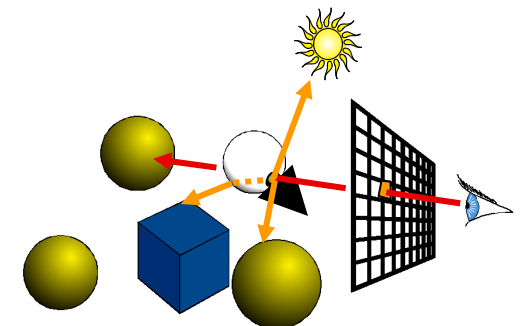
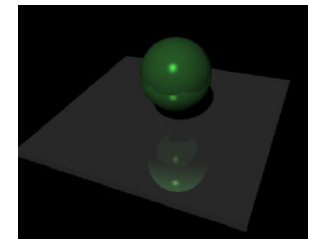
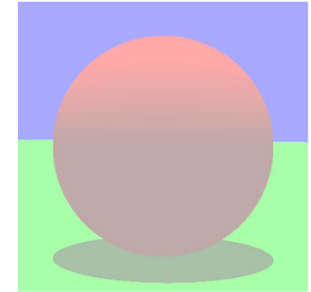
---



# Overview of today

---

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing

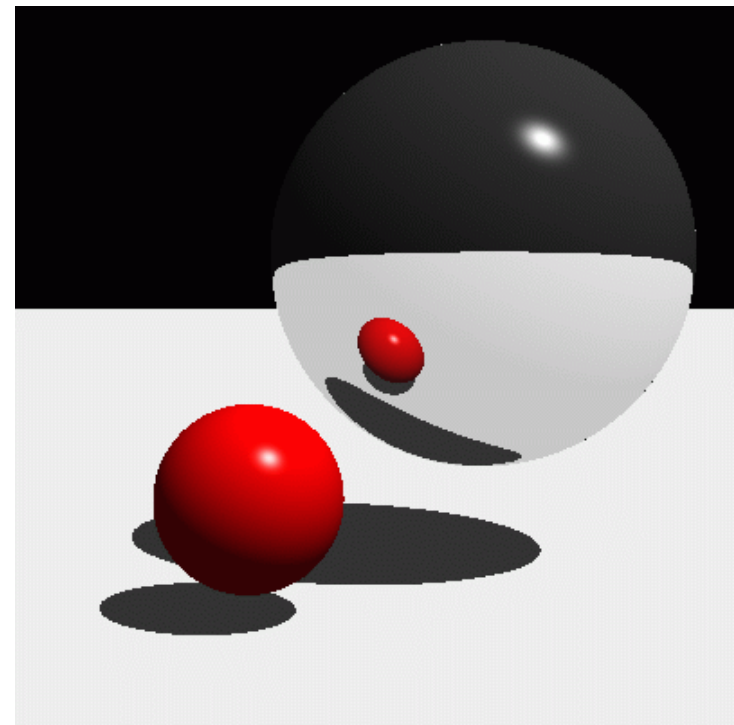
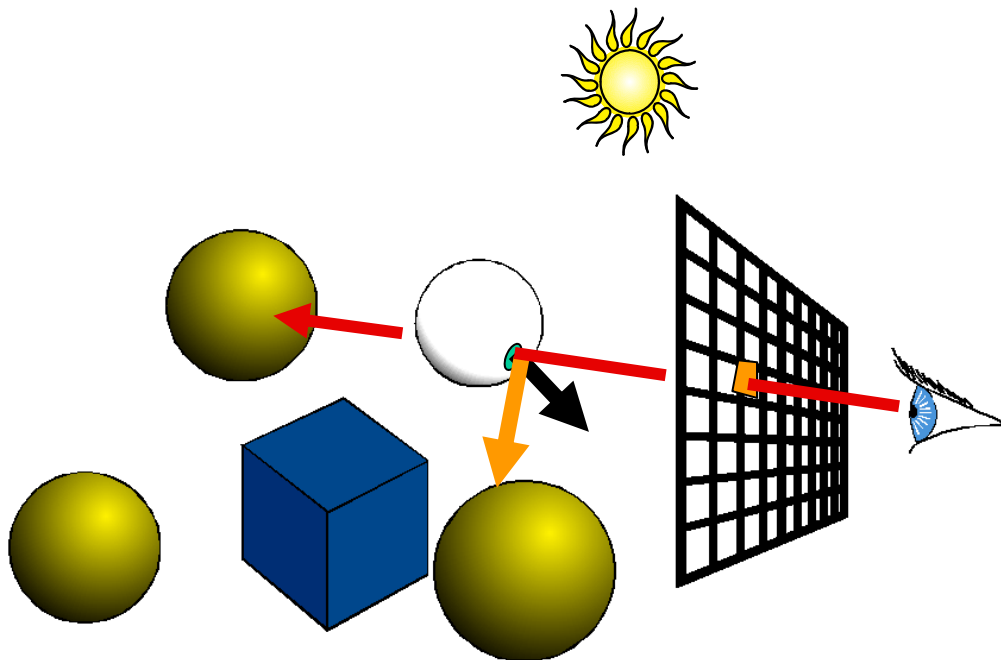




# Mirror Reflection

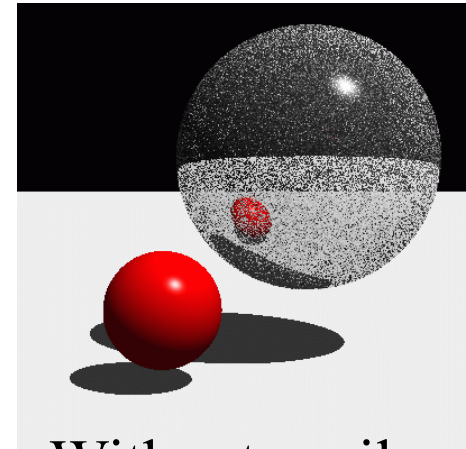
---

- Compute mirror contribution
- Cast ray in direction symmetric wrt normal
- Multiply by reflection coefficient (color)

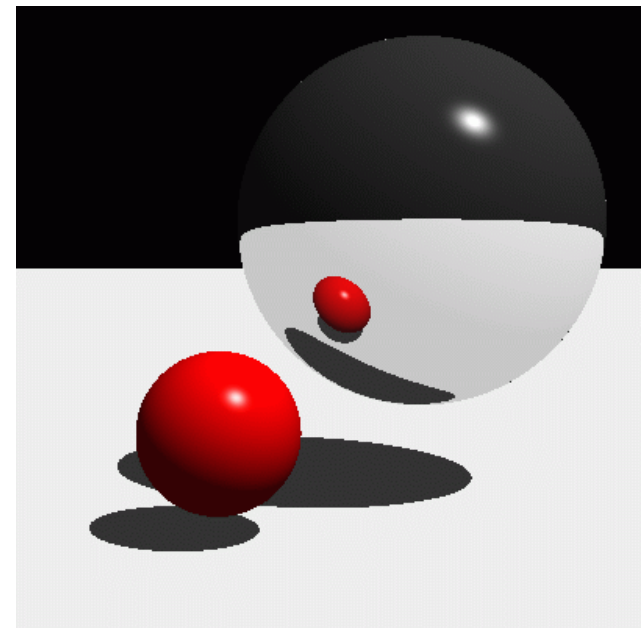
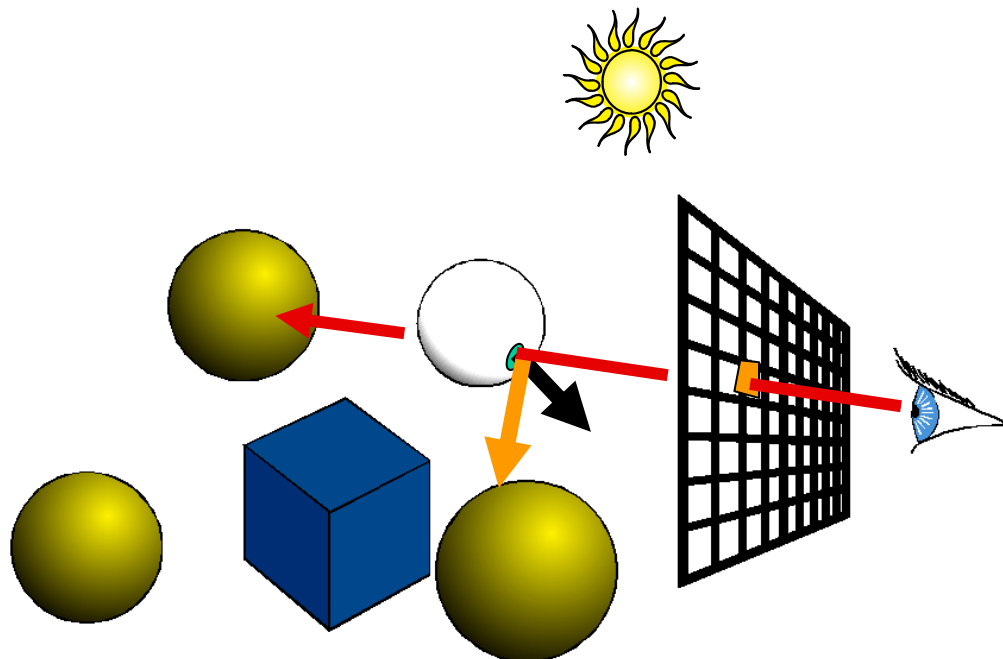


# Mirror Reflection

- Don't forget to add epsilon to the ray



Without epsilon

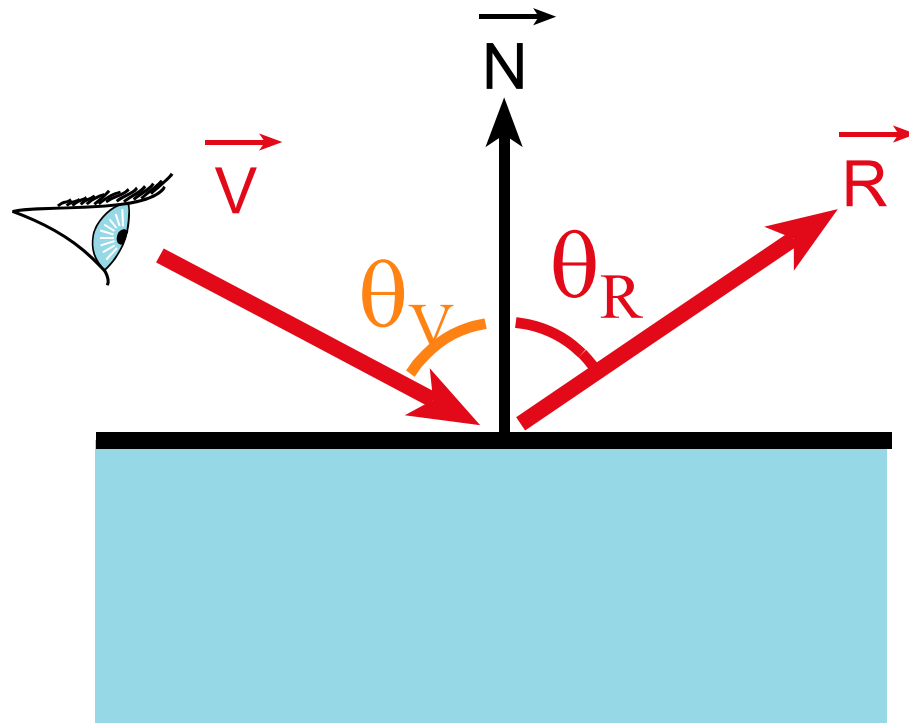


With epsilon

# Reflection

---

- Reflection angle = view angle

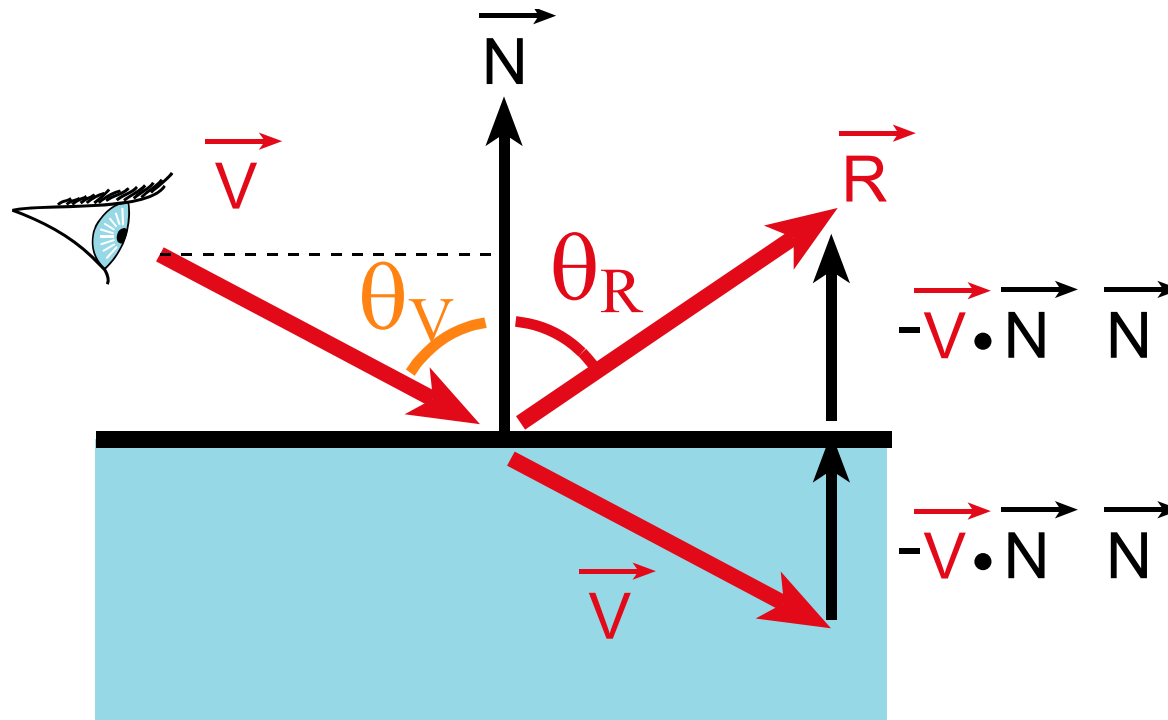


# Reflection

---

- Reflection angle = view angle

$$\vec{R} = \vec{V} - 2(\vec{V} \cdot \vec{N})\vec{N}$$

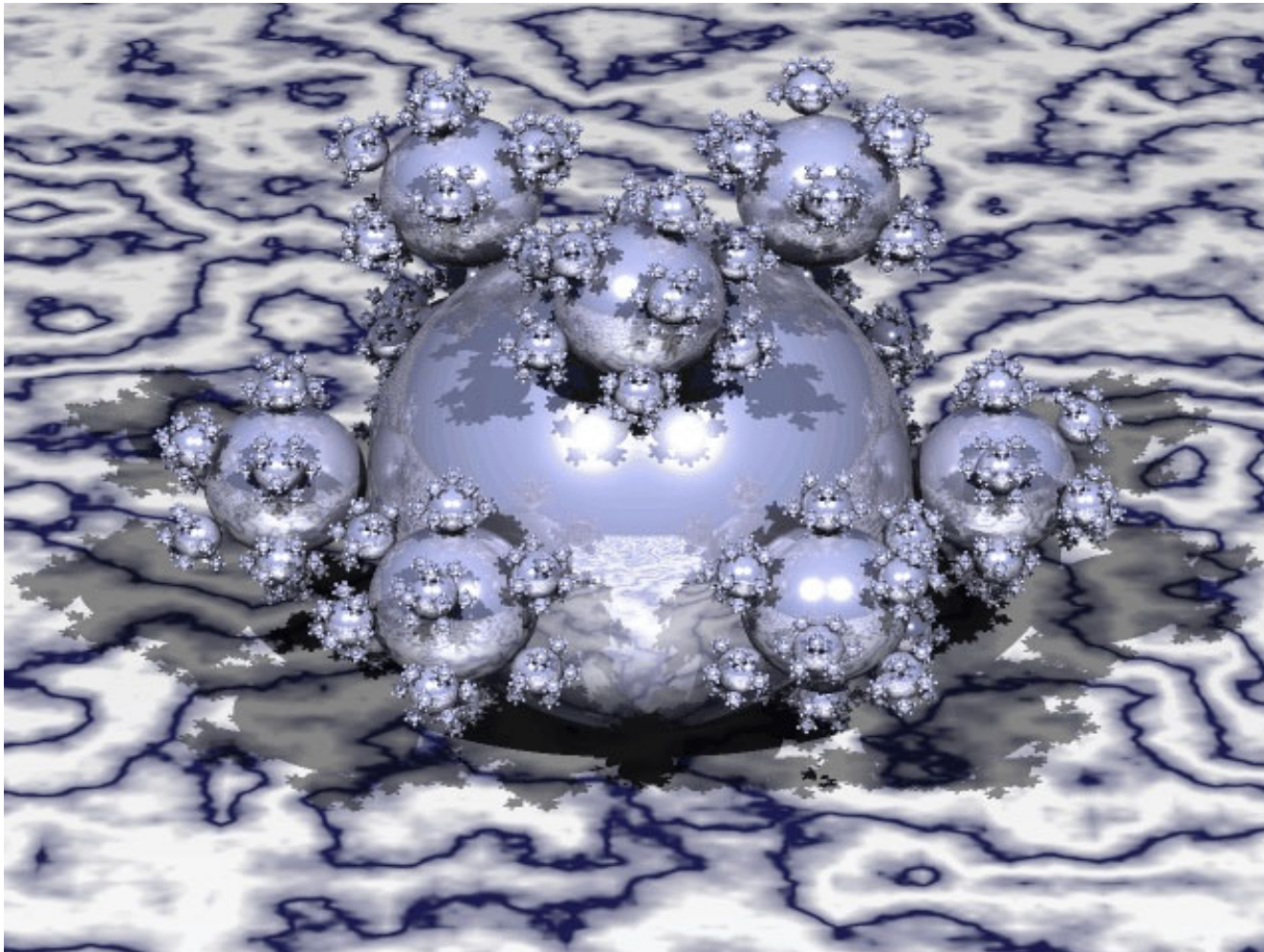




# Questions?

---

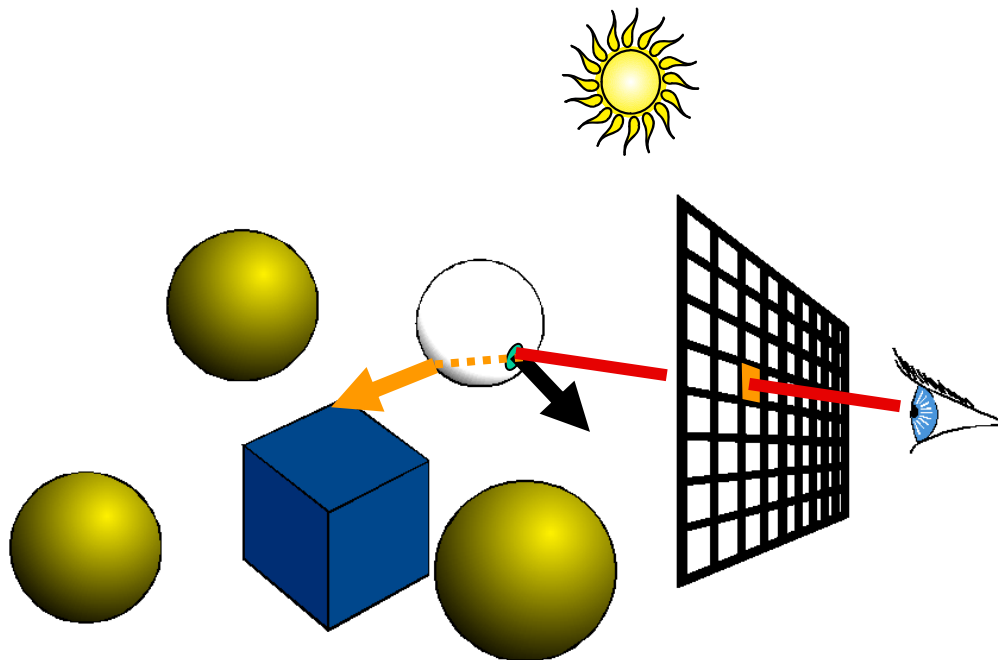
- Image by Henrik Wann Jensen



# Transparency

---

- Compute transmitted contribution
- Cast ray in refracted direction
- Multiply by transparency coefficient (color)



# Qualitative refraction

---

- From “Color and Light in Nature” by Lynch and Livingston

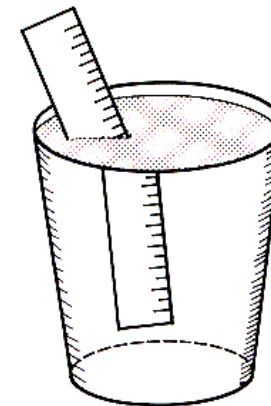
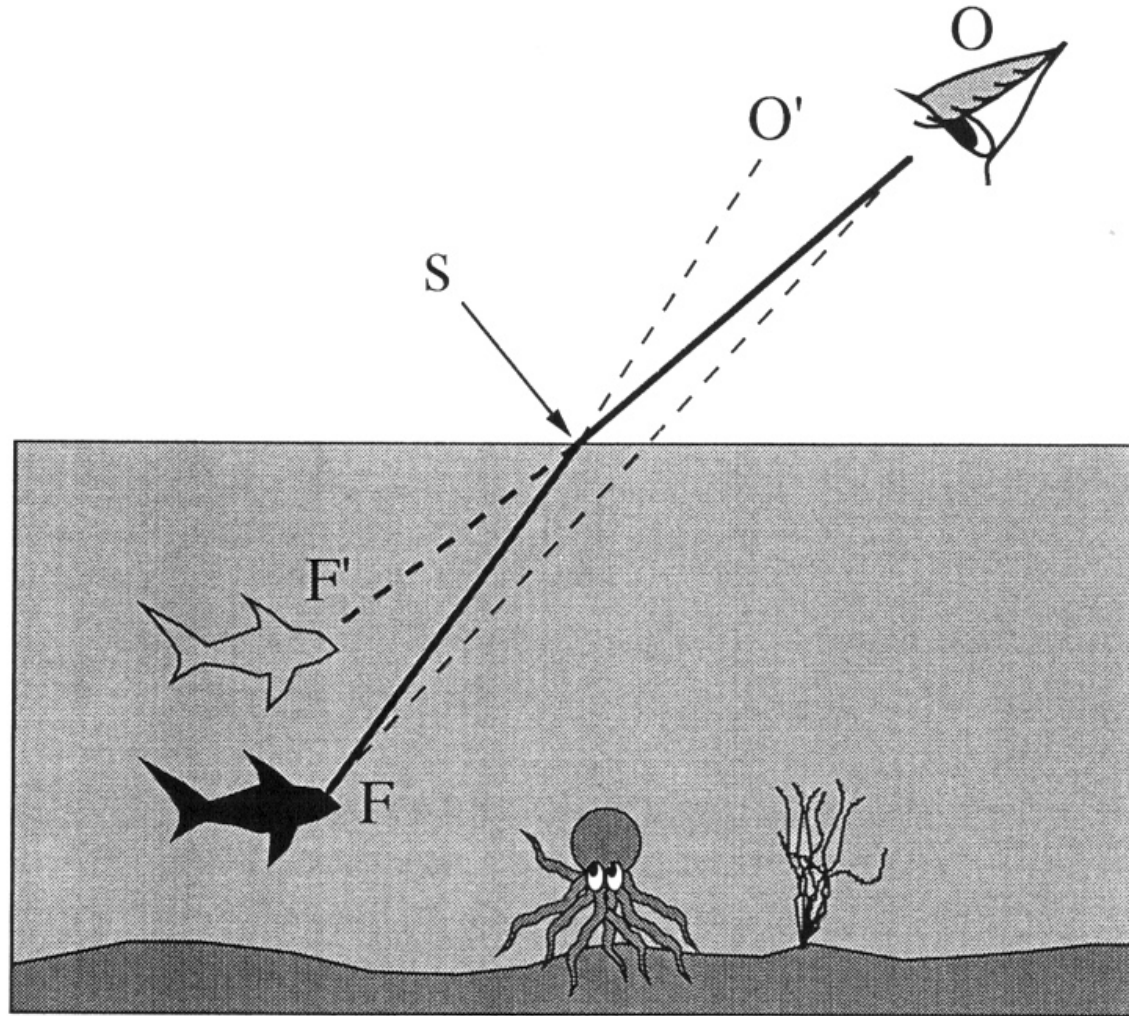


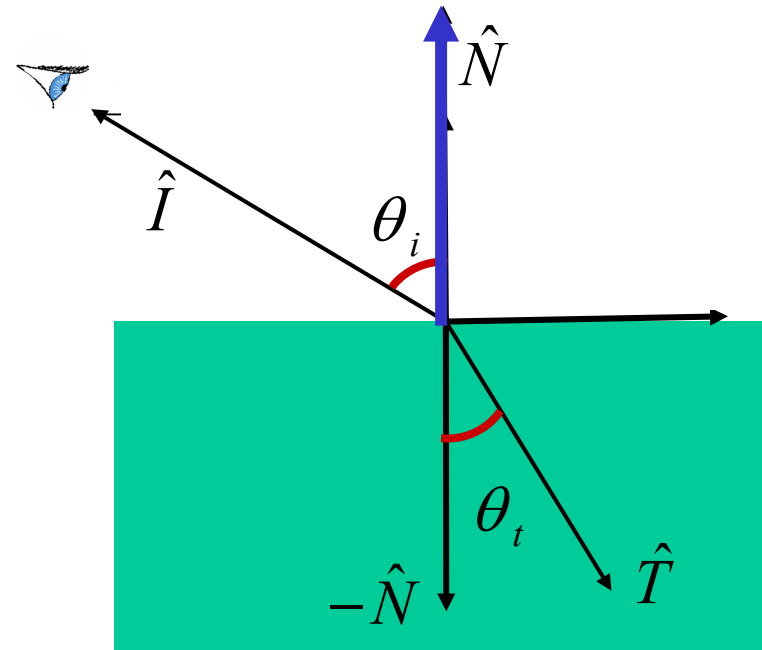
Fig. 9. Refraction causes the ruler to appear bent in a glass of water.

# Refraction

---

Snell-Descartes Law

$$\frac{\sin \theta_i}{\sin \theta_t} = \frac{\eta_t}{\eta_i} = \eta_r$$



Note that  $\hat{I}$  is the negative of the incoming ray



# Total internal reflection

- From “Color and Light in Nature” by Lynch and Livingstone



Fig. 3.7A The optical manhole. From under water, the entire celestial hemisphere is compressed into a circle only  $97.2^\circ$  across. The dark boundary defining the edges of the manhole is not sharp due to surface waves. The rays are analogous to the crepuscular type seen in hazy air, Section 1.9. (Photo by D. Granger)

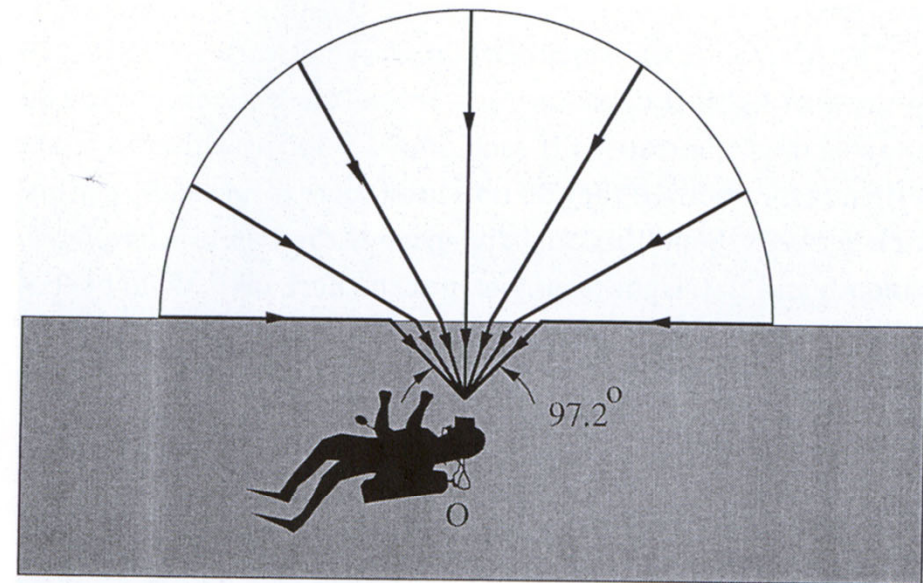
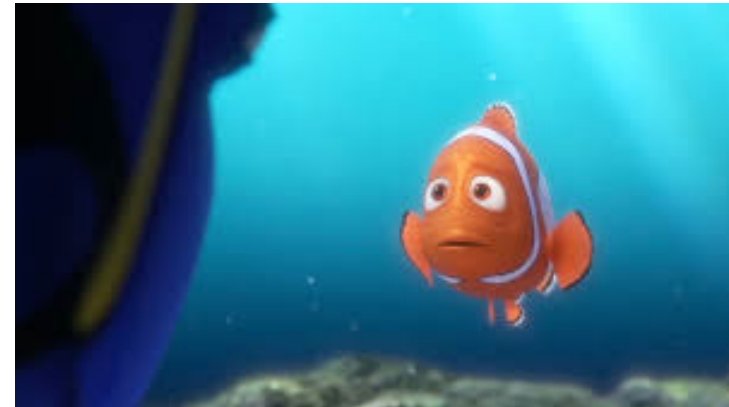


Fig. 3.7B The optical manhole. Light from the horizon (angle of incidence =  $90^\circ$ ) is refracted downward at an angle of  $48.6^\circ$ . This compresses the sky into a circle with a diameter of  $97.2^\circ$  instead of its usual  $180^\circ$ .





# Wavelength

---

- Refraction is wavelength-dependent
- Newton's experiment
- Usually ignored in graphics



Pink Floyd, *The Dark Side of the Moon*

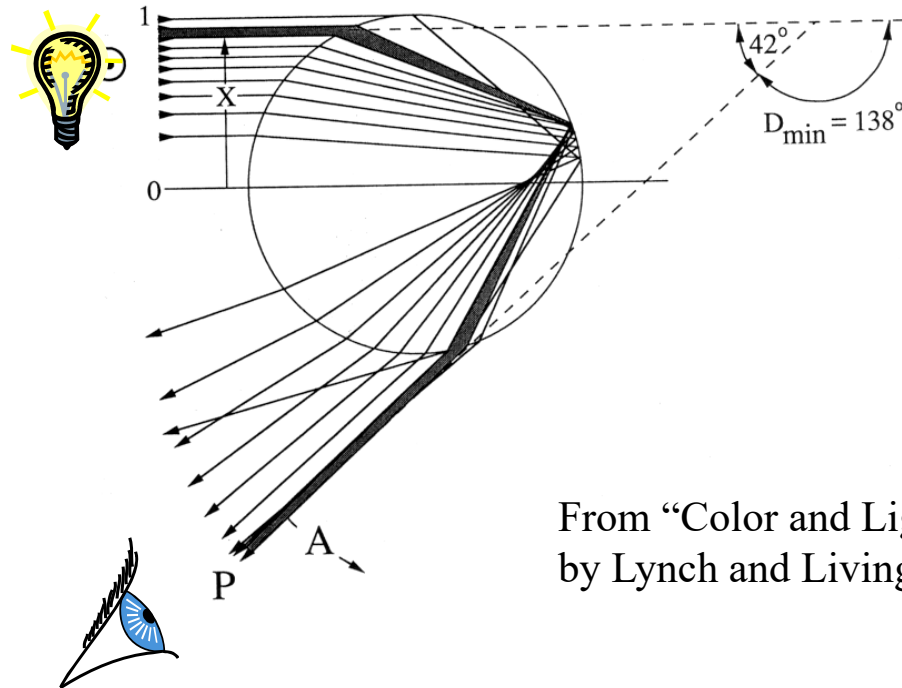


Pittoni, 1725, Allegory to Newton

# Rainbow

- Refraction depends on wavelength
- Rainbow is caused by refraction+internal reflection+refraction
- Maximum for angle around 42 degrees

*Digression*



From "Color and Light in Nature"  
by Lynch and Livingstone







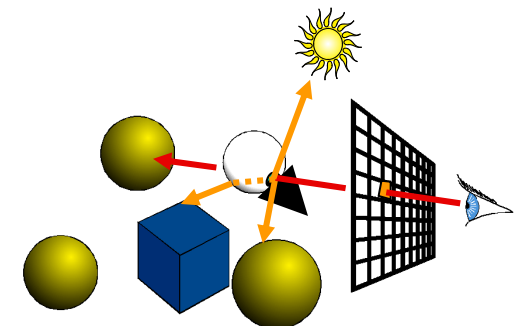
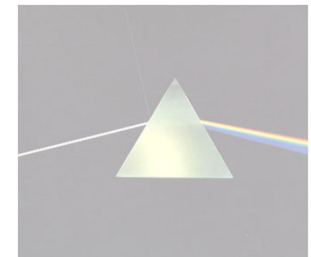
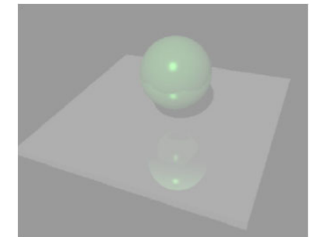
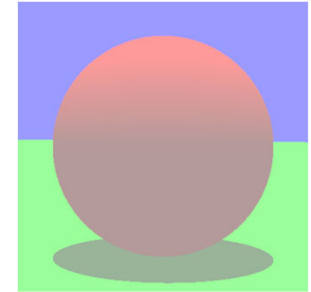




# Overview of today

---

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing





# Recap: Ray Tracing

---

**traceRay**

**Intersect all objects**

**Ambient shading**

**For every light**

**Shadow ray**

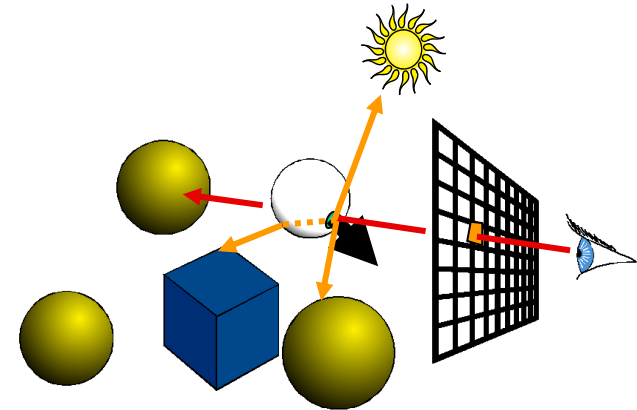
**shading**

**If mirror**

**Trace reflected ray**

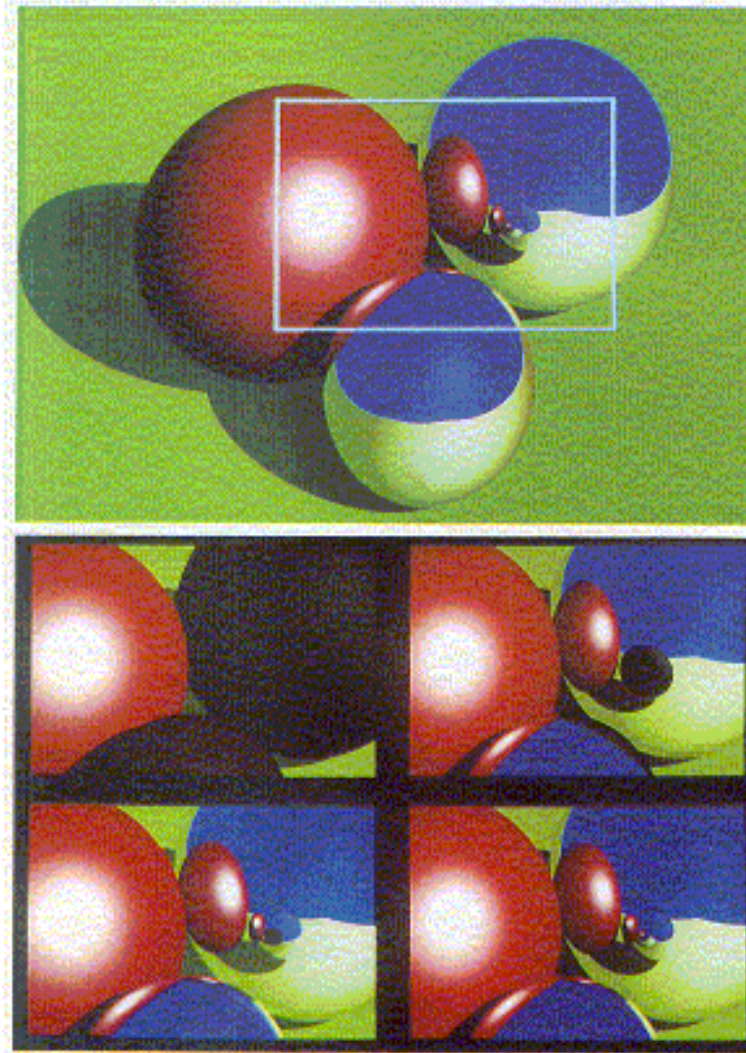
**If transparent**

**Trace transmitted ray**



# The depth of reflection

---



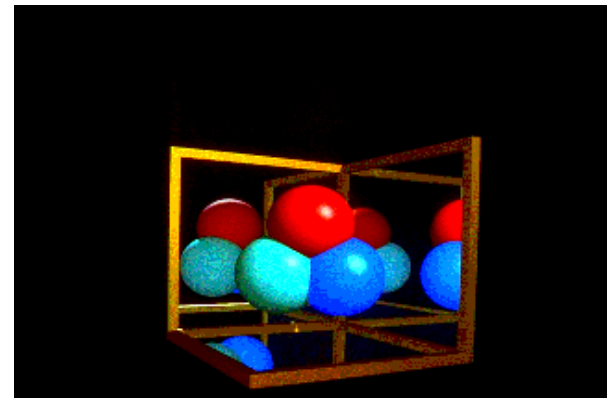
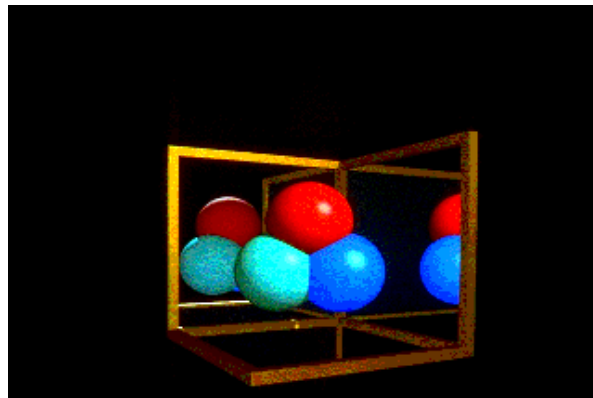
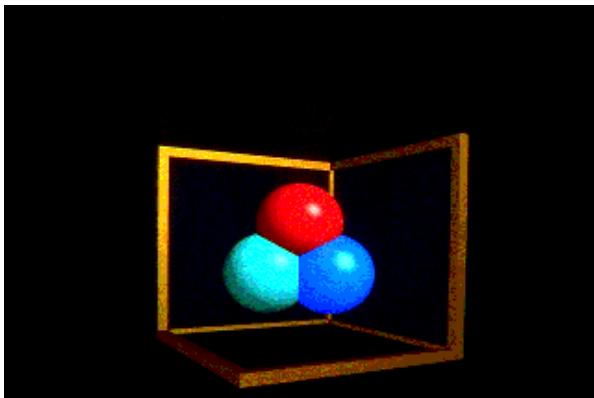
# Avoiding infinite recursion

---

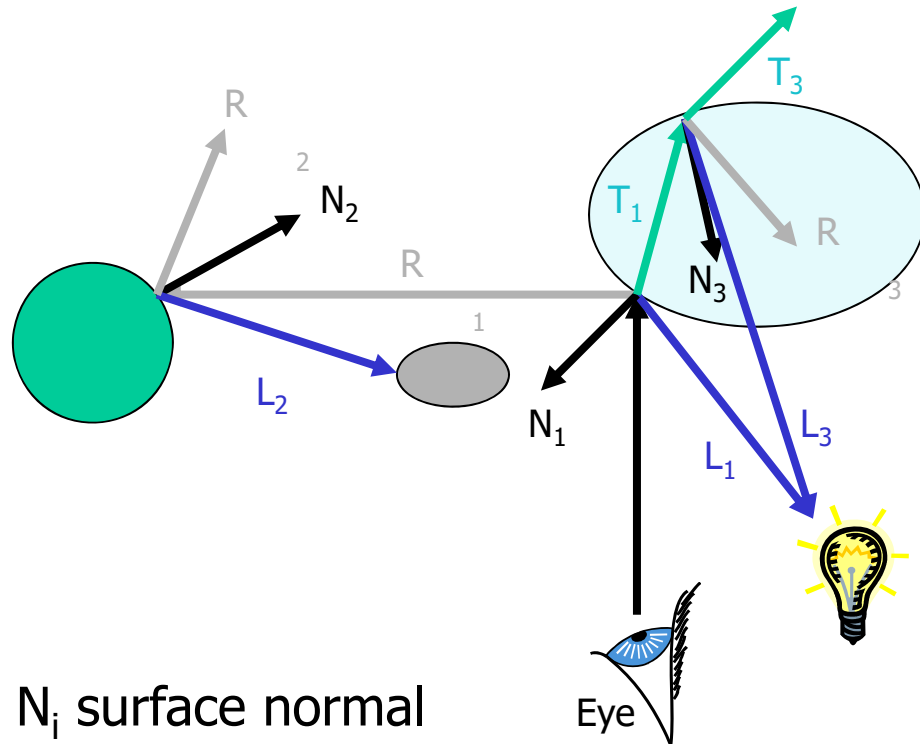
Stopping criteria:

- Recursion depth
  - Stop after a number of bounces
- Ray contribution
  - Stop if transparency/transmitted attenuation becomes too small

Usually do both



# The Ray Tree

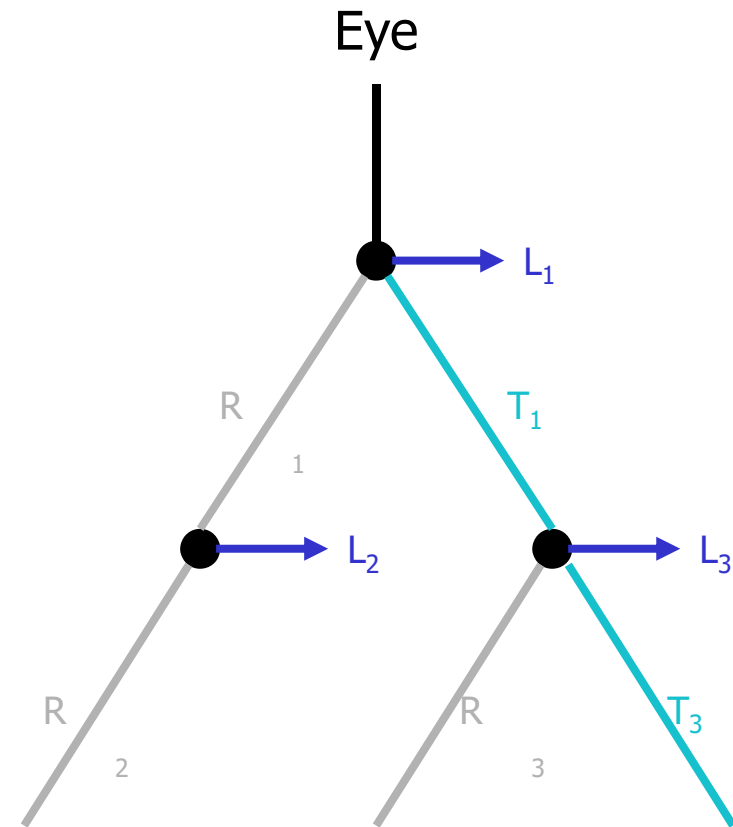


$N_i$  surface normal

$R_i$  reflected ray

$L_i$  shadow ray

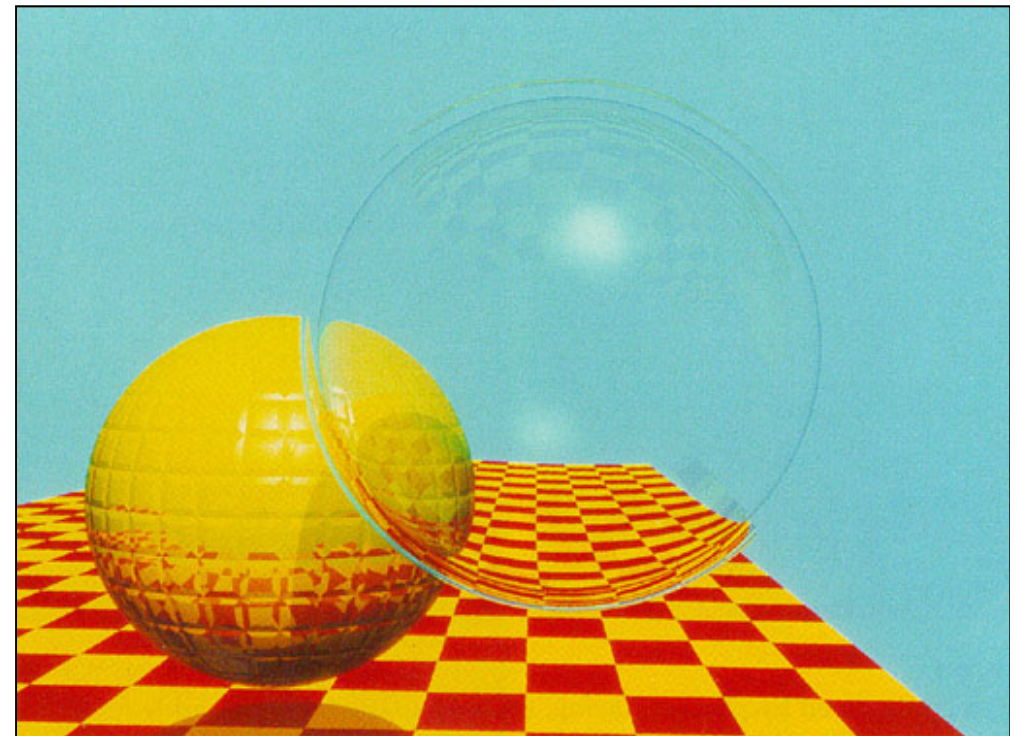
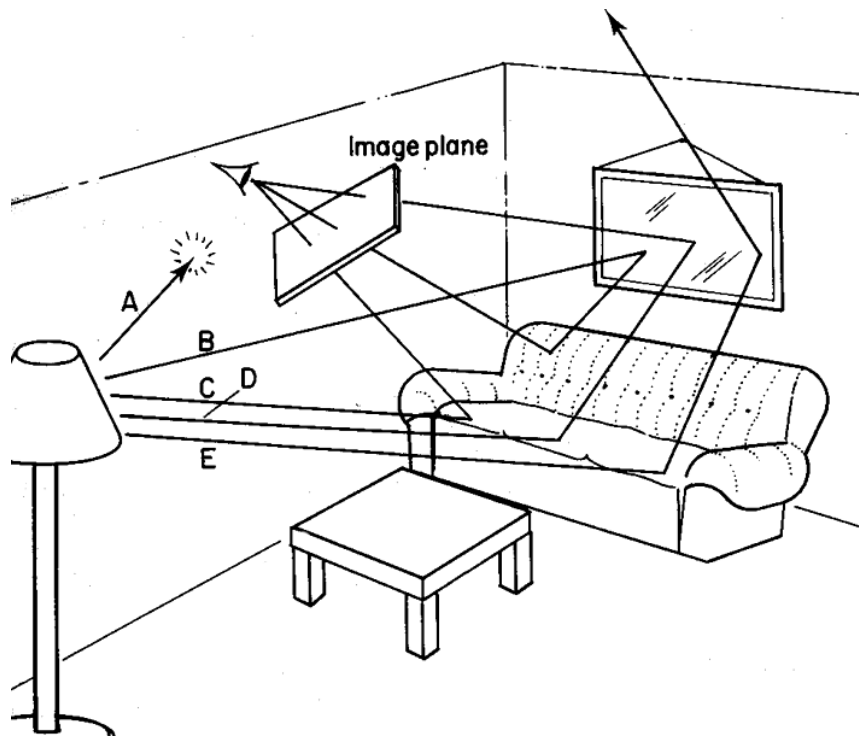
$T_i$  transmitted (refracted) ray



# Ray Tracing History

---

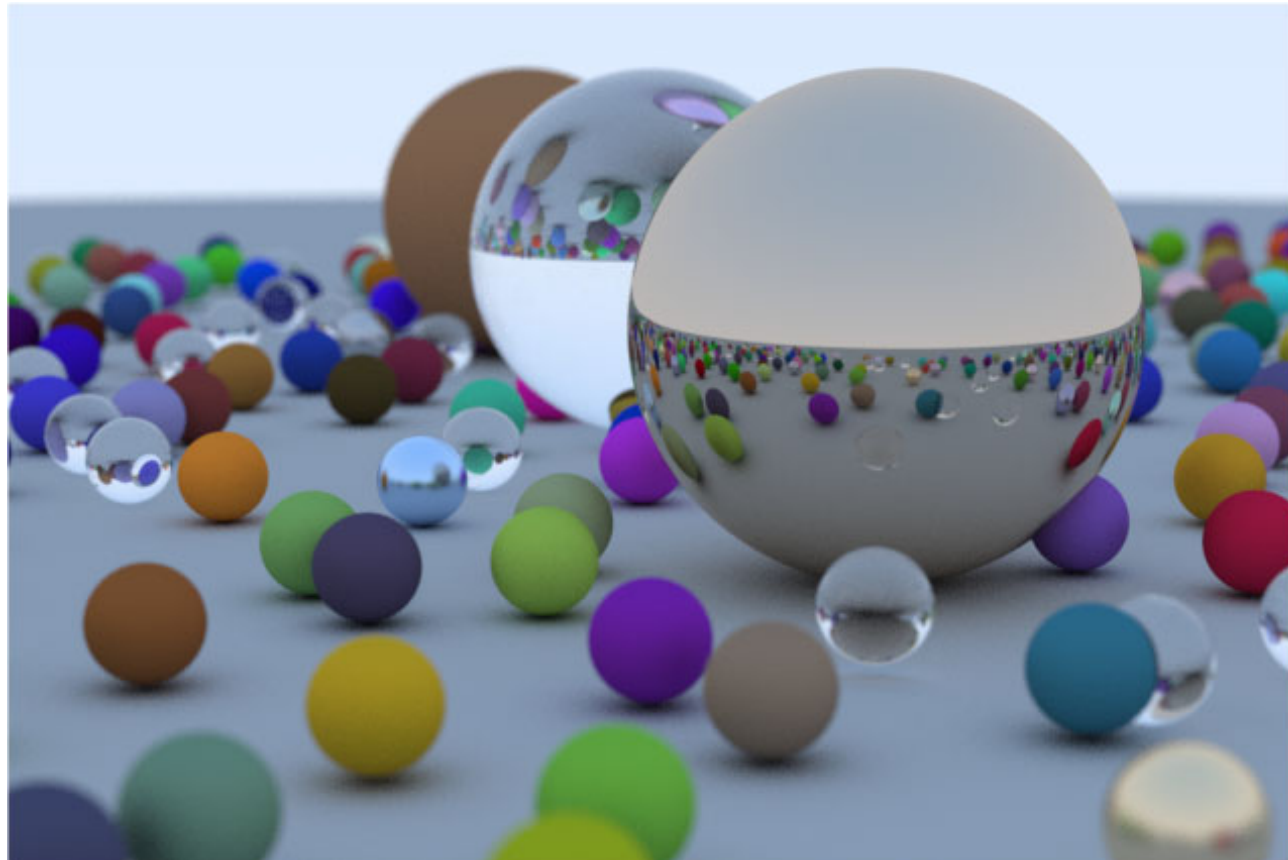
- Ray Casting: Appel, 1968
- CSG and quadrics: Goldstein & Nagel 1971
- Recursive ray tracing: Whitted, 1980







*Mirror morphine* This scene is composed entirely of spheres: the 40-sphere morphine molecule is tucked in the corner between two large mirrored balls and the yellow ground ball. The image was calculated at a resolution of  $2048 \times 2048$  with 10 levels of reflections,  $3 \times 3$  supersampling, and analytic penumbra calculations (not probabilistic methods), in 8 days of VAX 11/780 time. For a discussion of shadows and penumbræ, see Section 5.1. (Copyright © Paul Heckbert, NYIT, 1983)

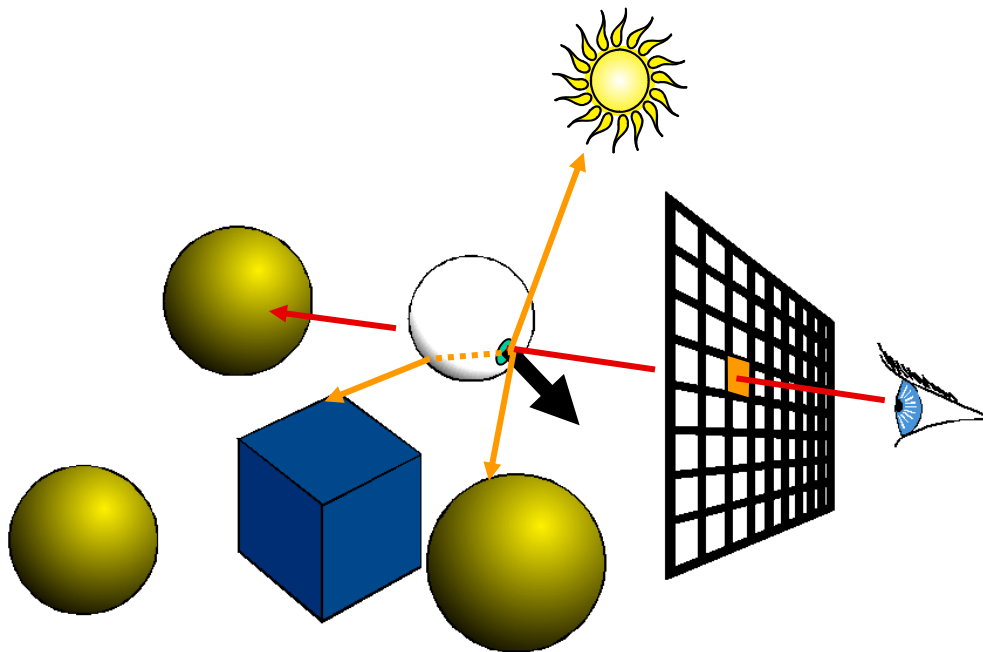




# Does Ray Tracing simulate physics?

---

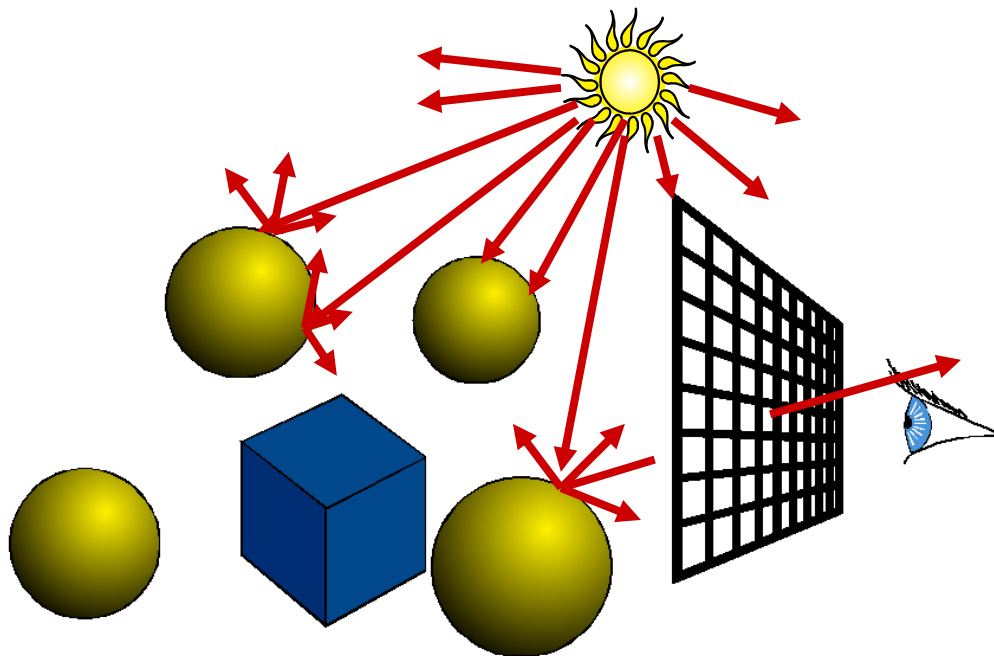
- Photons go from the light to the eye, not the other way
- What we do is backward ray tracing



# Forward ray tracing

---

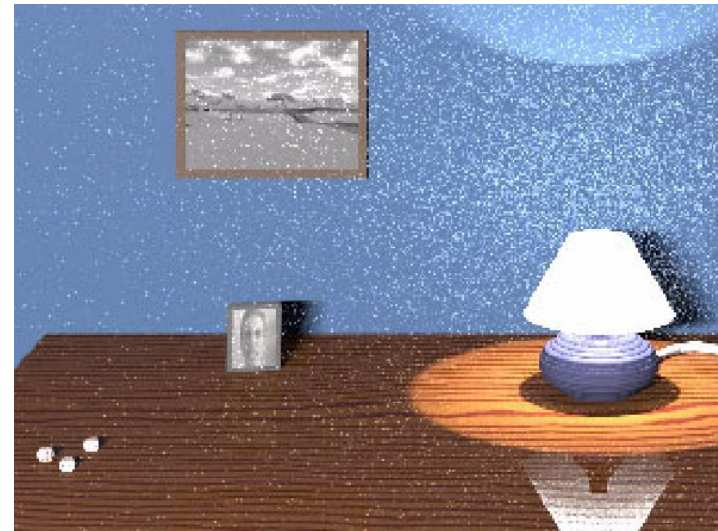
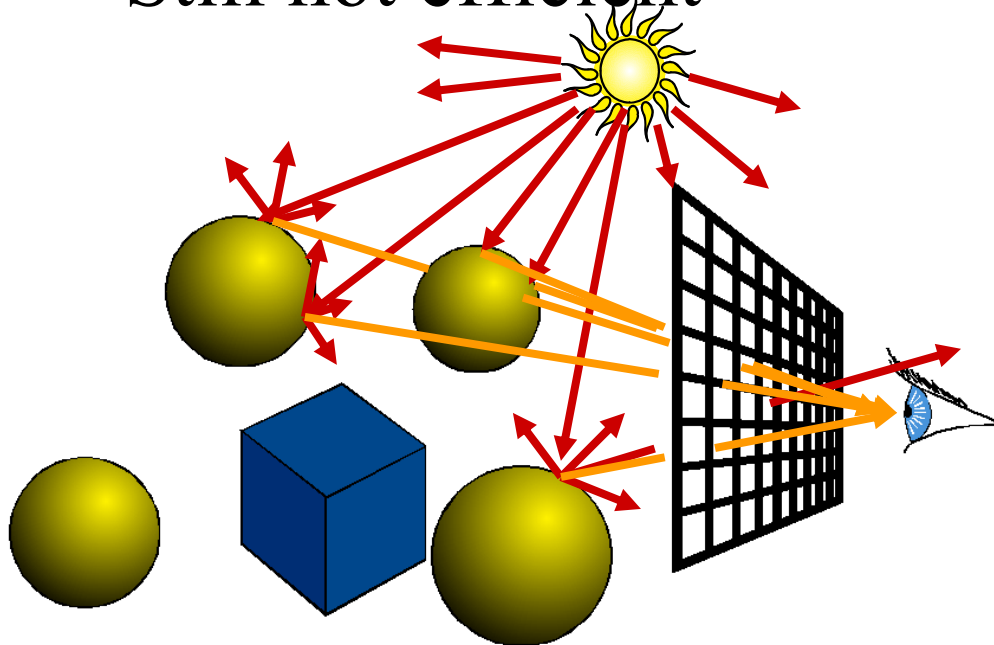
- Start from the light source
- But low probability to reach the eye
  - What can we do about it?



# Forward ray tracing

---

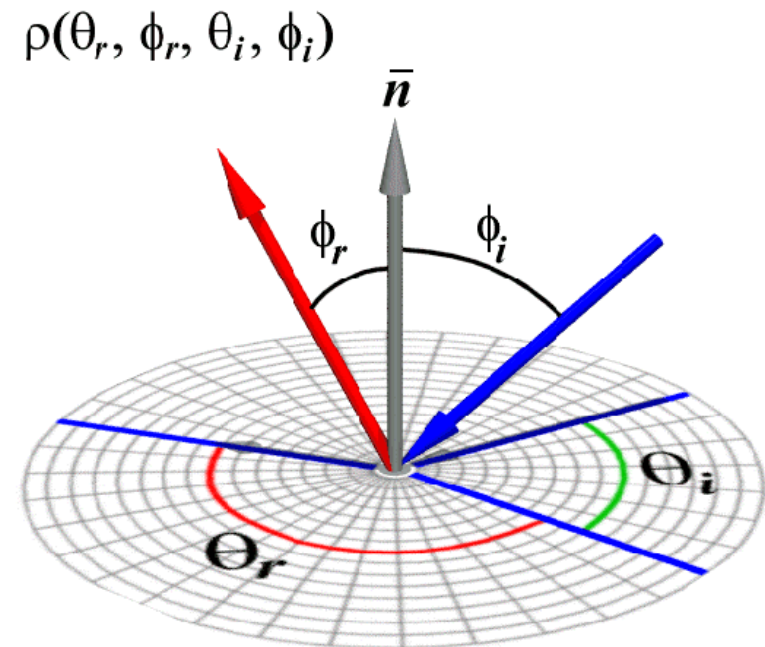
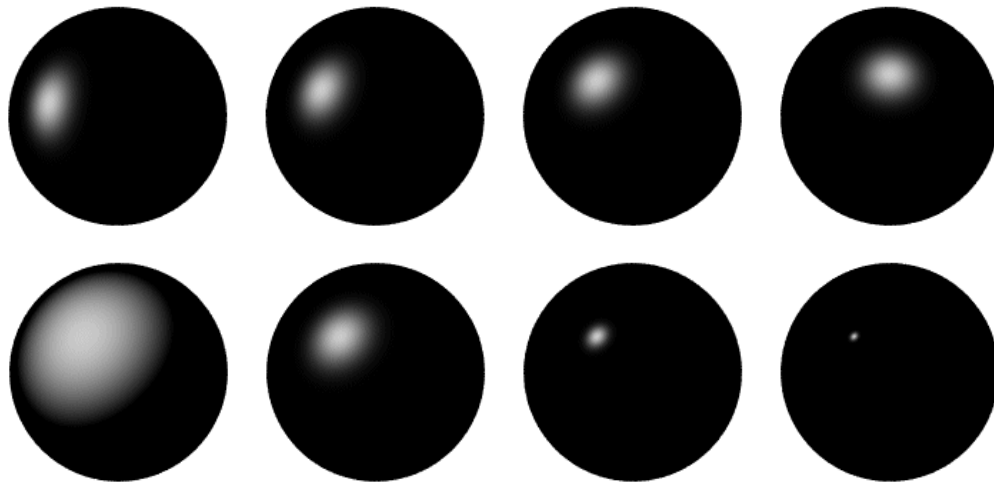
- Start from the light source
- But low probability to reach the eye
  - What can we do about it?
  - Always send a ray to the eye
- Still not efficient



# BRDF

---

- Reflectance properties, shading and BRDF



# Material

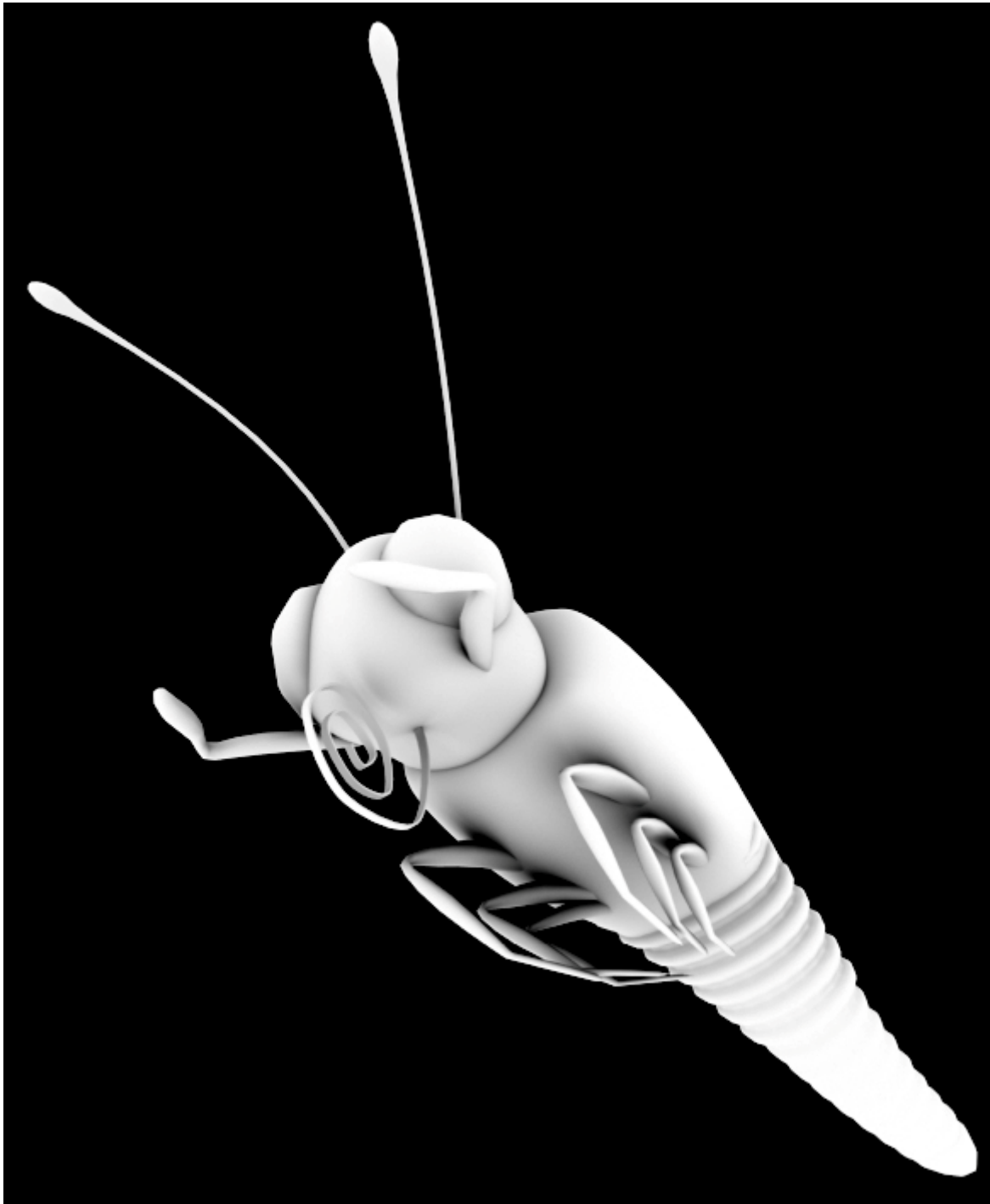
---



# Ambient Occlusion

---

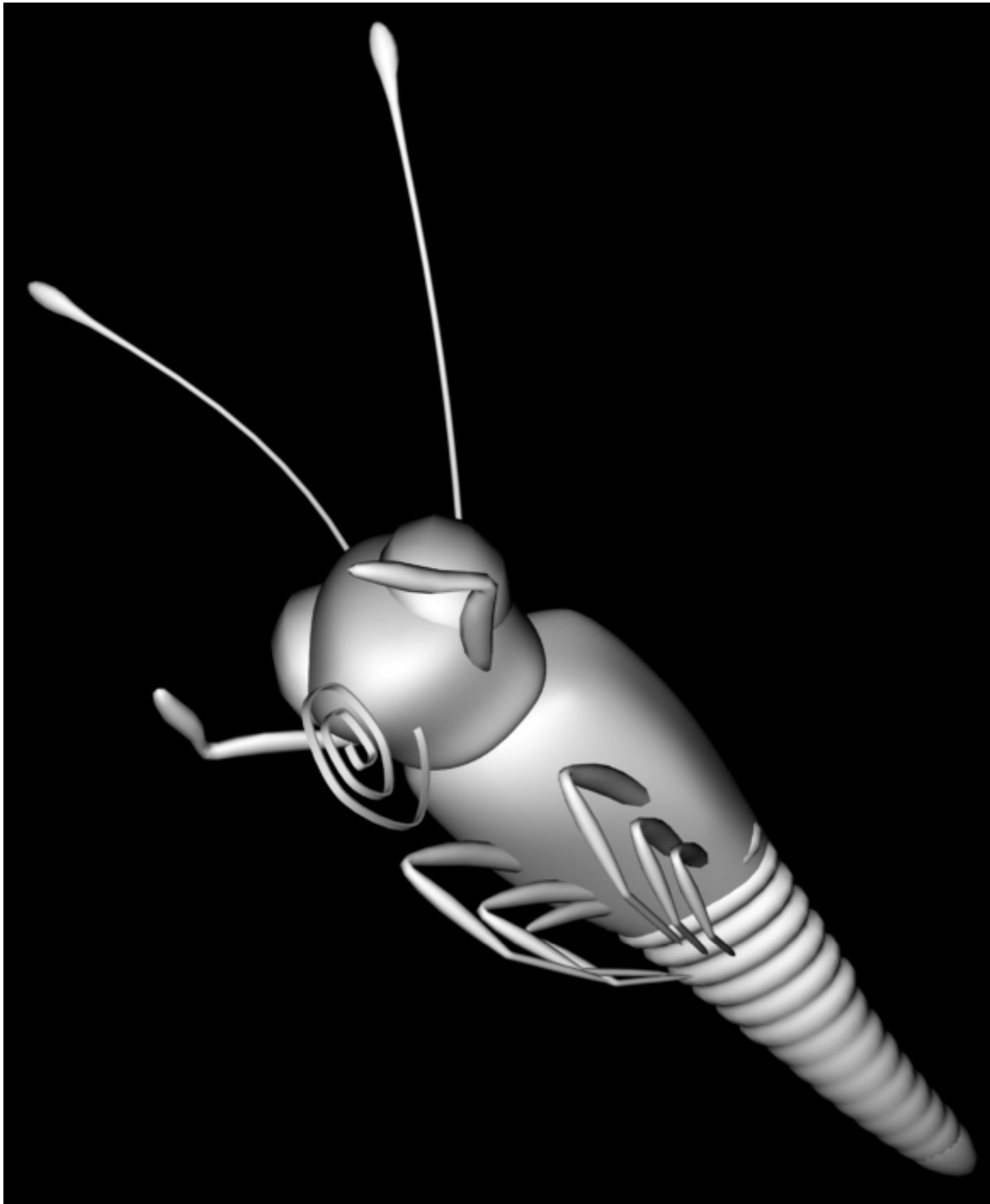




---

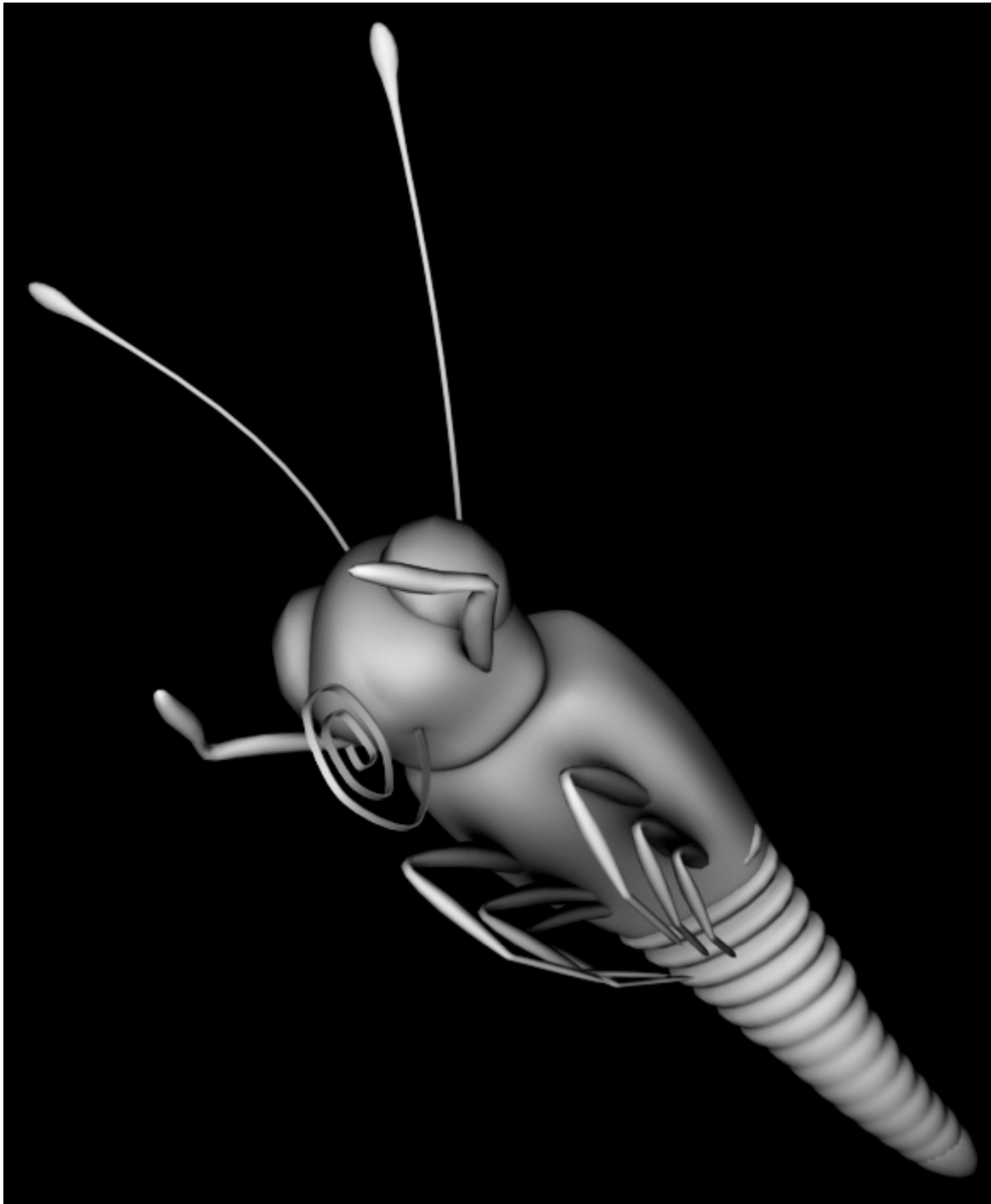
## **Ambient Occlusion**





---

**Diffuse Only**

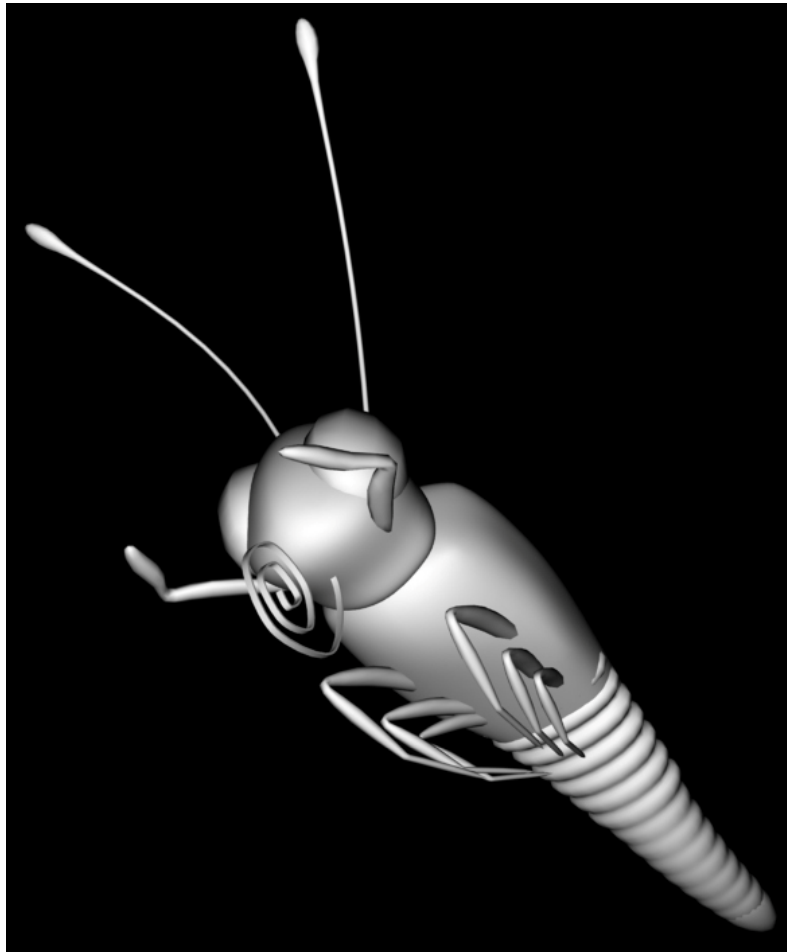


---

## **Diffuse and Ambient**

---

**Diffuse Only**



**Diffuse and Ambient**

