



3D Modeling

0368-3236, Spring 2019

Tel-Aviv University

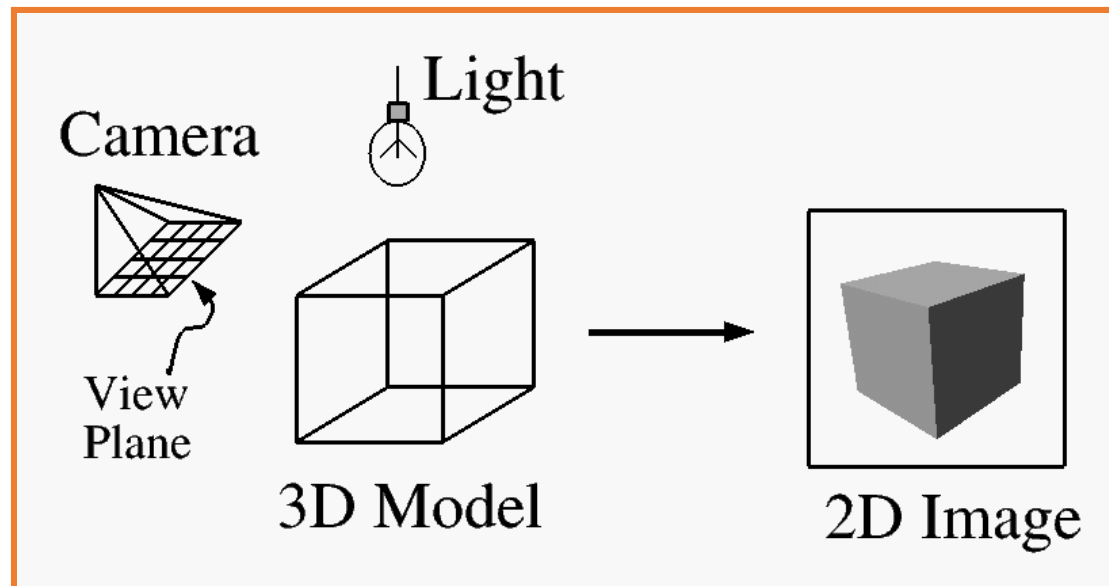
Amit Bermano

What is 3D Modeling?



Topics in computer graphics

- Imaging = *representing & manipulating 2D images*
- Rendering = *constructing 2D images from 3D models*
- Modeling = *representing & manipulating 3D objects*
- Animation = *simulating changes over time*

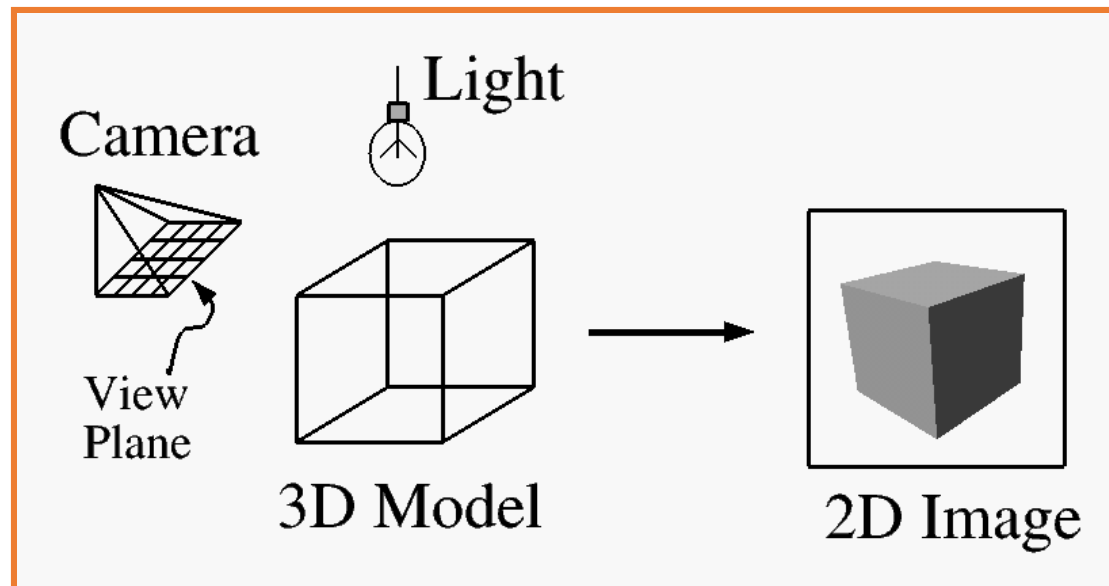


What is 3D Modeling?



Topics in computer graphics

- Imaging = *representing & manipulating 2D images*
- Rendering = *constructing 2D images from 3D models*
- **Modeling** = *representing & manipulating 3D objects*
- Animation = *simulating changes over time*



Modeling



Blender demoreel 2018/2019

<https://www.youtube.com/watch?v=HBwtw3J4mhA>

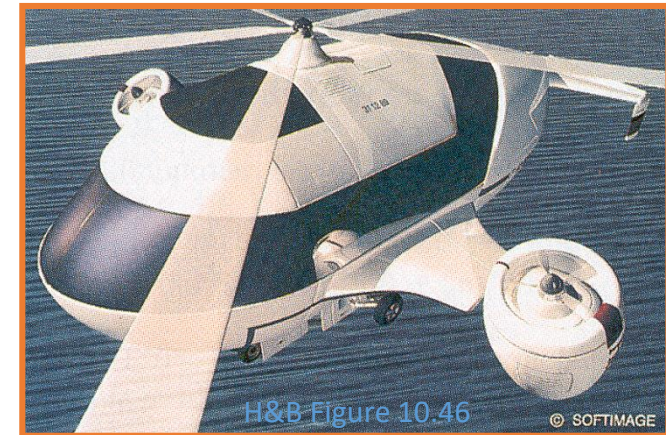
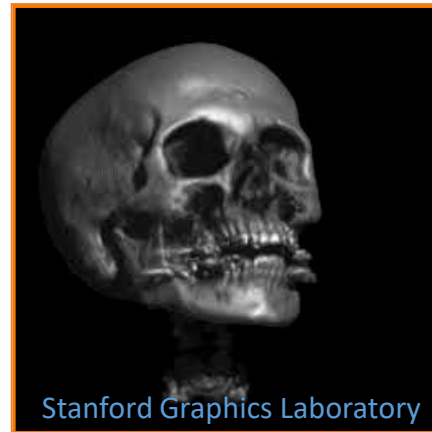
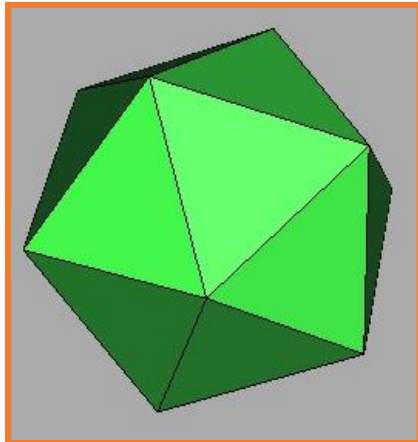
Blender

Modeling

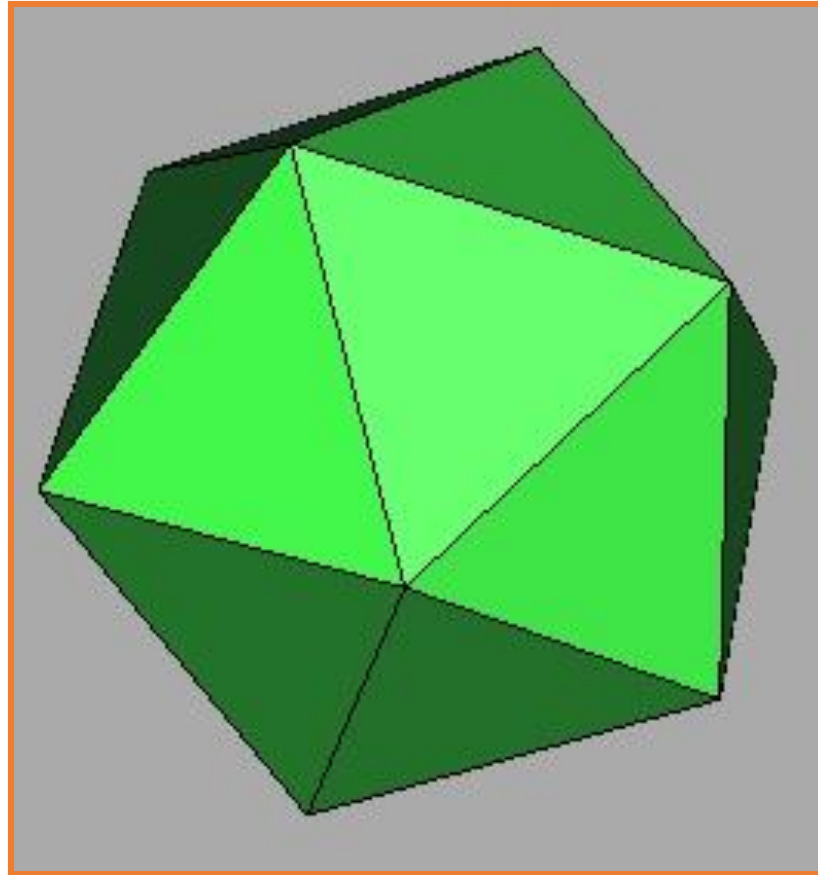


How do we ...

- Represent 3D objects in a computer?
- Acquire computer representations of 3D objects?
- Manipulate computer representations of 3D objects?

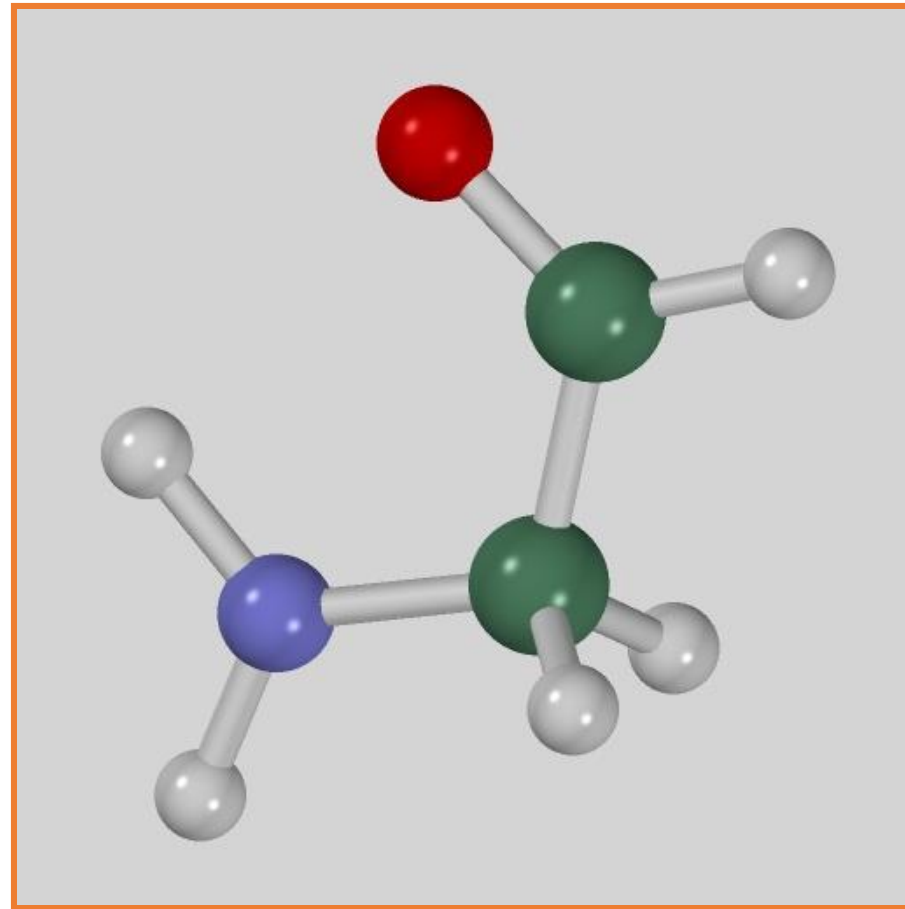


3D Object Representations



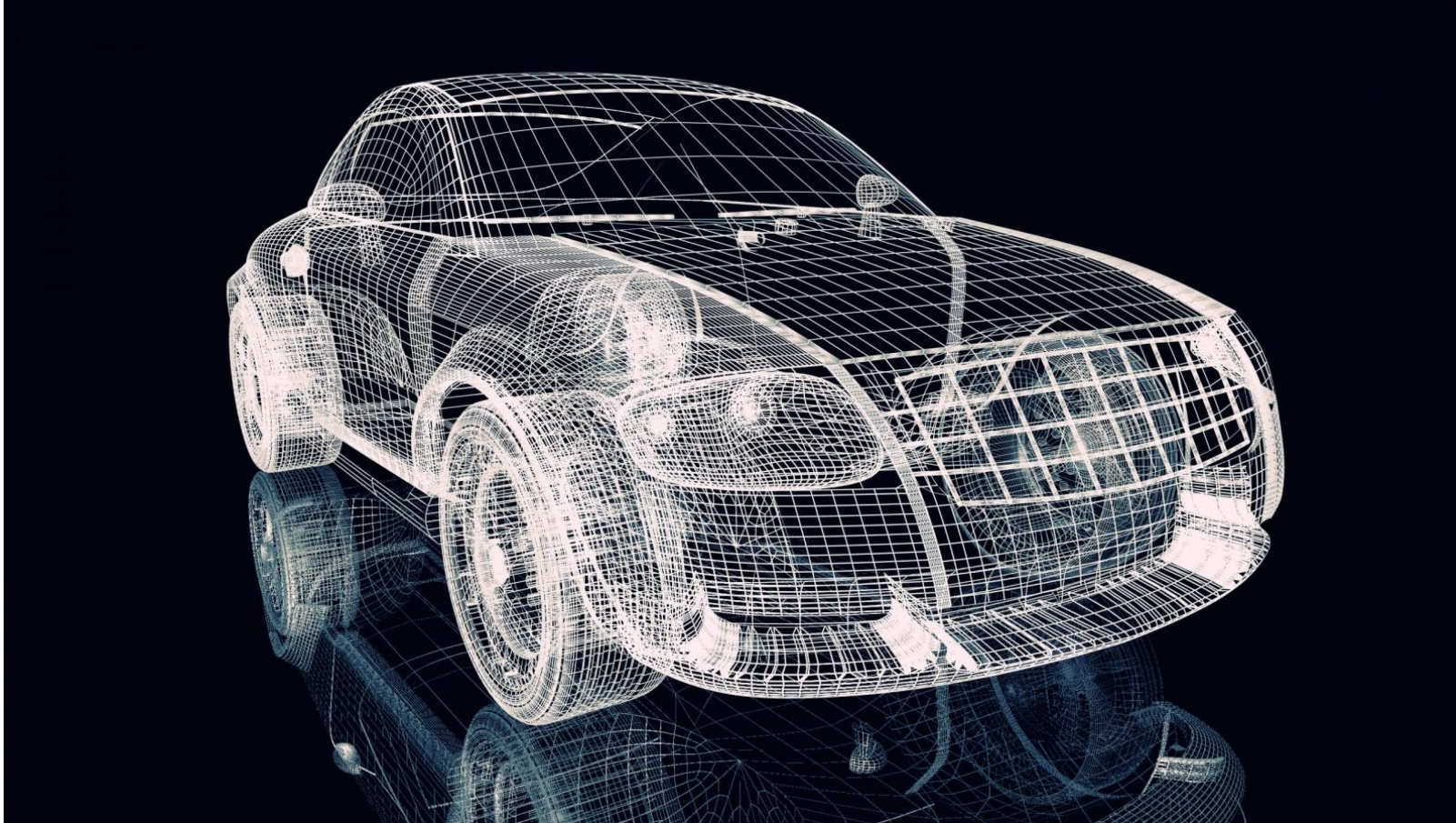
How can this object be represented in a computer?

3D Object Representations



How about this one?

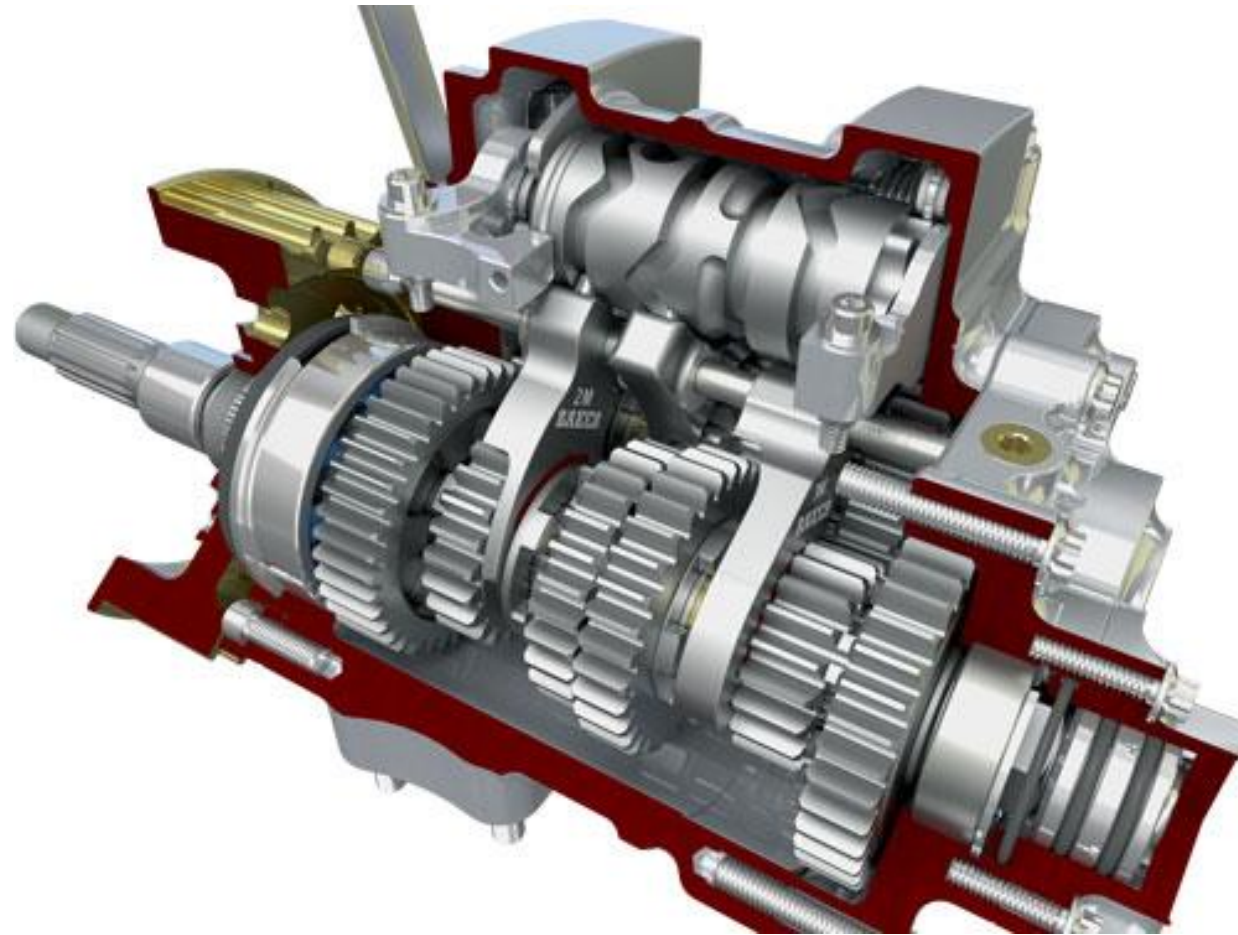
3D Object Representations



Wallpaperonly.net

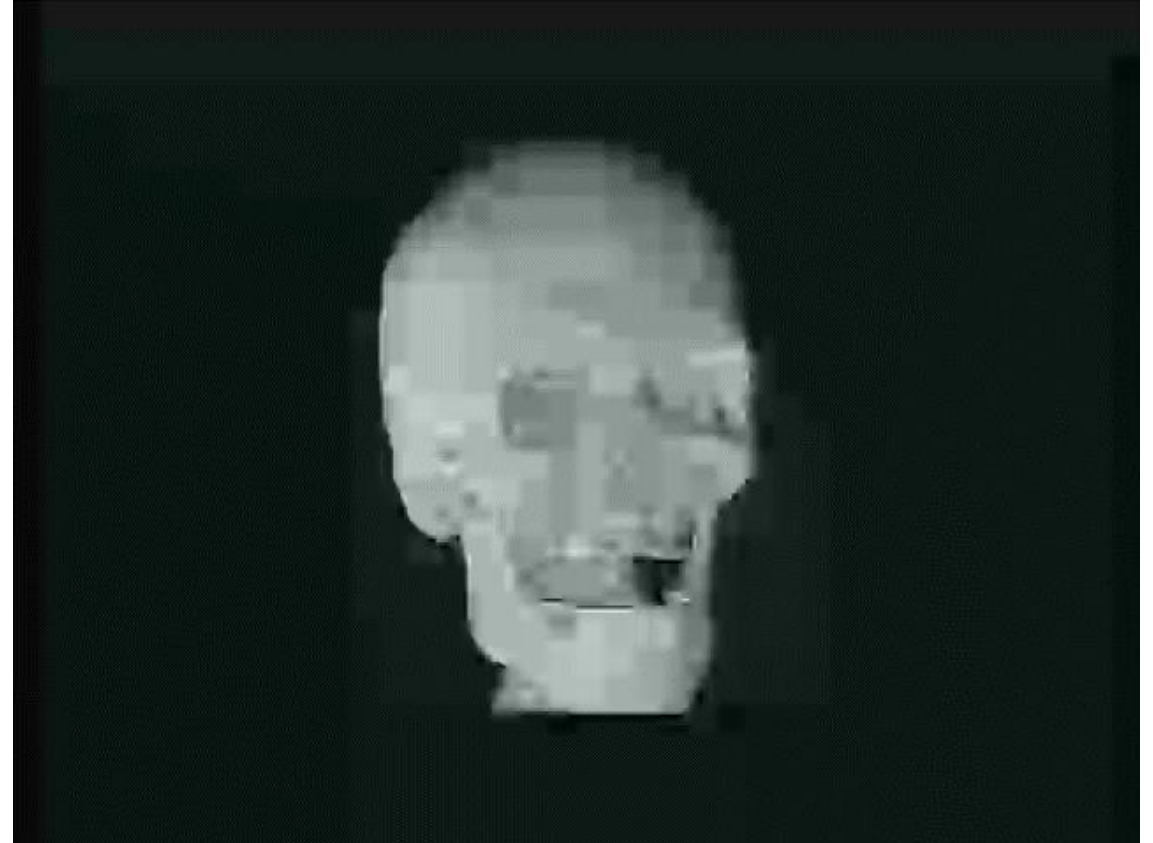
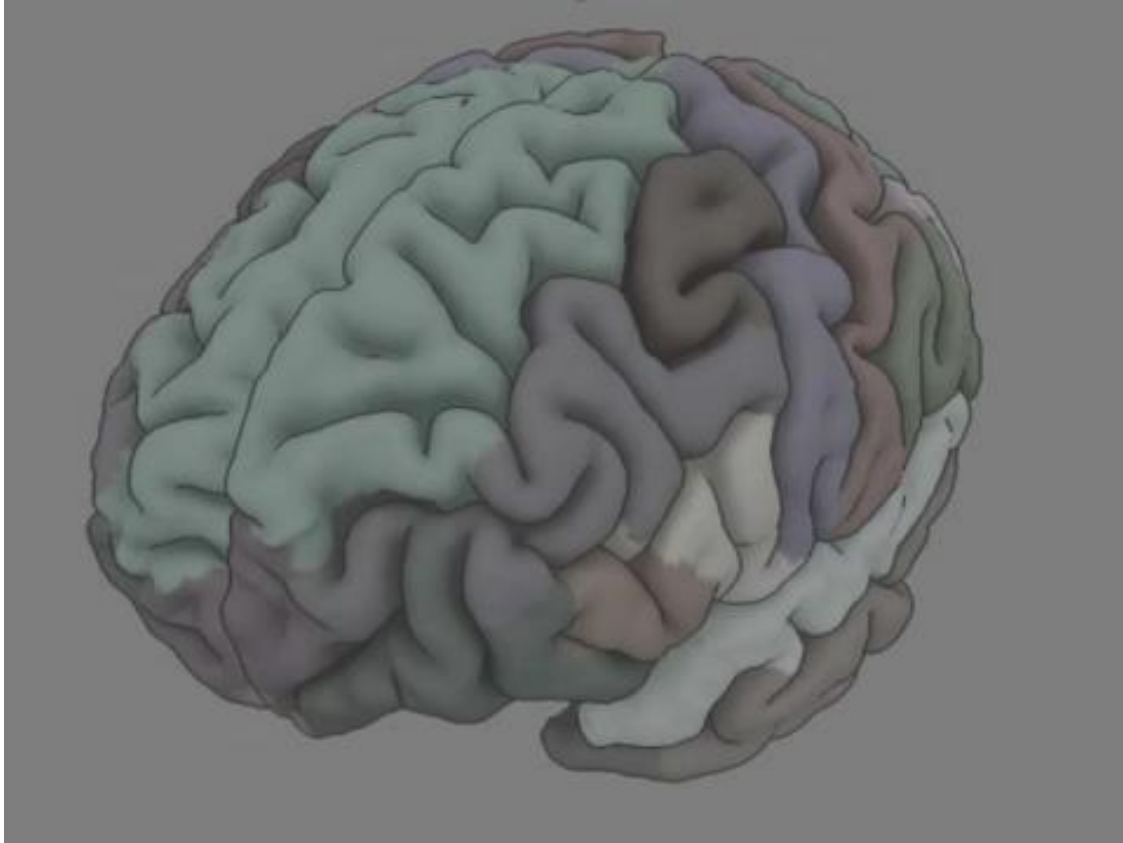
And this one?

3D Object Representations



This one? Solidworks

3D Object Representations

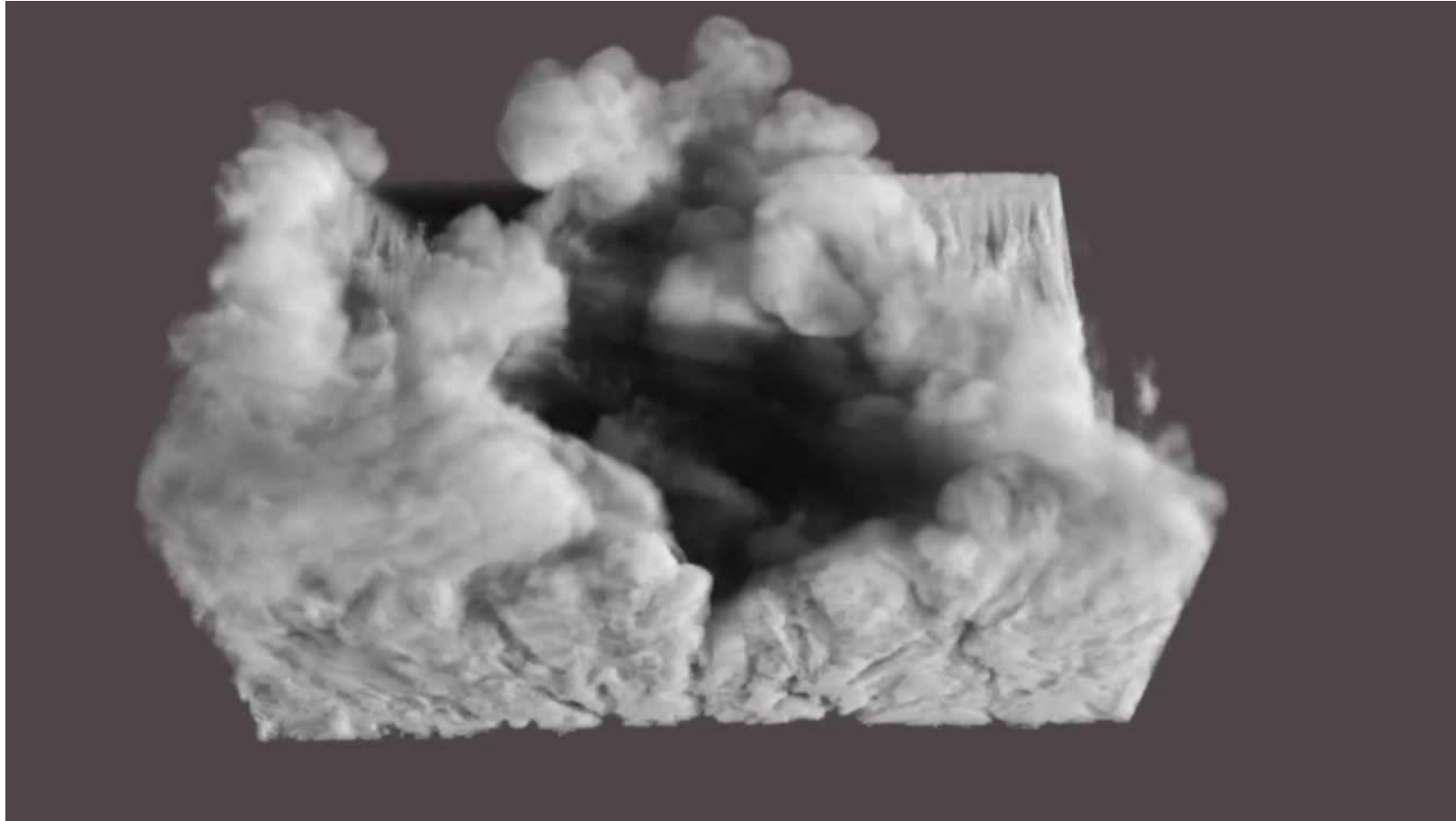


<https://www.youtube.com/watch?v=0gmJYugUU8>

This one?

The visible human

3D Object Representations



FumeFx

This one?

3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Equivalence of Representations



Thesis:

- Each representation has enough expressive power to model the shape of any geometric object
- It is possible to perform all geometric operations with any fundamental representation

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation

Data structures determine algorithms

Why Different Representations?



Efficiency for different tasks

- Acquisition
 - Computer Vision
- Rendering
- Analysis
- Manipulation
- Animation



Indiana University



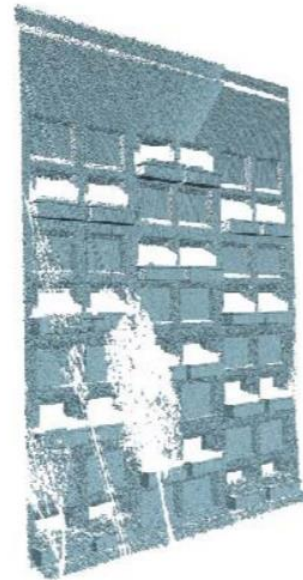
© 2012 CRS Interactive

Why Different Representations?



Efficiency for different tasks

- Acquisition
 - Range Scanning
- Rendering
- Analysis
- Manipulation
- Animation

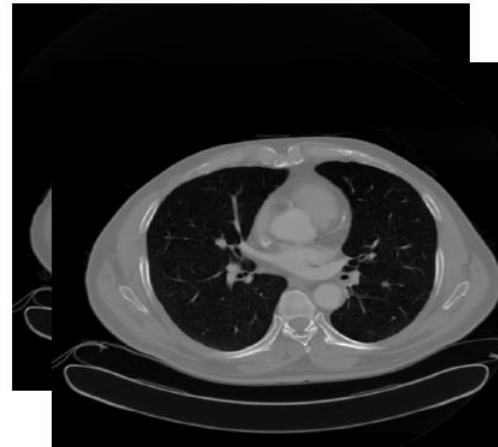


Why Different Representations?



Efficiency for different tasks

- Acquisition
 - Tomography
- Rendering
- Analysis
- Manipulation
- Animation



DGP course notes, Technion

Why Different Representations?



Efficiency for different tasks

- Acquisition
- **Rendering**
 - **Intersection**
- Analysis
- Manipulation
- Animation

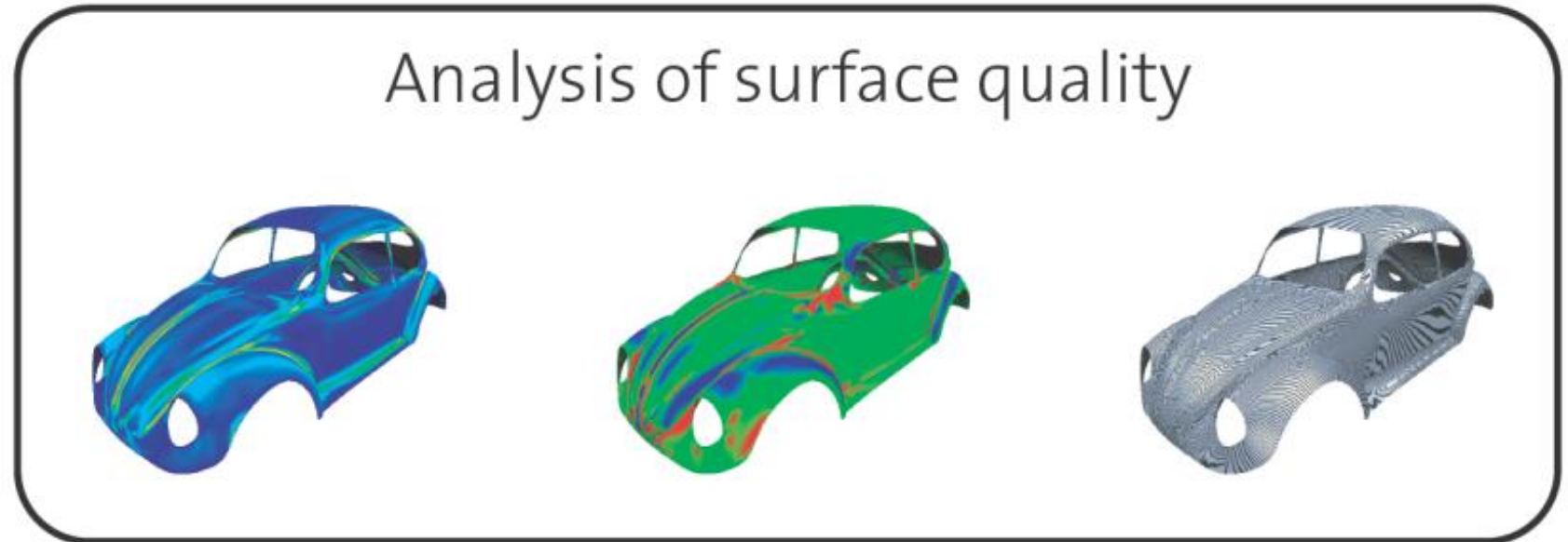


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Curvature, smoothness**
- Manipulation
- Animation



DGP course notes, Technion

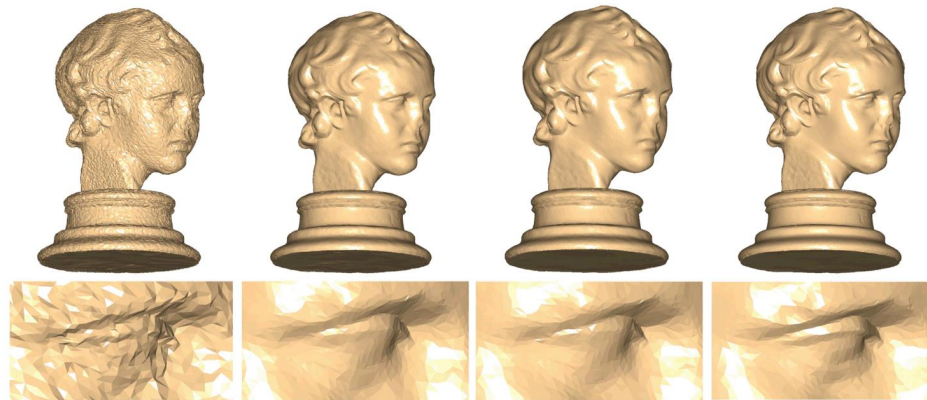
Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Fairing**
- Manipulation
- Animation

Surface smoothing for noise removal



DGP course notes, Technion

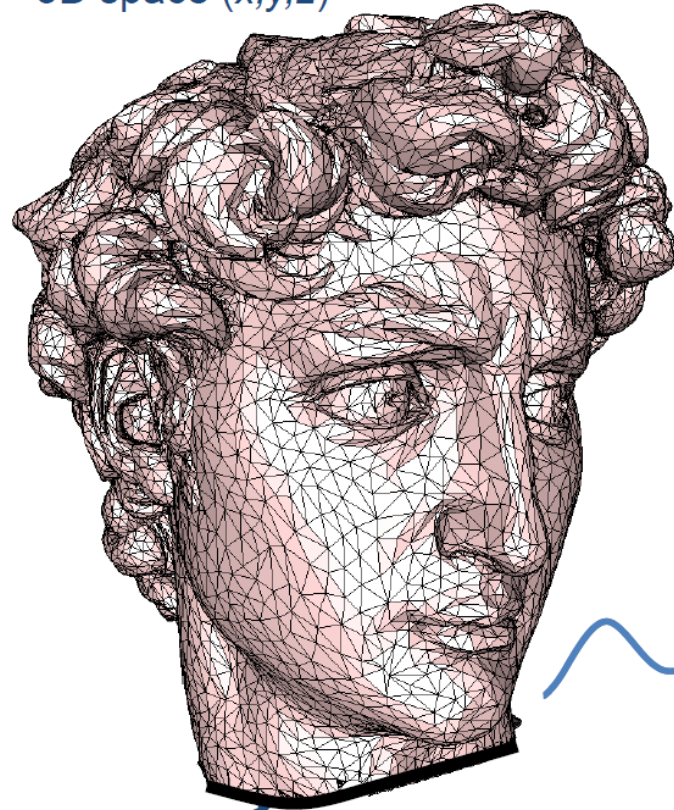
Why Different Representations?



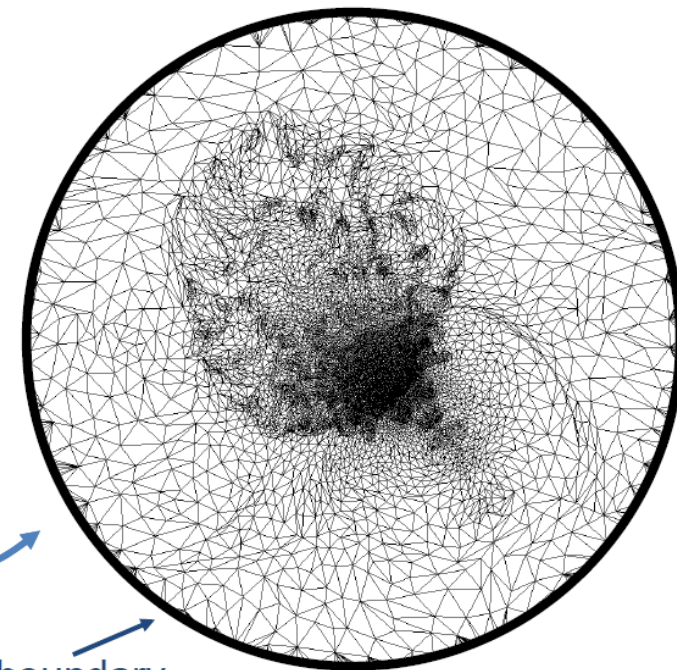
Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Parametrization**
- Manipulation
- Animation

3D space (x,y,z)



2D parameter domain (u,v)



boundary

boundary

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Texture mapping**
- Manipulation
- Animation

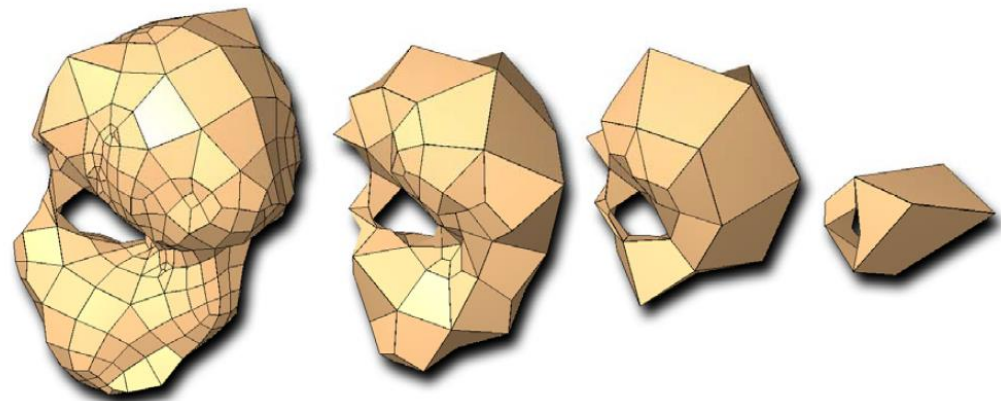
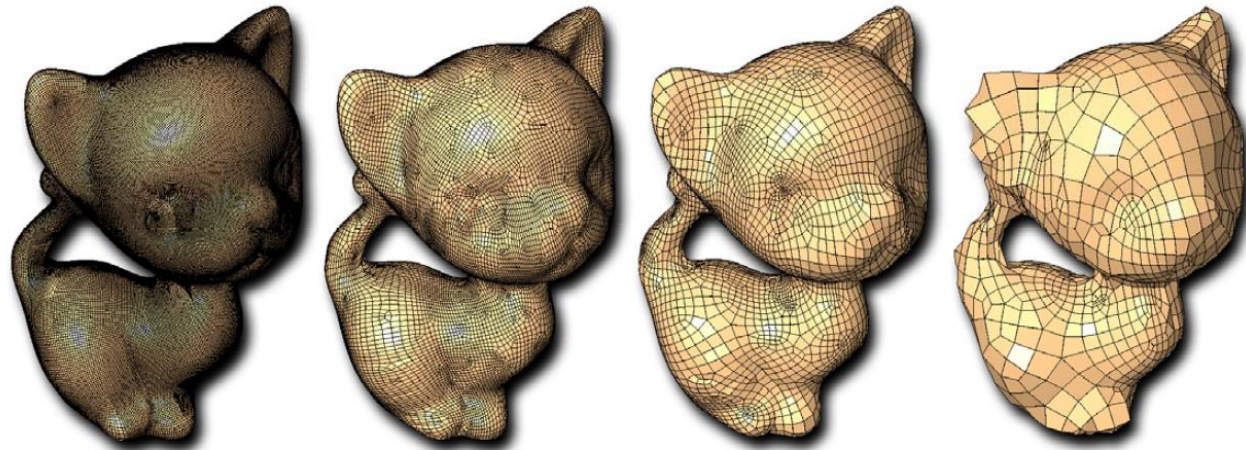


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Reduction
- Manipulation
- Animation

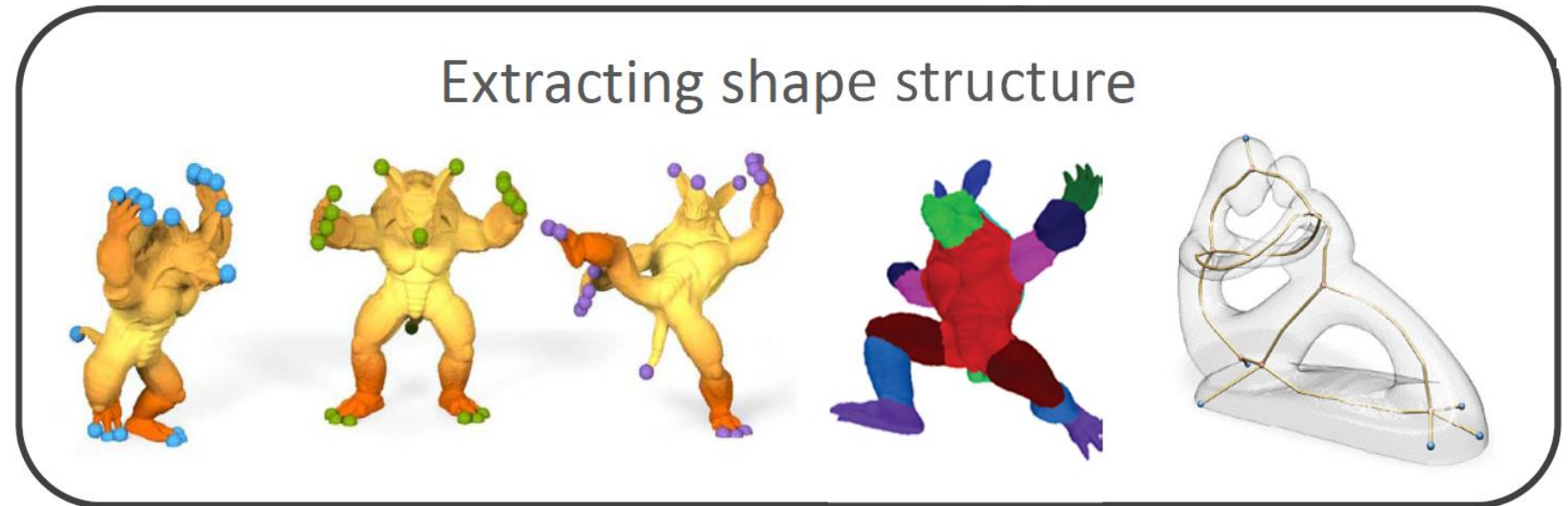


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Structure**
- Manipulation
- Animation



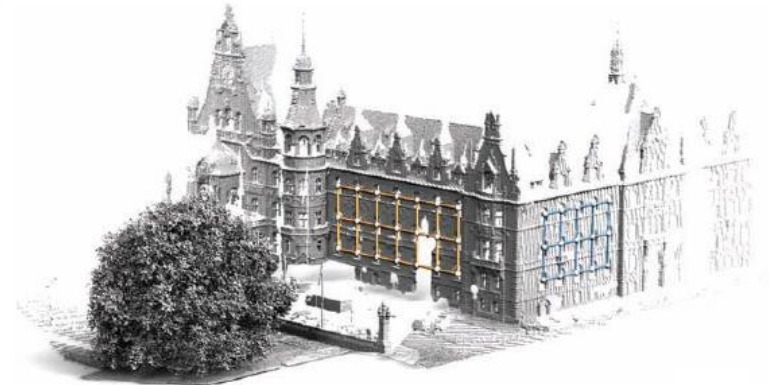
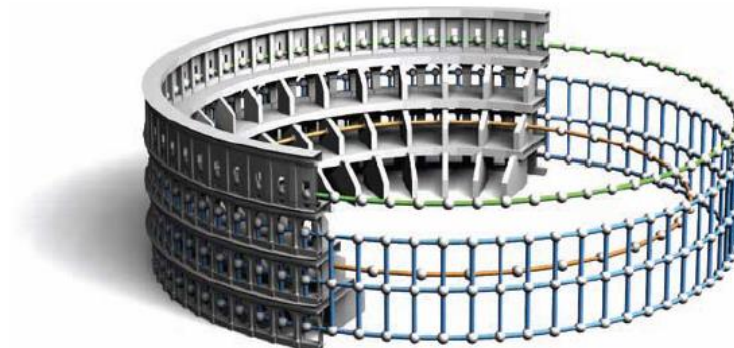
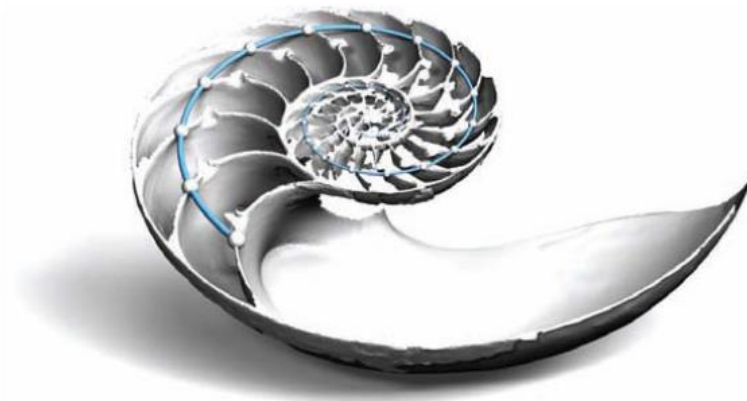
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Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Symmetry detection**
- Manipulation
- Animation

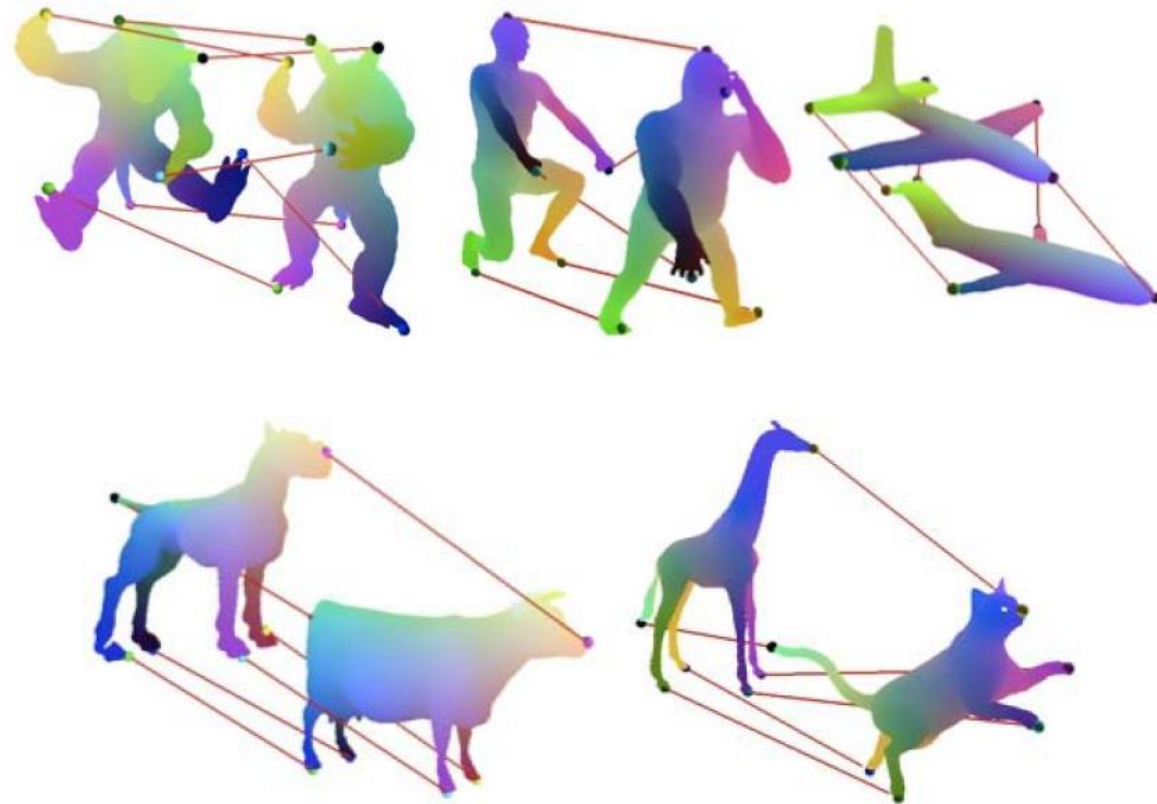


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - Correspondence
- Manipulation
- Animation

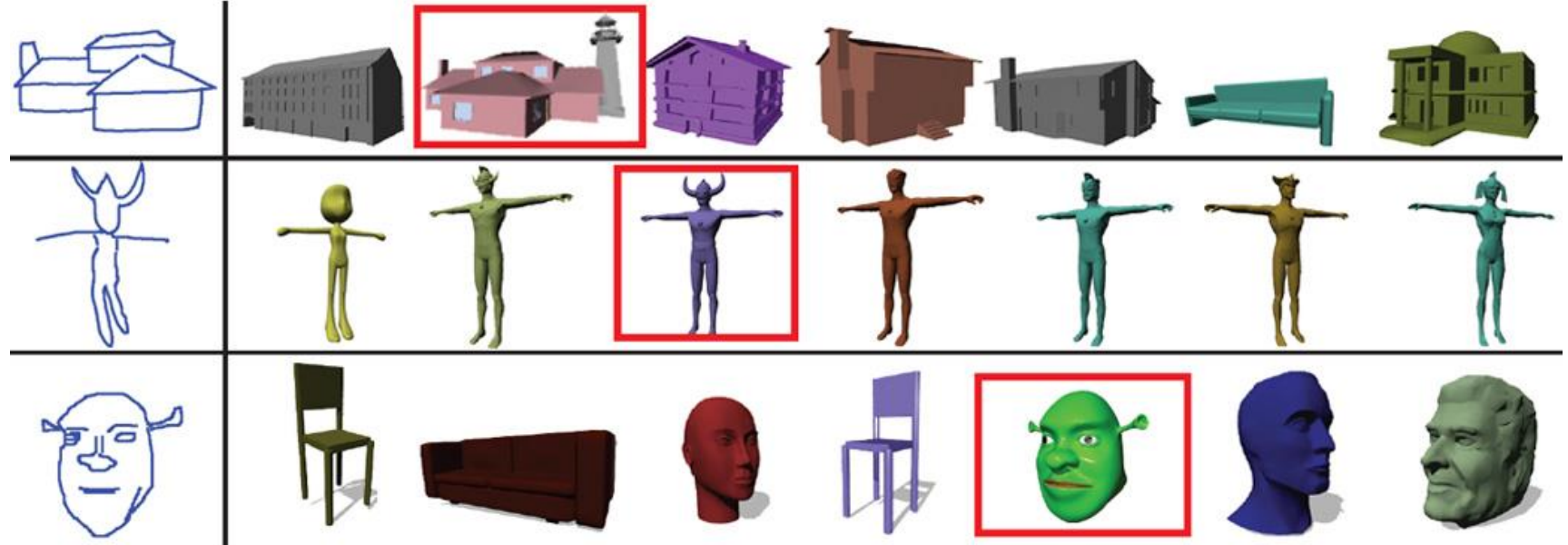


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Shape retrieval**
- Manipulation
- Animation



Shao et al. 2011

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Segmentation**
- Manipulation
- Animation

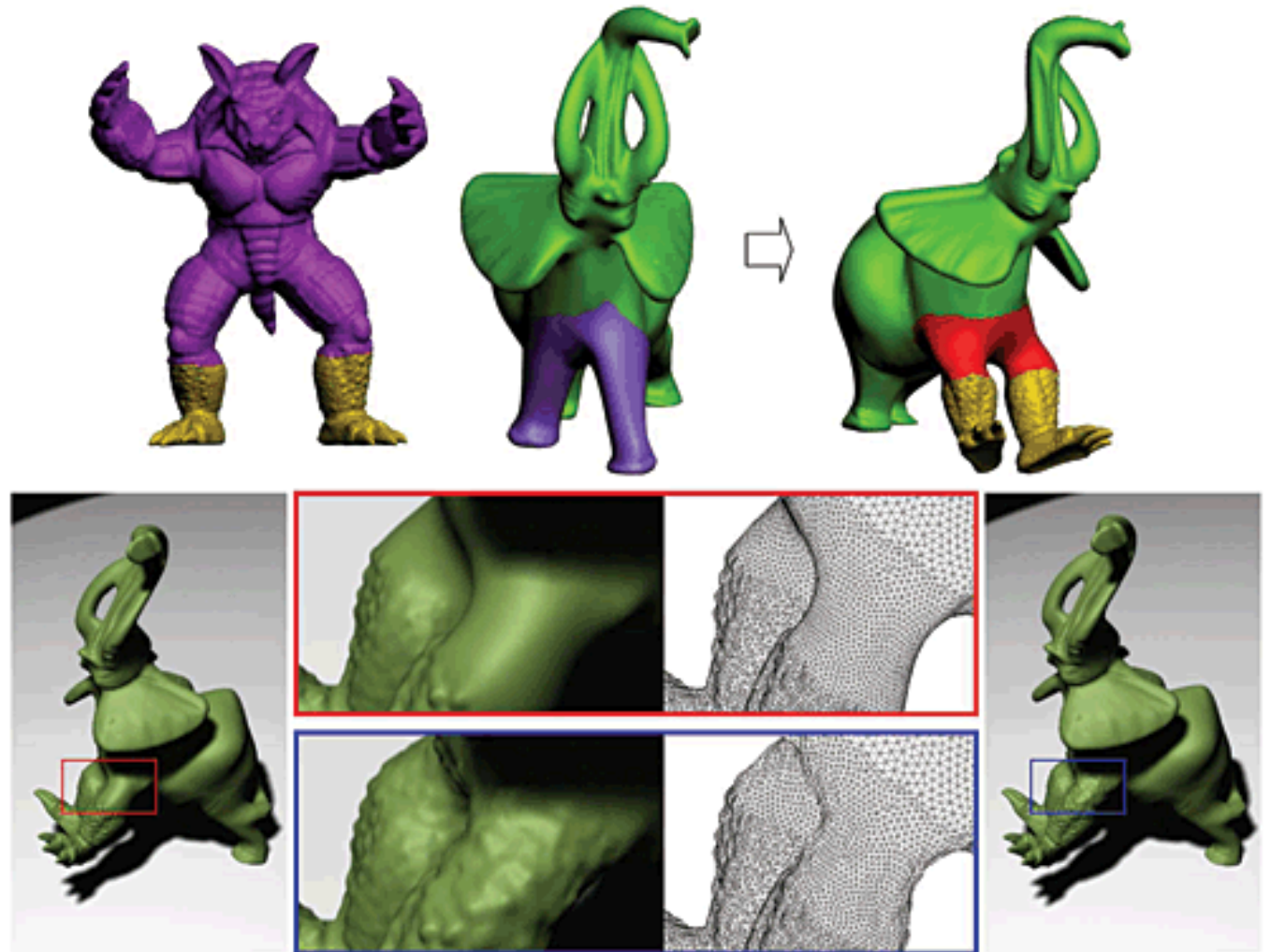


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- **Analysis**
 - **Composition**
- Manipulation
- Animation

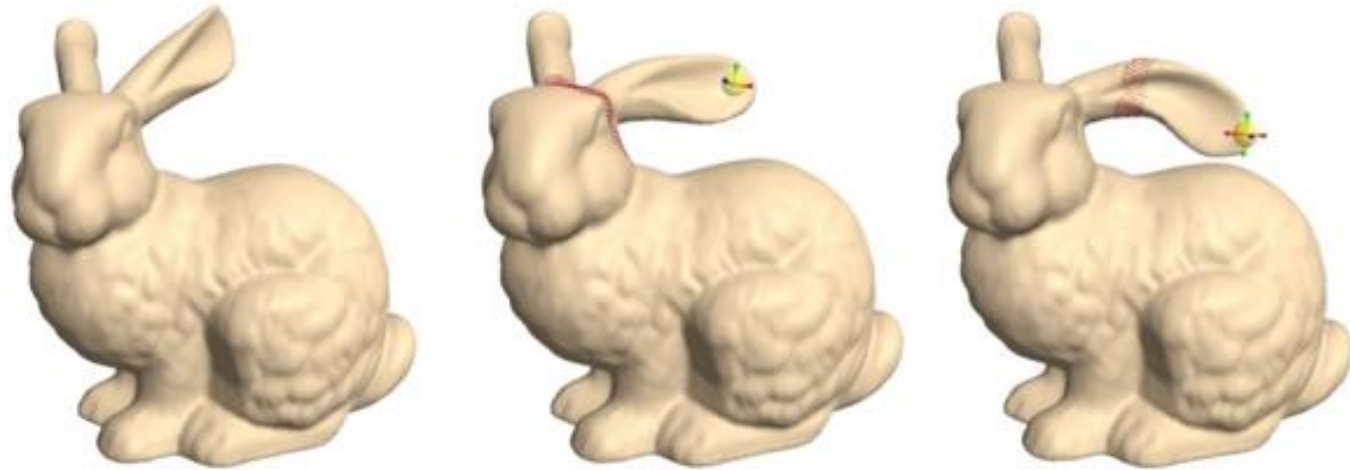


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - **Deformation**
- Animation



IGL

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - Deformation
- Animation

Freeform and multiresolution modeling



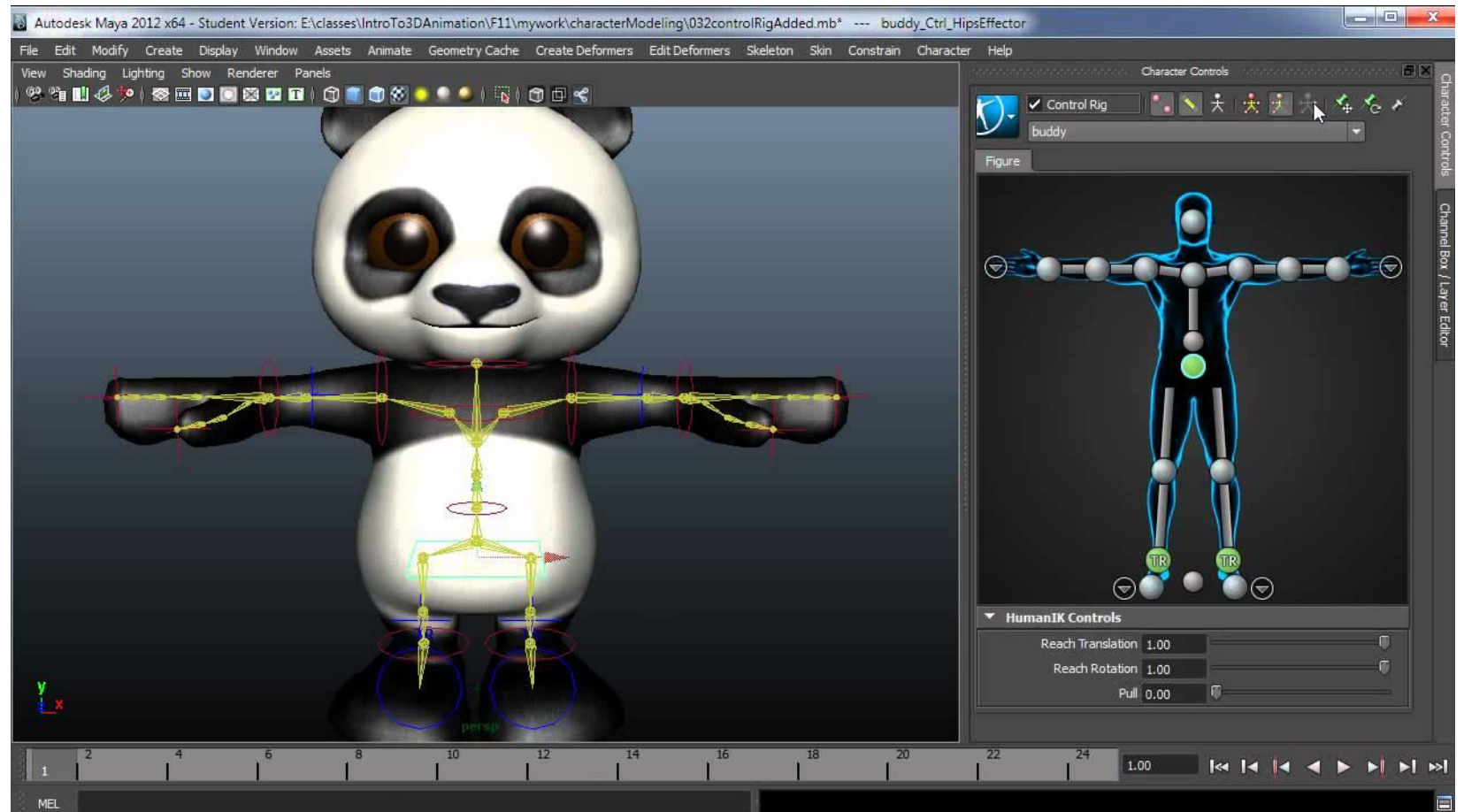
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Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - **Control**
- Animation



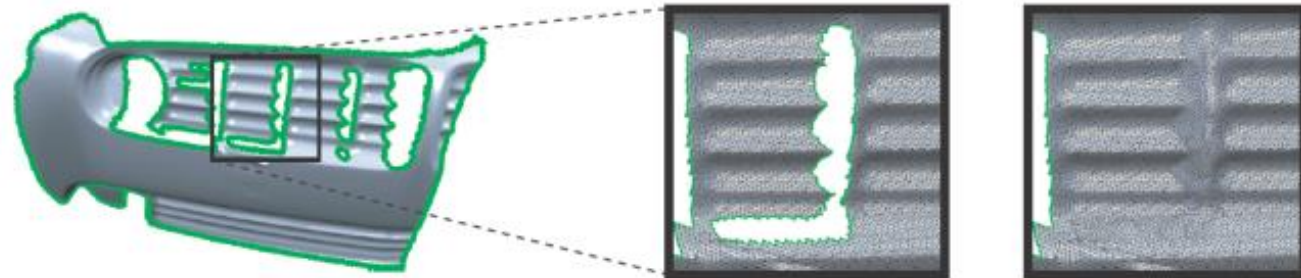
Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- **Manipulation**
 - **Healing**
- Animation

Removal of topological and geometrical errors



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Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - Rigging

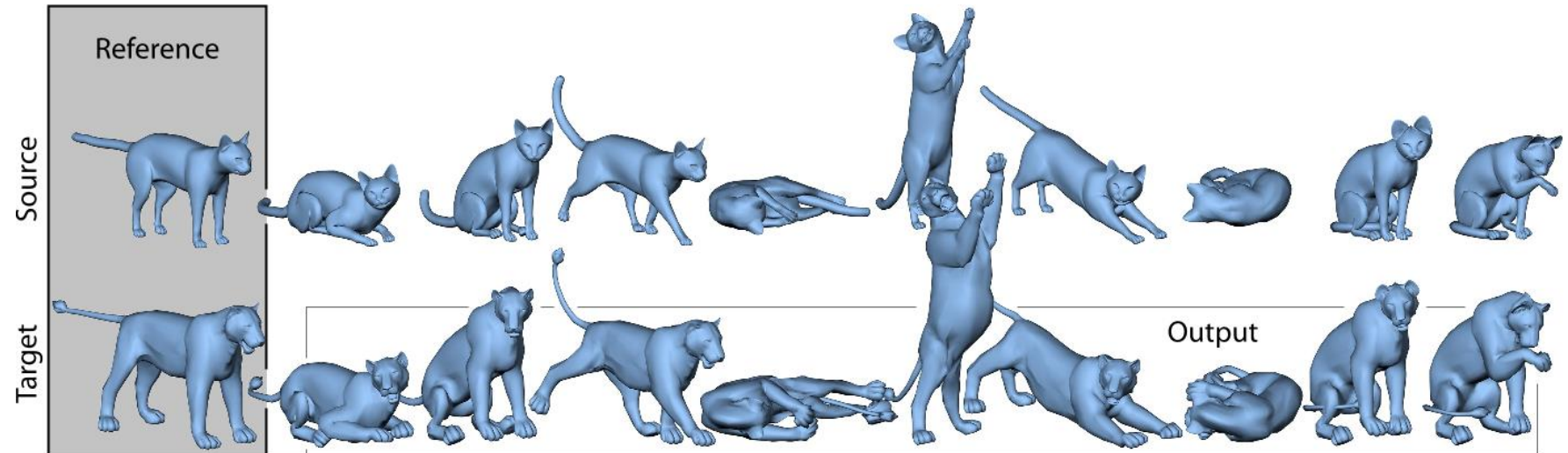


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - **Deformation transfer**



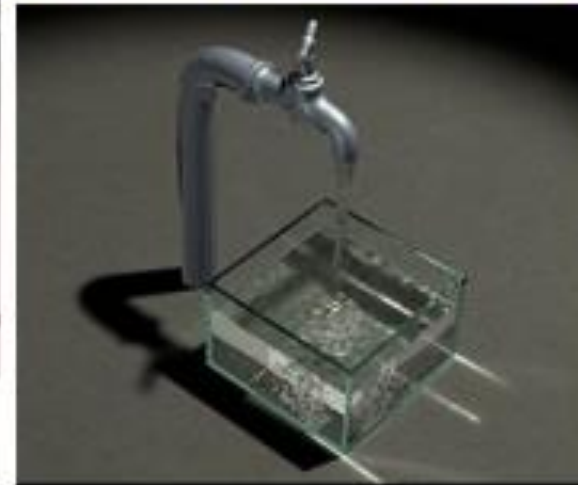
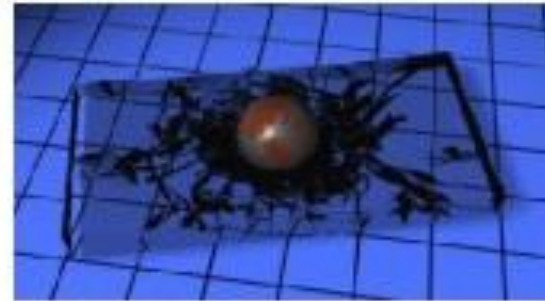
Sumner et al. 2004

Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - **Simulation**

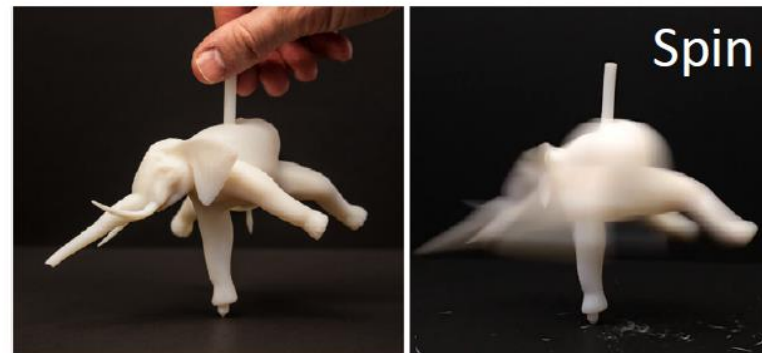


Why Different Representations?



Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- **Animation**
 - **Fabrication**



3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

3D Object Representations



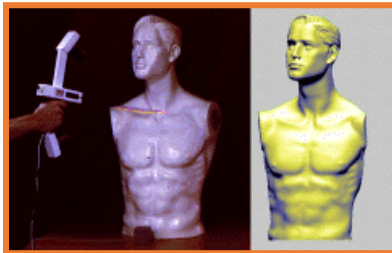
- Points
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Range Image

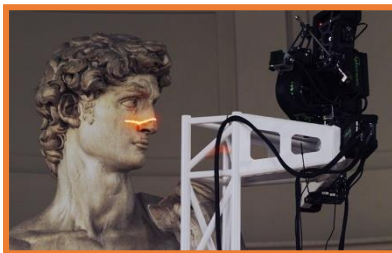


Set of 3D points mapping to pixels of depth image

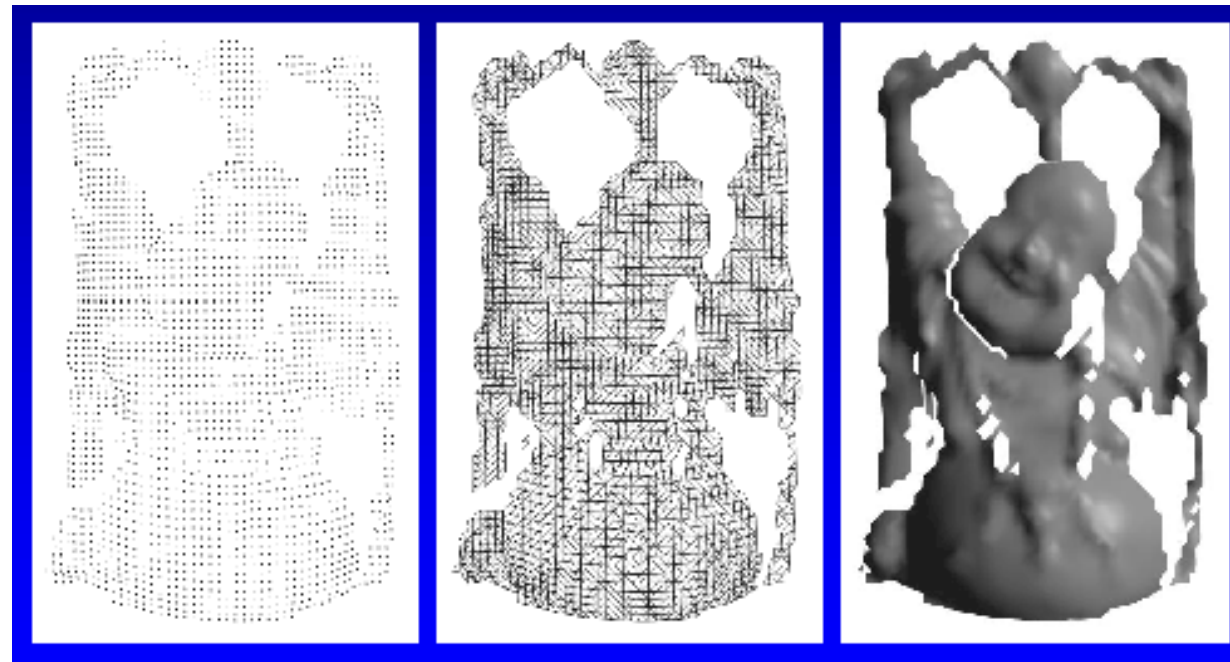
- Can be acquired from range scanner



Cyberware



Stanford



Range Image

Tessellation

Range Surface

Point Cloud



Unstructured set of 3D point samples

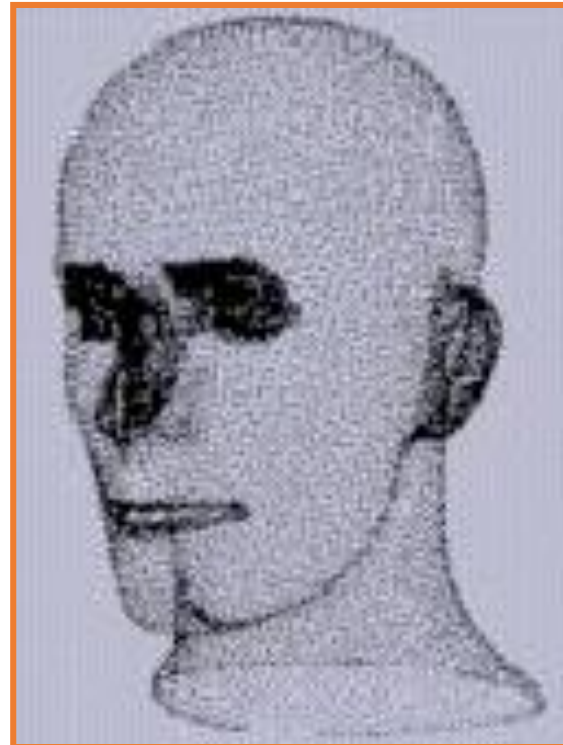
- Acquired from range finder, computer vision, etc



Polhemus



Microscribe-3D



Hoppe



Hoppe

Meshlab demo



3D Object Representations

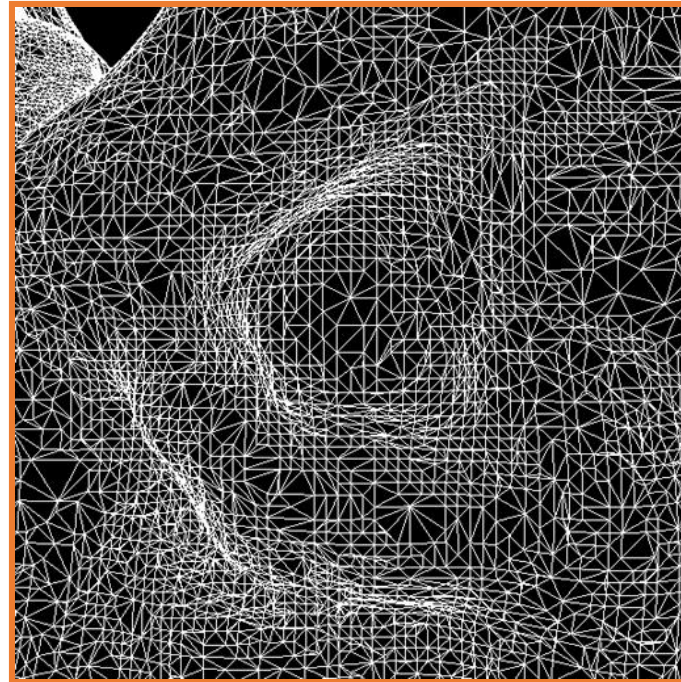


- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
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 - Parametric
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Polygonal Mesh



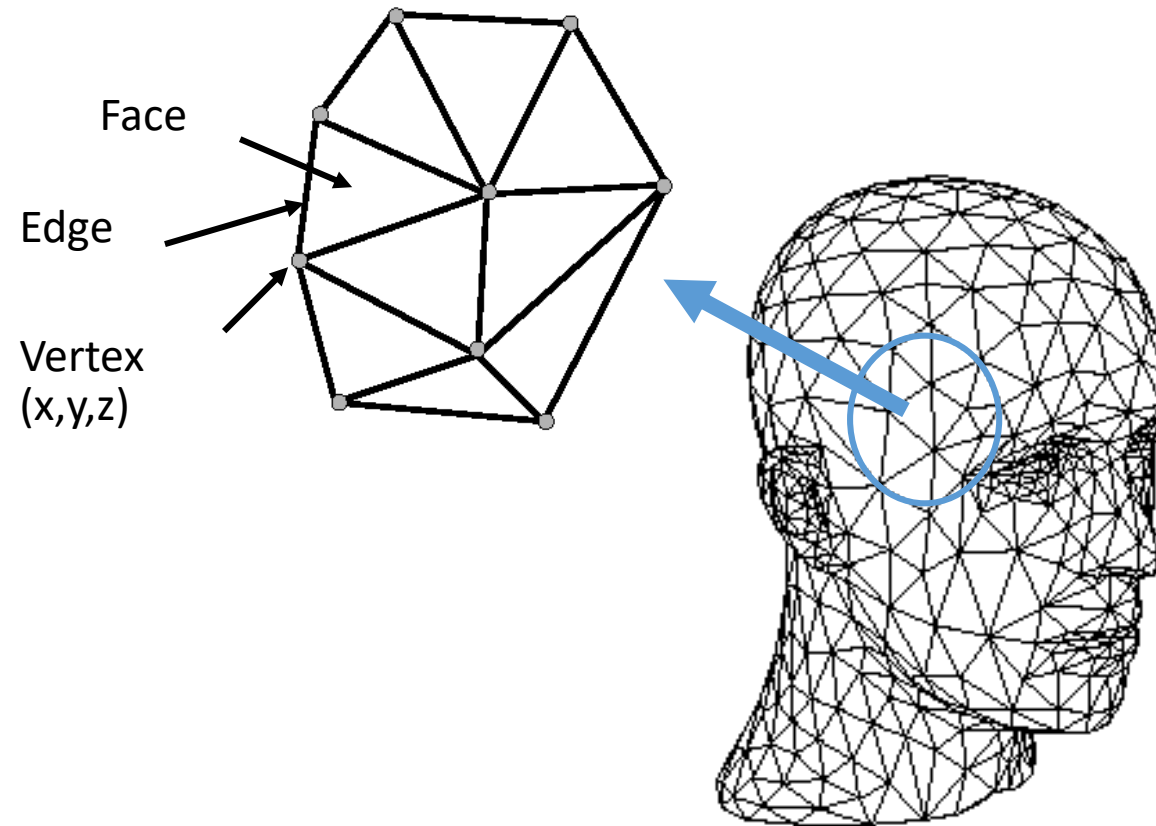
Connected set of polygons (often triangles)



3D Polygonal Mesh



Set of polygons representing a 2D surface embedded in 3D



Meshlab demo



Parametric Surfaces



Applications

- Design of smooth surfaces in cars, ships, etc.

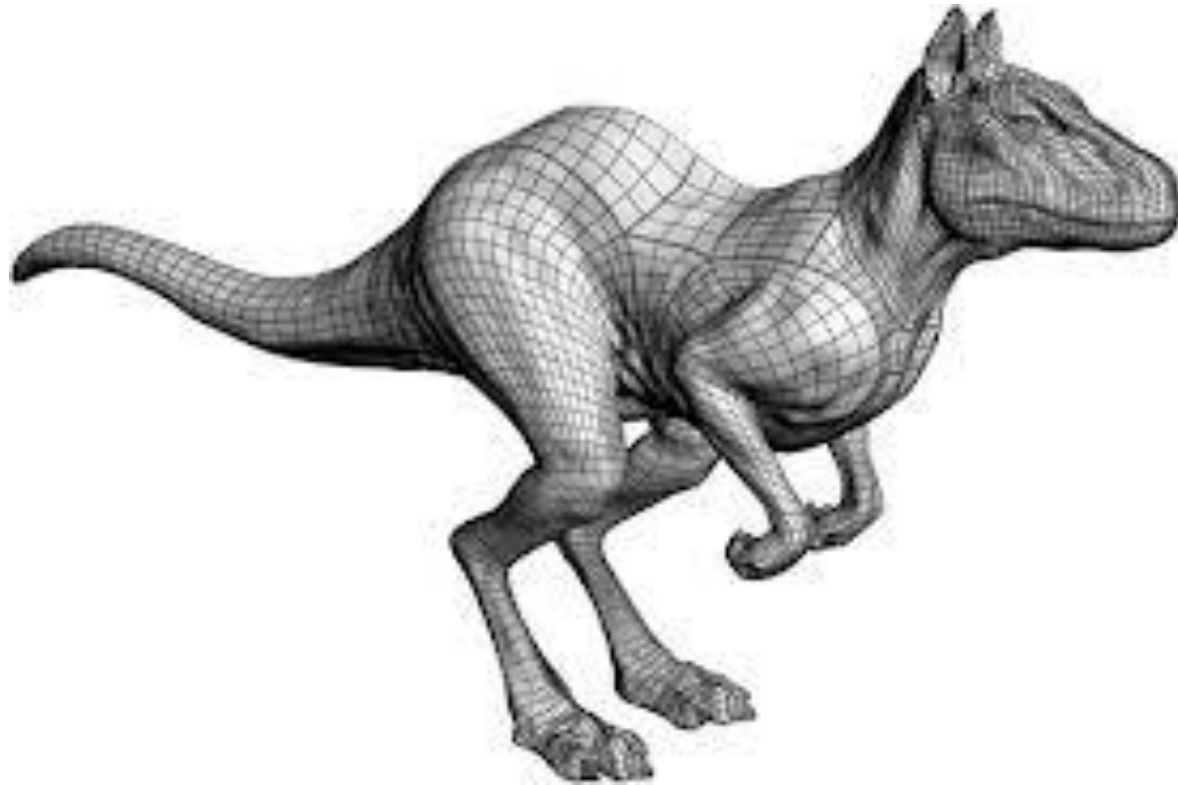


Parametric Surfaces



Applications

- Design of smooth surfaces in cars, ships, etc.
- Creating characters or scenes for movies

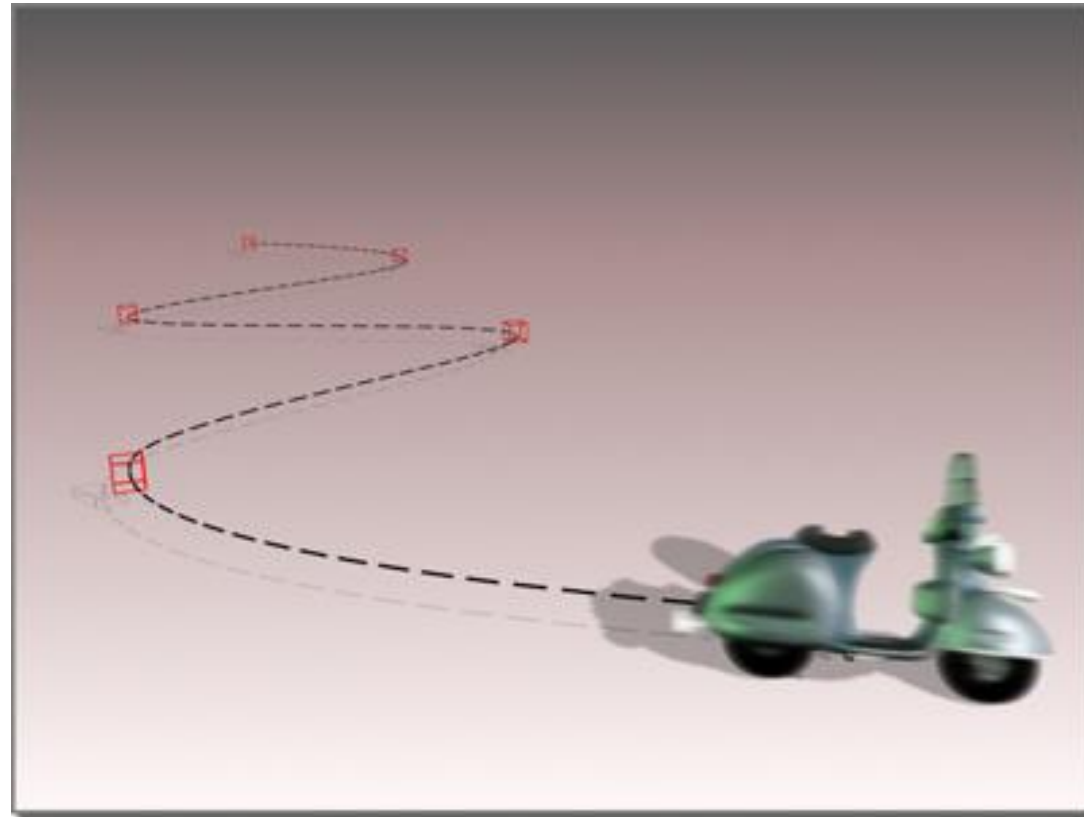


Parametric Curves



Applications

- Defining motion trajectories for objects or cameras



Parametric Curves



- Defined by parametric functions:

- $x = f_x(u)$

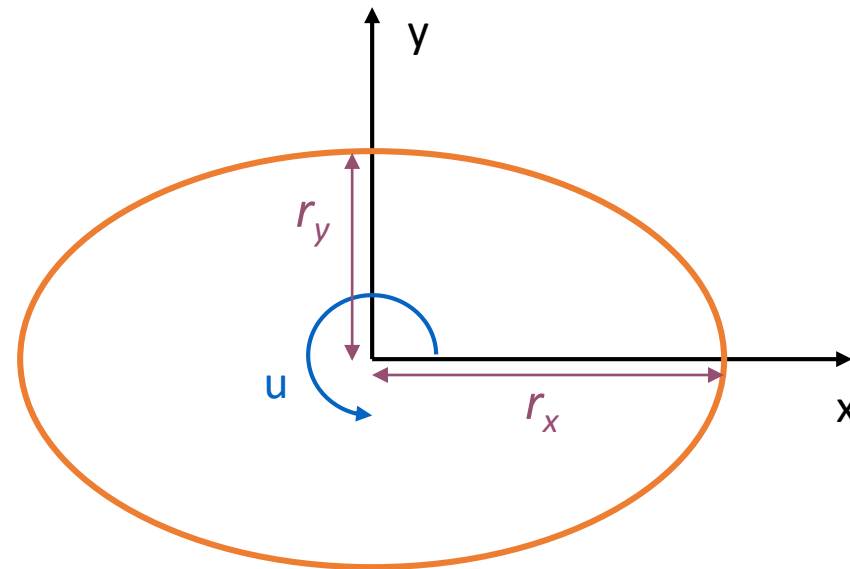
- $y = f_y(u)$

- Example: ellipse

$$f_x(u) = r_x \cos(2\rho u)$$

$$f_y(u) = r_y \sin(2\rho u)$$

$$u \hat{=} [0..1]$$



H&B Figure 10.10

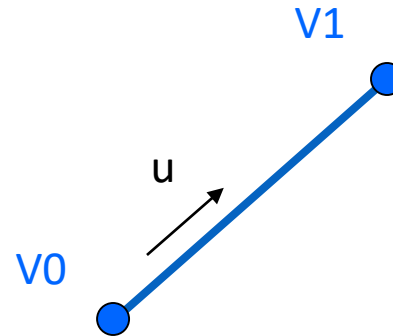
Parametric curves



How to easily define arbitrary curves?

$$x = f_x(u)$$

$$y = f_y(u)$$



Use functions that “blend” control points

$$x = f_x(u) = V0_x * (1 - u) + V1_x * u$$

$$y = f_y(u) = V0_y * (1 - u) + V1_y * u$$

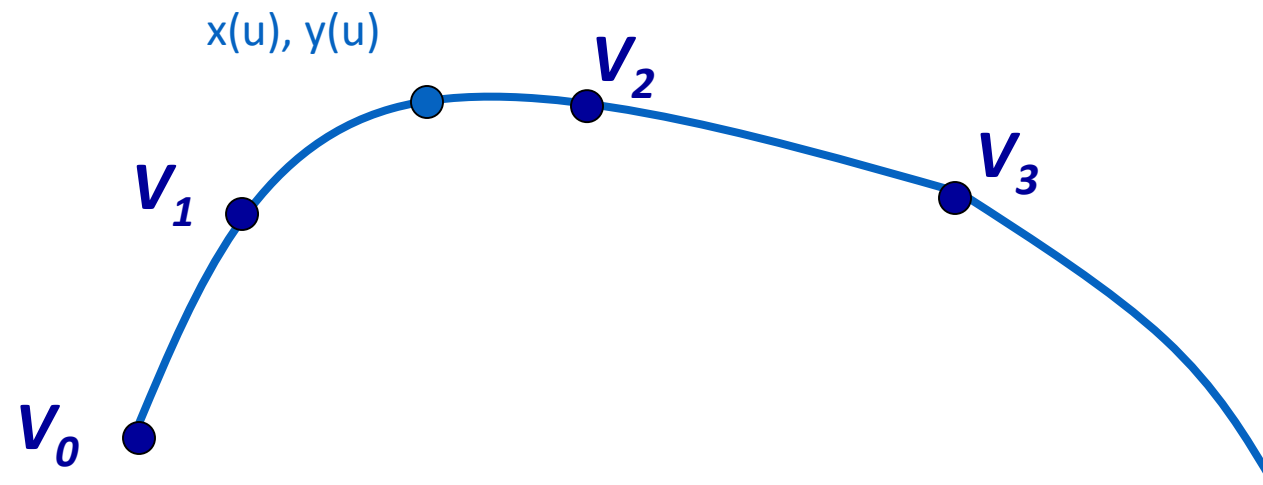
Parametric curves



More generally:

$$x(u) = \sum_{i=0}^n B_i(u) * Vi_x$$

$$y(u) = \sum_{i=0}^n B_i(u) * Vi_y$$



Cubic B-Spline Blending Functions



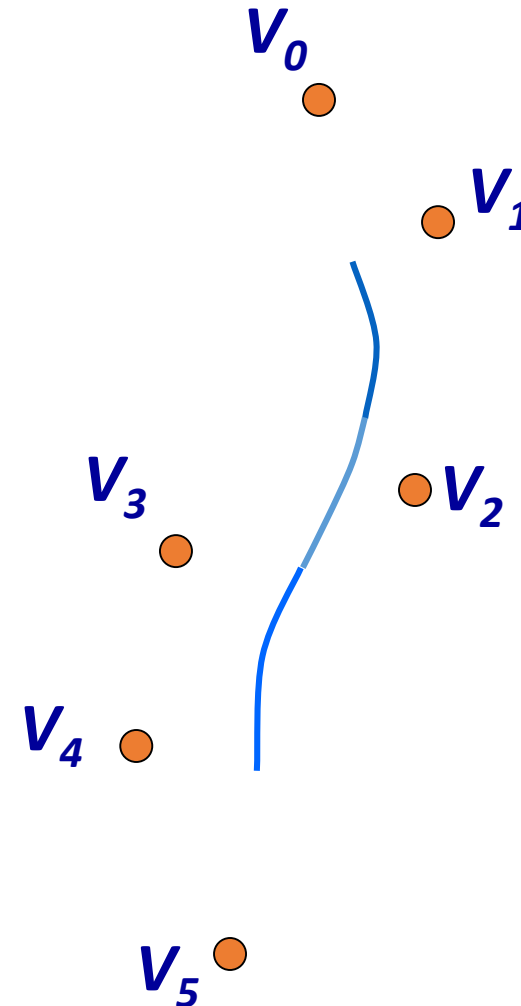
- Four cubic polynomials for four vertices
 - 16 variables (degrees of freedom)
 - Variables are a_i, b_i, c_i, d_i for four blending functions

$$b_{-0}(u) = a_0u^3 + b_0u^2 + c_0u^1 + d_0$$

$$b_{-1}(u) = a_1u^3 + b_1u^2 + c_1u^1 + d_1$$

$$b_{-2}(u) = a_2u^3 + b_2u^2 + c_2u^1 + d_2$$

$$b_{-3}(u) = a_3u^3 + b_3u^2 + c_3u^1 + d_3$$



Cubic B-Spline Blending Functions



Fifteen continuity constraints:

$$\begin{array}{lll} 0 = b_{-0}(0) & 0 = b_{-0}'(0) & 0 = b_{-0}''(0) \\ b_{-0}(1) = b_{-1}(0) & b_{-0}'(1) = b_{-1}'(0) & b_{-0}''(1) = b_{-1}''(0) \\ b_{-1}(1) = b_{-2}(0) & b_{-1}'(1) = b_{-2}'(0) & b_{-1}''(1) = b_{-2}''(0) \\ b_{-2}(1) = b_{-3}(0) & b_{-2}'(1) = b_{-3}'(0) & b_{-2}''(1) = b_{-3}''(0) \\ b_{-3}(1) = 0 & b_{-3}'(1) = 0 & b_{-3}''(1) = 0 \end{array}$$

One more convenient constraint:

$$b_{-0}(0) + b_{-1}(0) + b_{-2}(0) + b_{-3}(0) = 1$$

Cubic B-Spline Blending Functions



Solving the system of equations yields:

$$b_{-3}(u) = -\frac{1}{6}u^3 + \frac{1}{2}u^2 - \frac{1}{2}u + \frac{1}{6}$$

$$b_{-2}(u) = \frac{1}{2}u^3 - u^2 + \frac{2}{3}$$

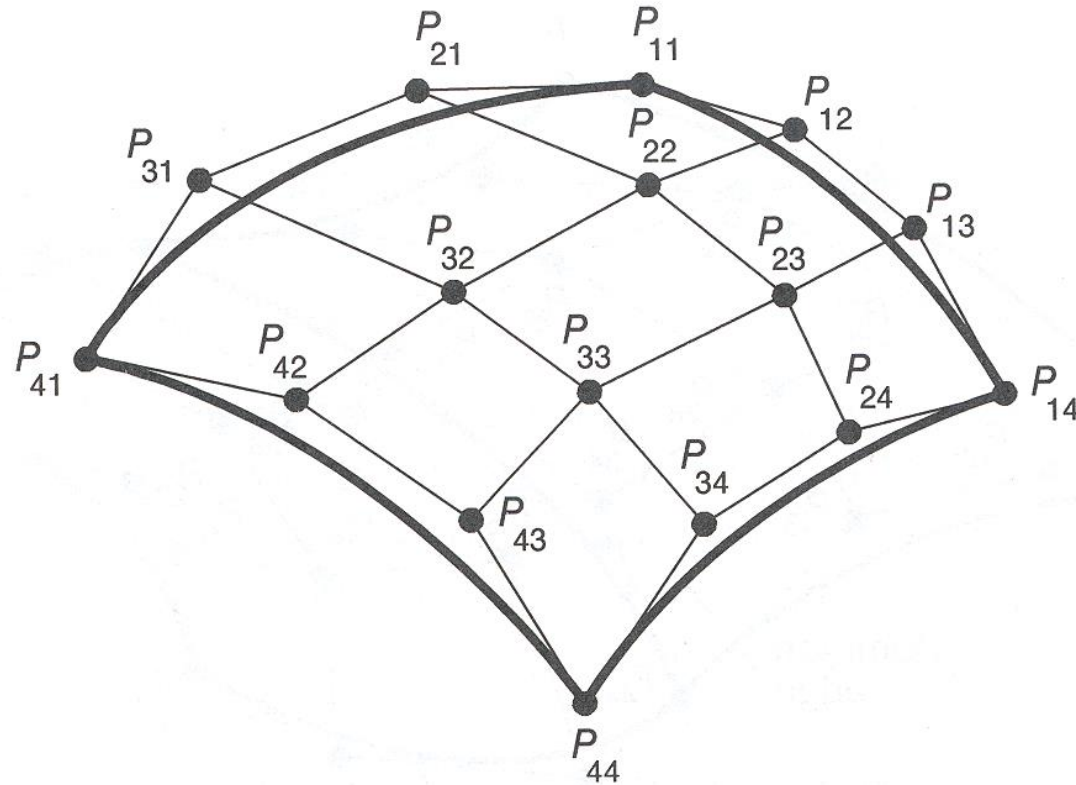
$$b_{-1}(u) = \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{1}{2}u + \frac{1}{6}$$

$$b_{-0}(u) = \frac{1}{6}u^3$$

Parametric Patches



- Each patch is defined by blending control points



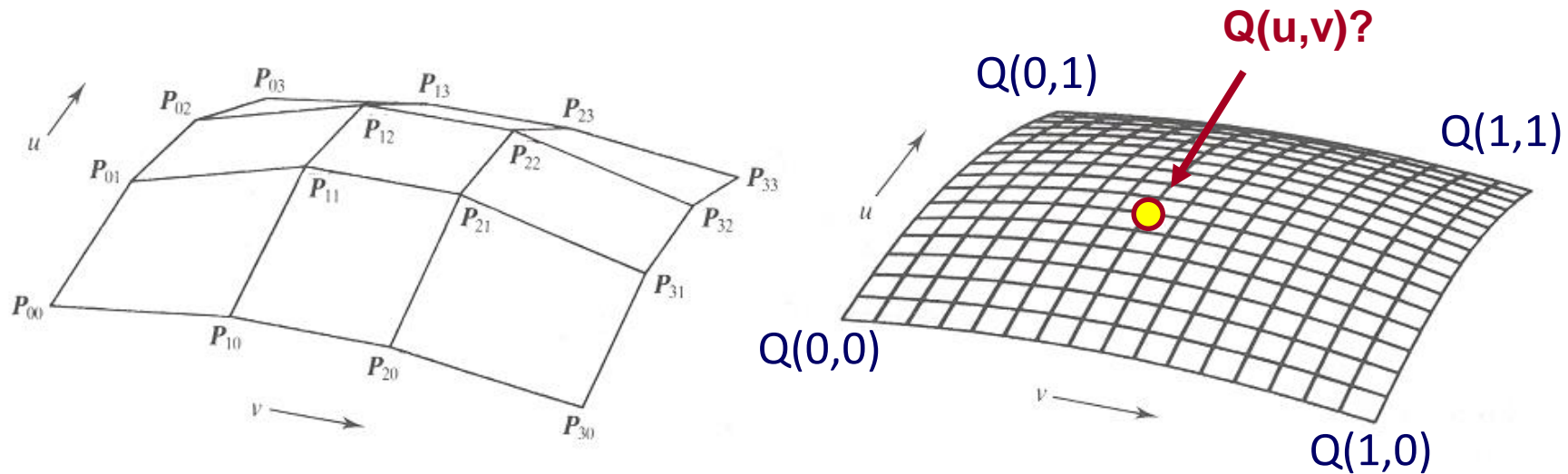
Same ideas as parametric curves!

FvDFH Figure 11.44

Parametric Patches



- Point $Q(u,v)$ on the patch is the tensor product of parametric curves defined by the control points

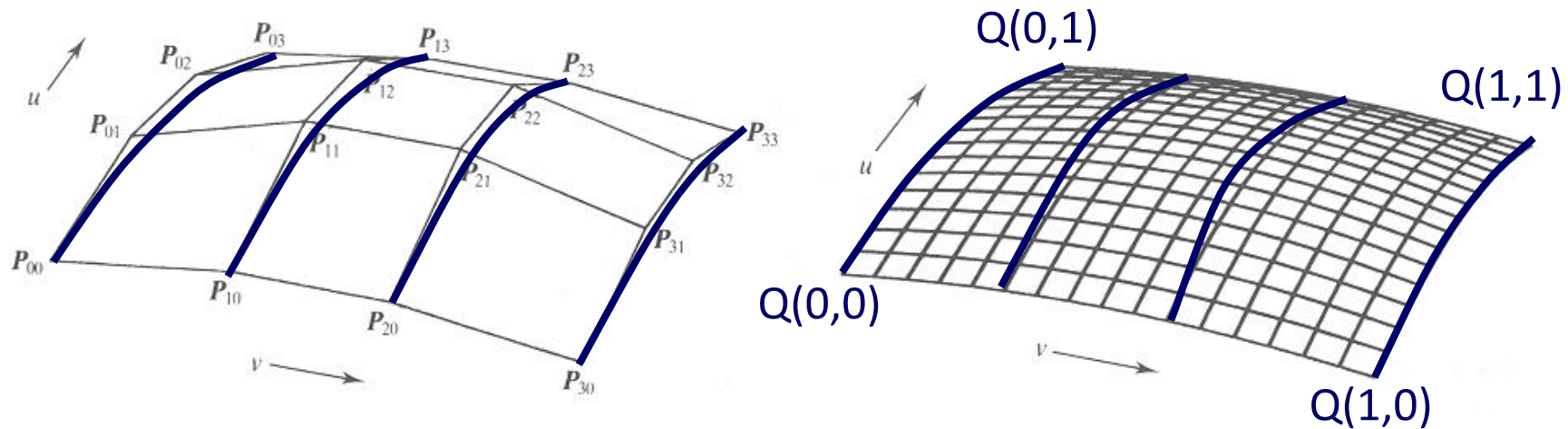


Watt Figure 6.21

Parametric Patches



- Point $Q(u,v)$ on the patch is the tensor product of parametric curves defined by the control points

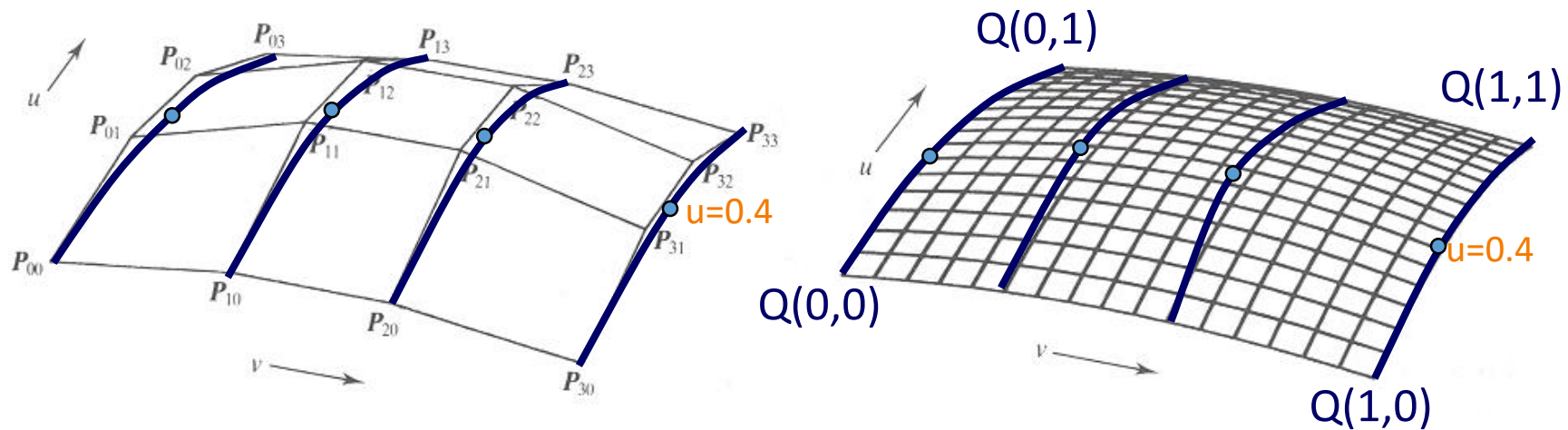


Watt Figure 6.21

Parametric Patches



- Point $Q(u,v)$ on the patch is the tensor product of parametric curves defined by the control points

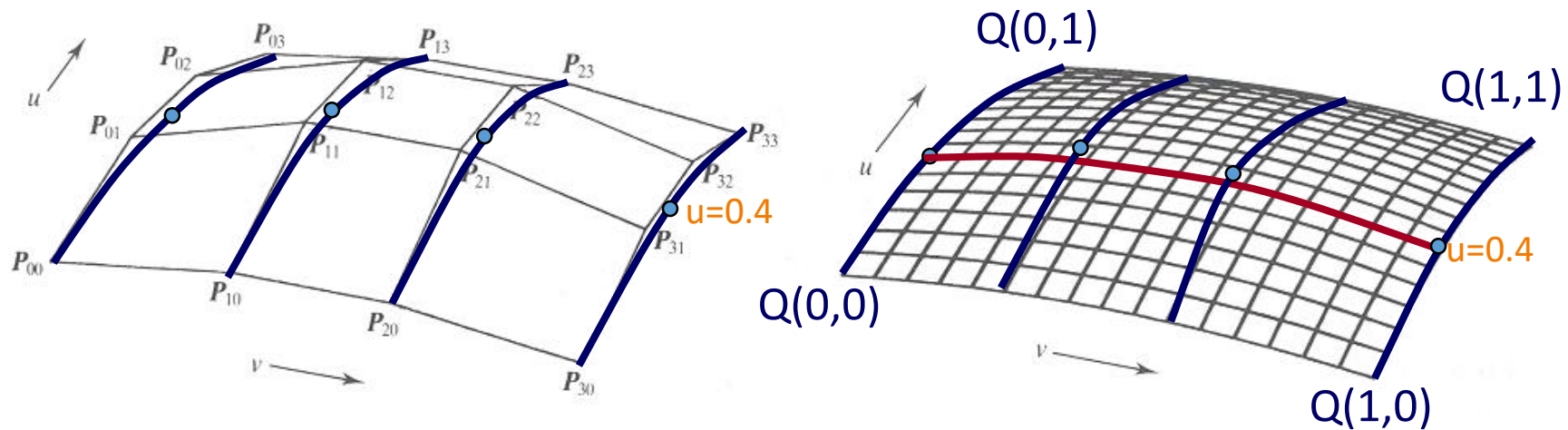


Watt Figure 6.21

Parametric Patches



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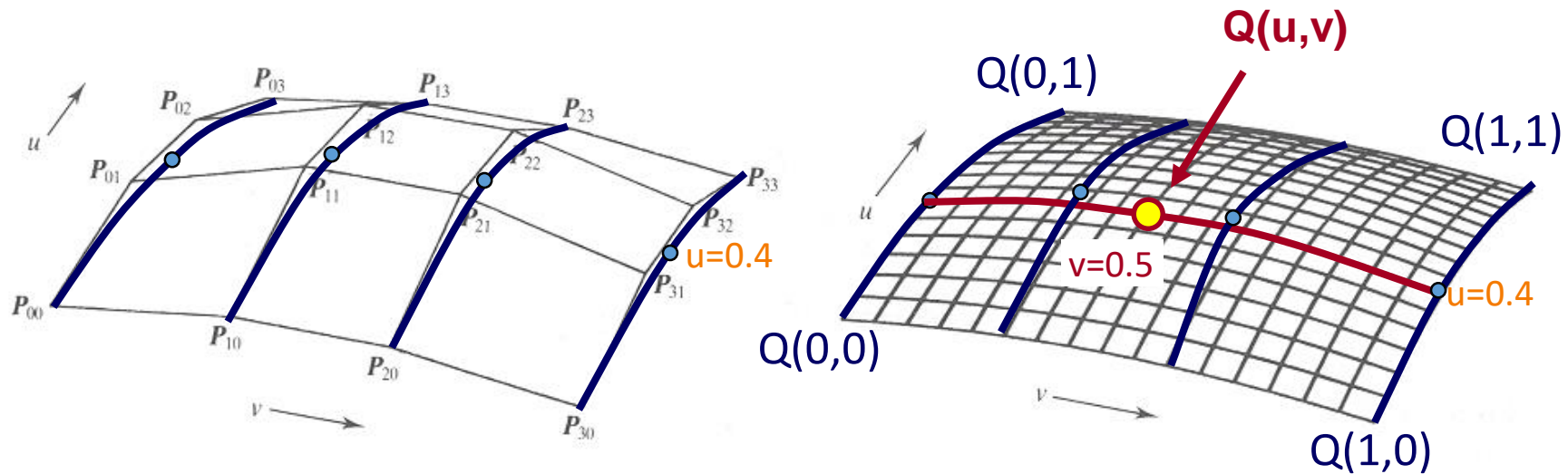


Watt Figure 6.21

Parametric Patches

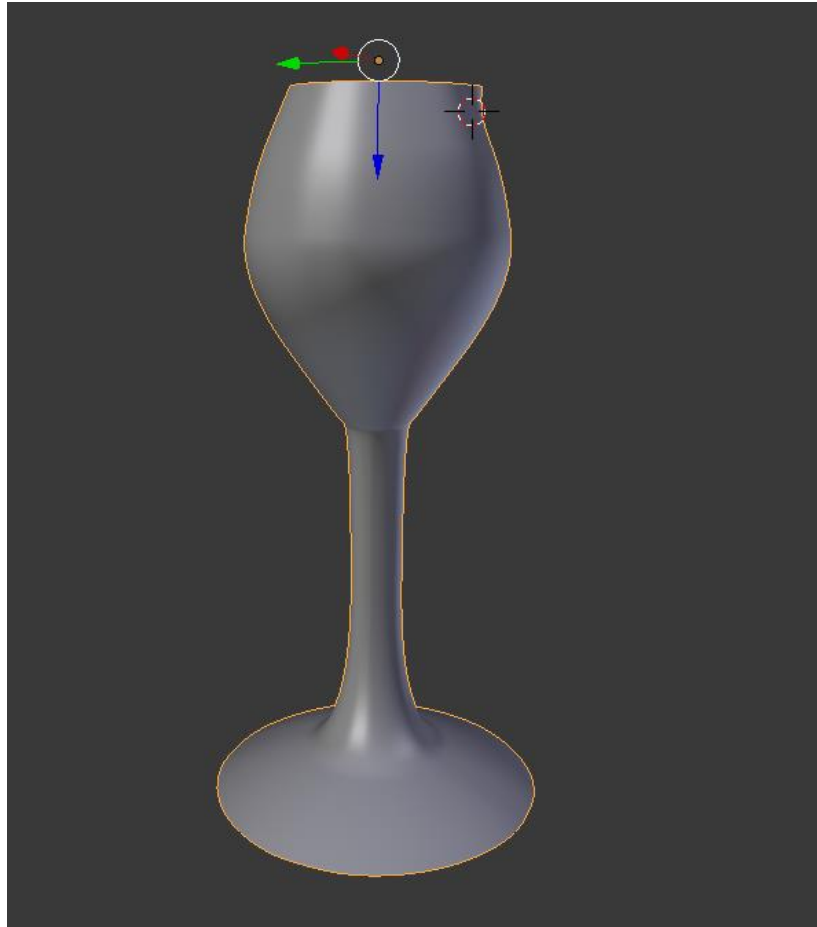


- Point $Q(u,v)$ on the patch is the tensor product of parametric curves defined by the control points



Watt Figure 6.21

NURBS Surfaces

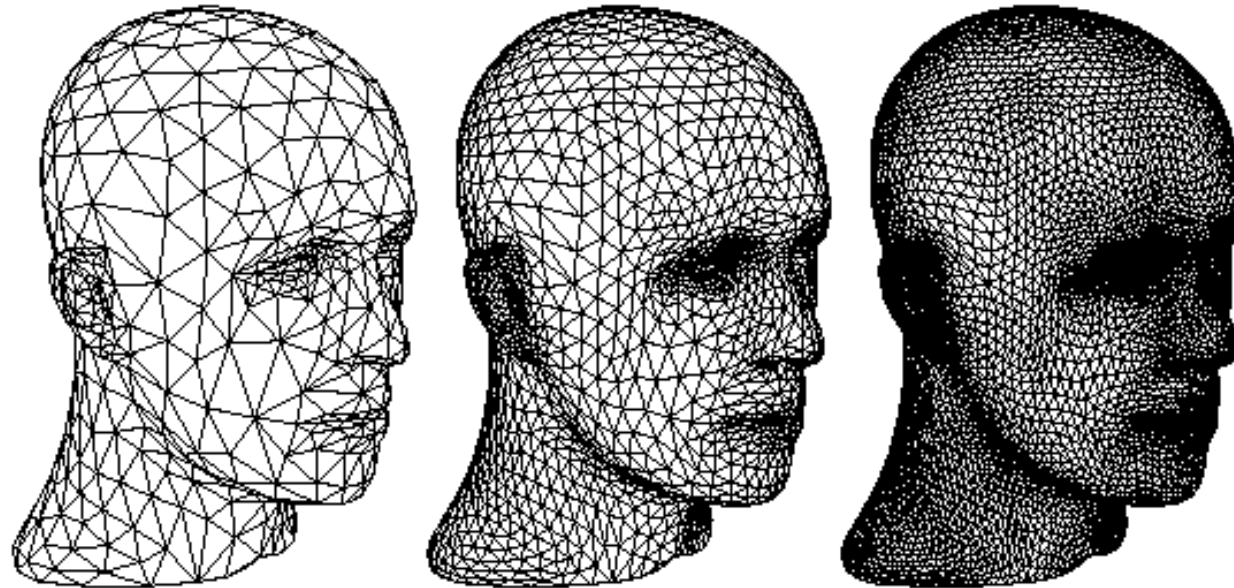


Subdivision Surface



Coarse mesh & subdivision rule

- Smooth surface is **limit** of sequence of refinements

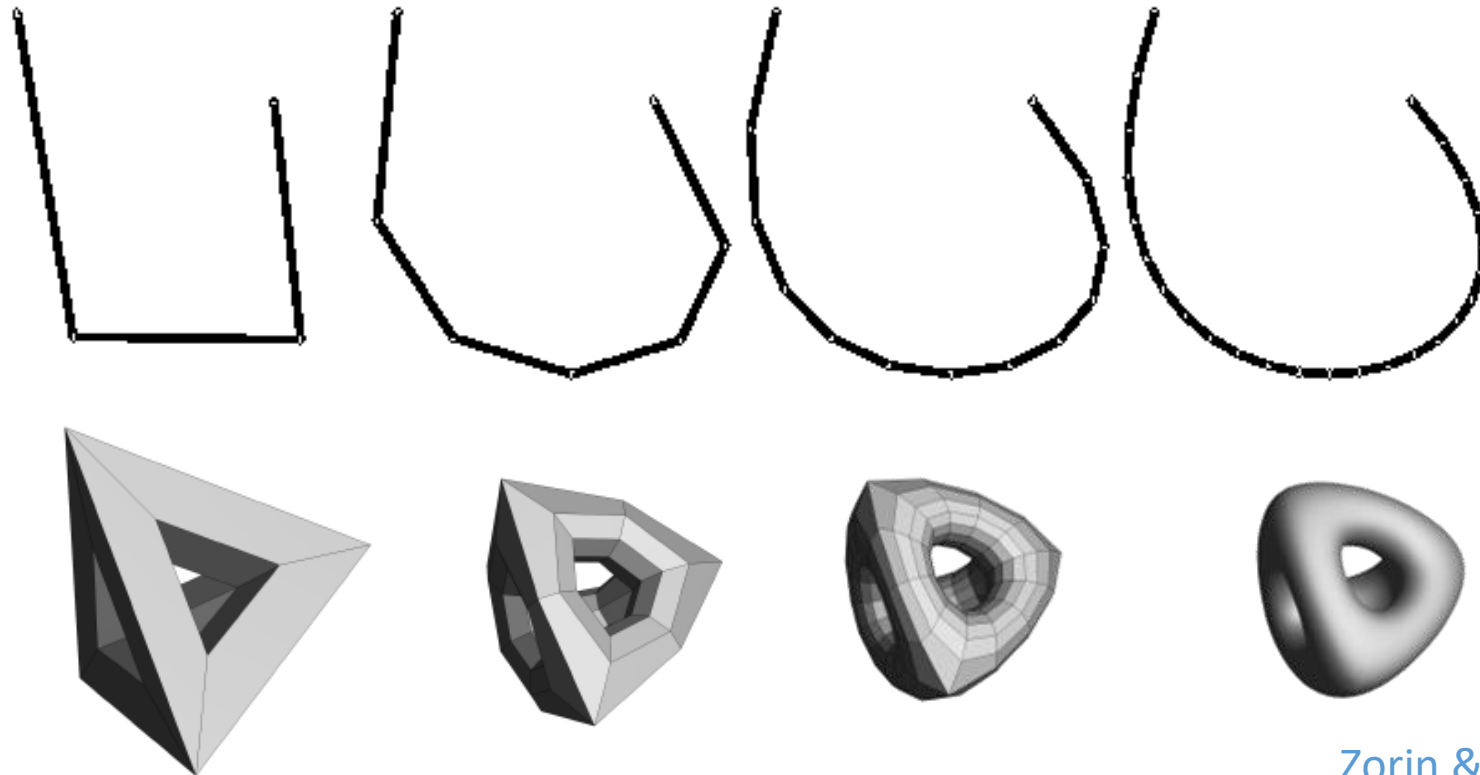


Zorin & Schroeder
SIGGRAPH 99
Course Notes

Subdivision



How do you make a surface with guaranteed continuity?



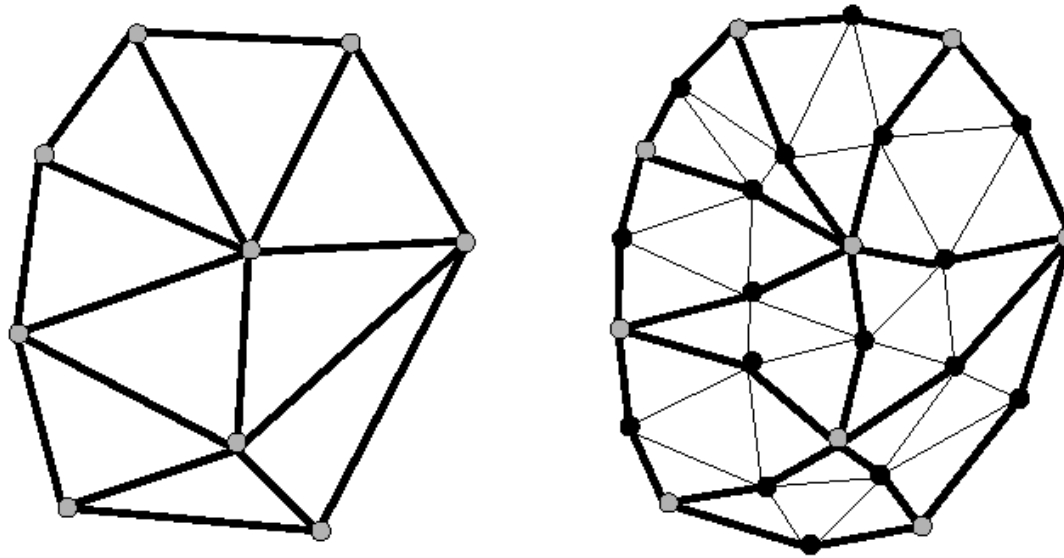
Zorin & Schroeder
SIGGRAPH 99
Course Notes

Subdivision Surfaces



Repeated application of

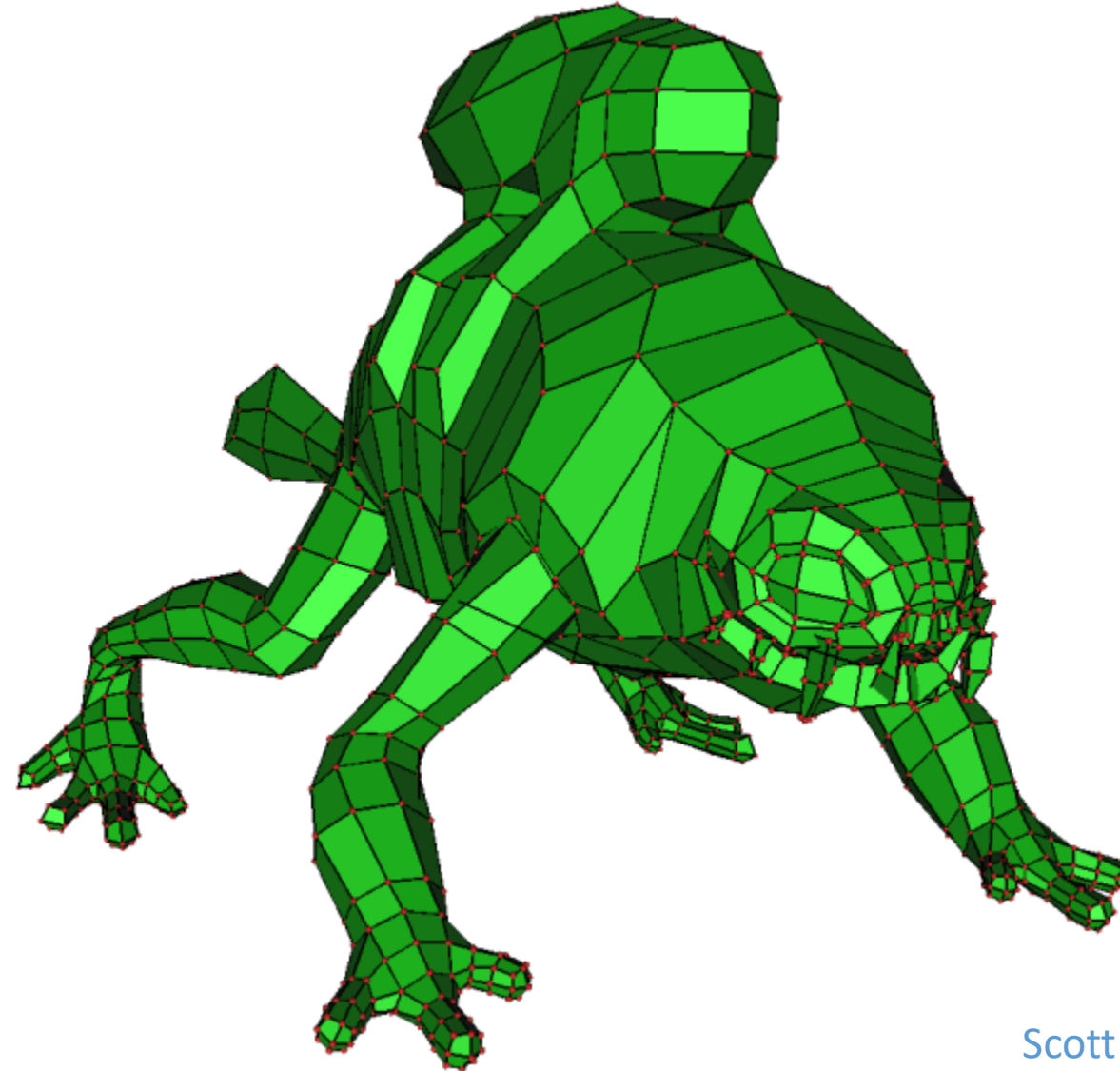
- Topology refinement (splitting faces)
- Geometry refinement (weighted averaging)



Subdivision Surfaces – Examples



Base mesh

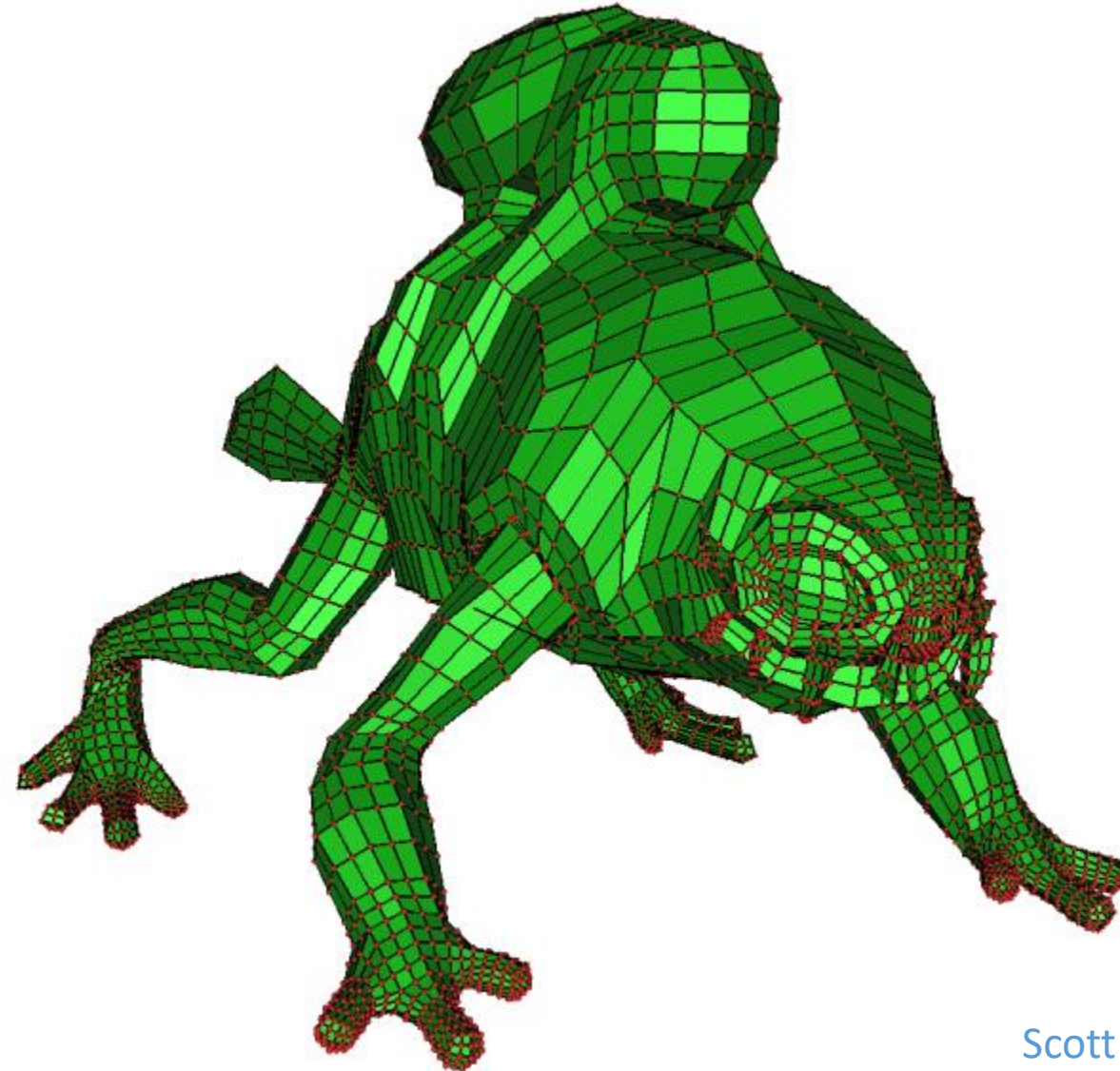


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Subdivision Surfaces – Examples



Topology refinement

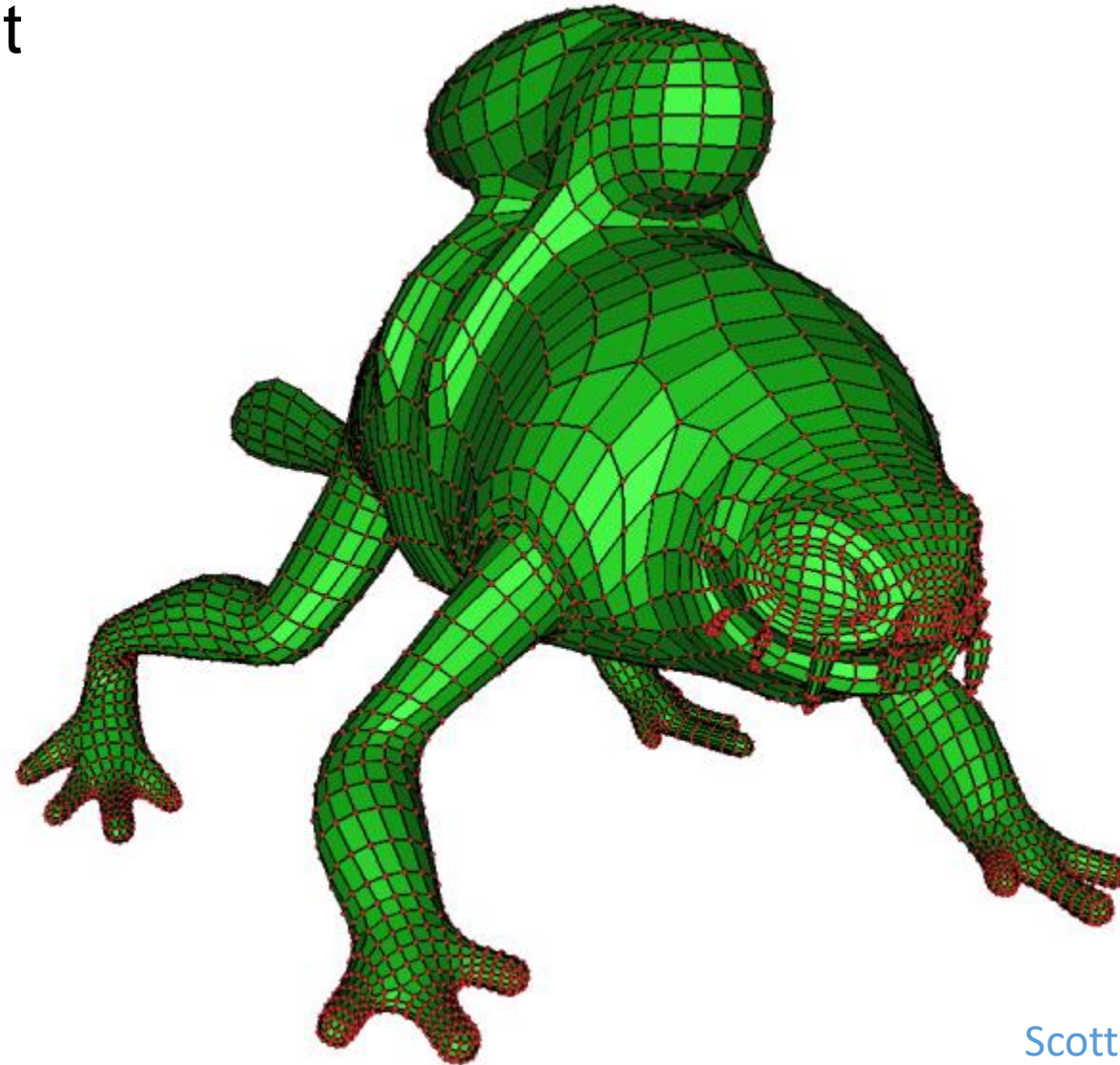


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Subdivision Surfaces – Examples



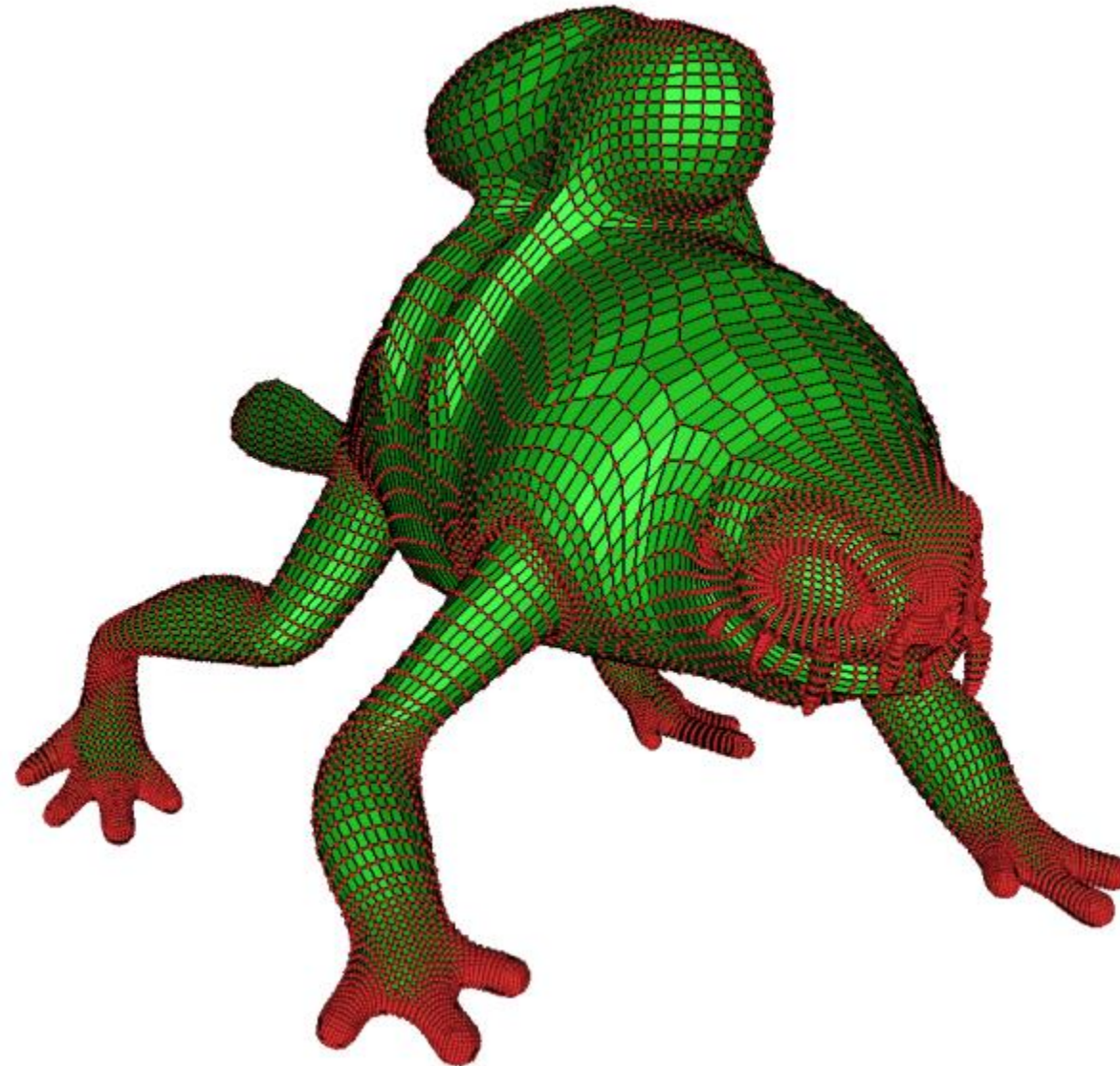
Geometry refinement



Subdivision Surfaces – Examples



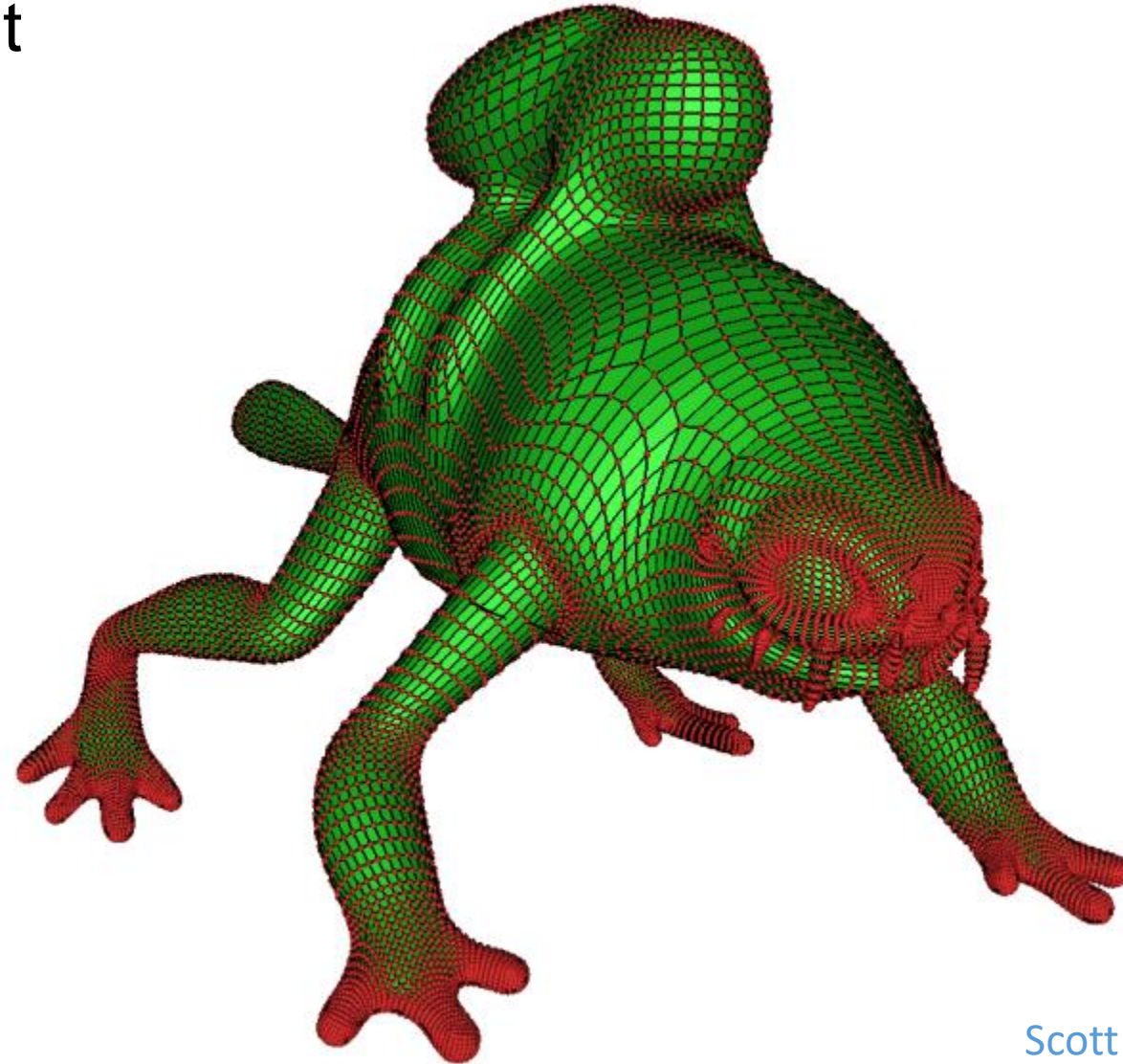
Topology refinement



Subdivision Surfaces – Examples



Geometry refinement

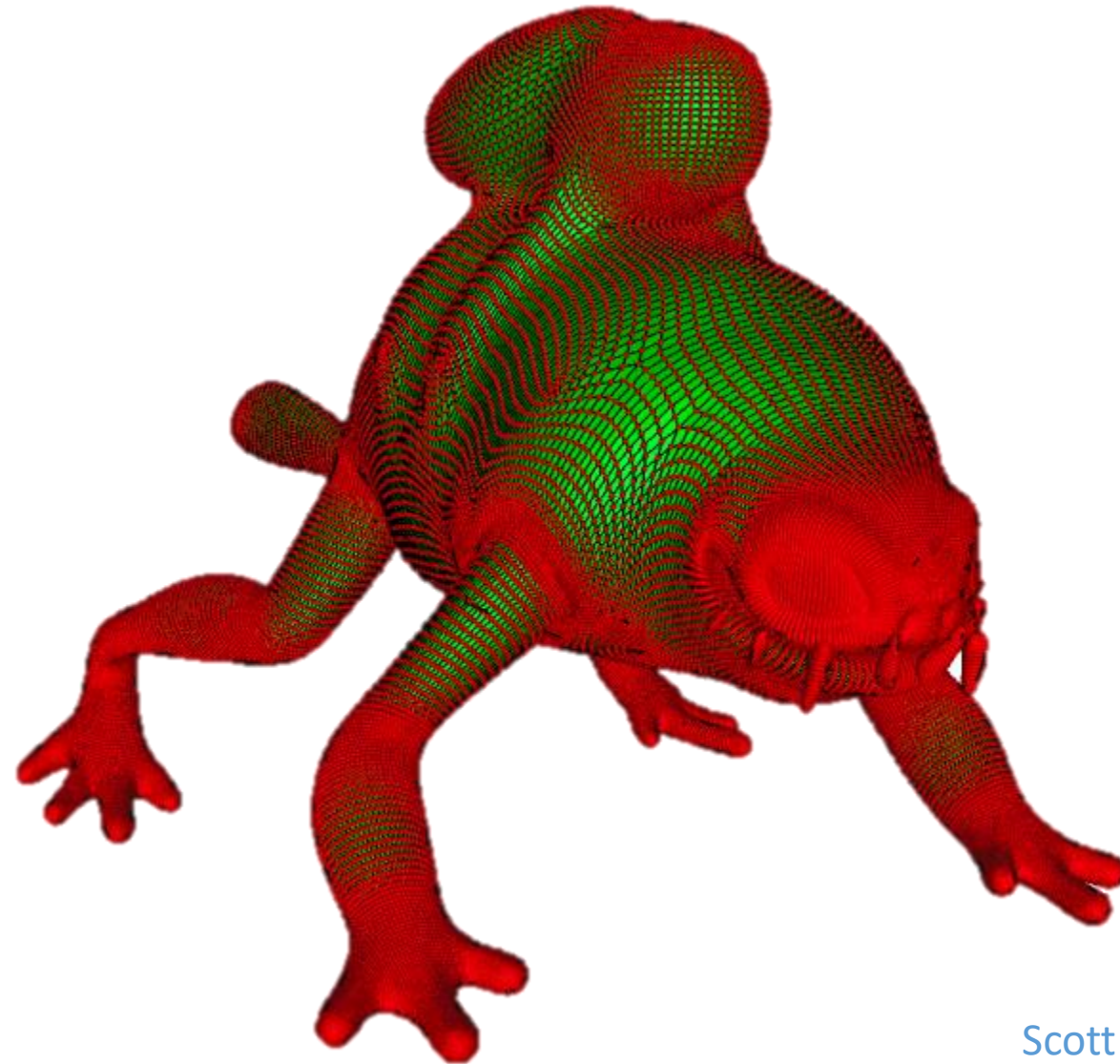


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Subdivision Surfaces – Examples



Topology refinement

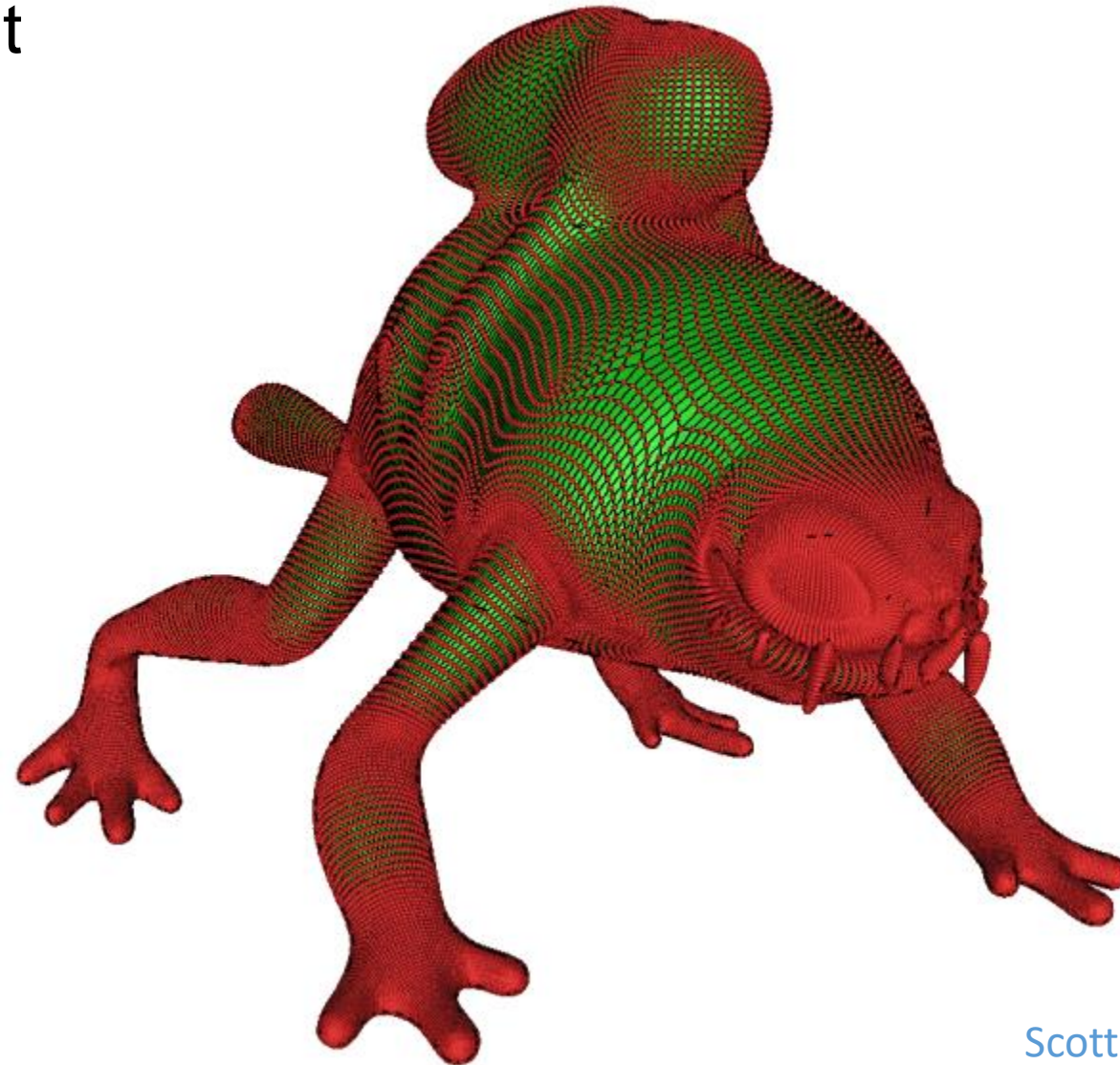


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Subdivision Surfaces – Examples



Geometry refinement

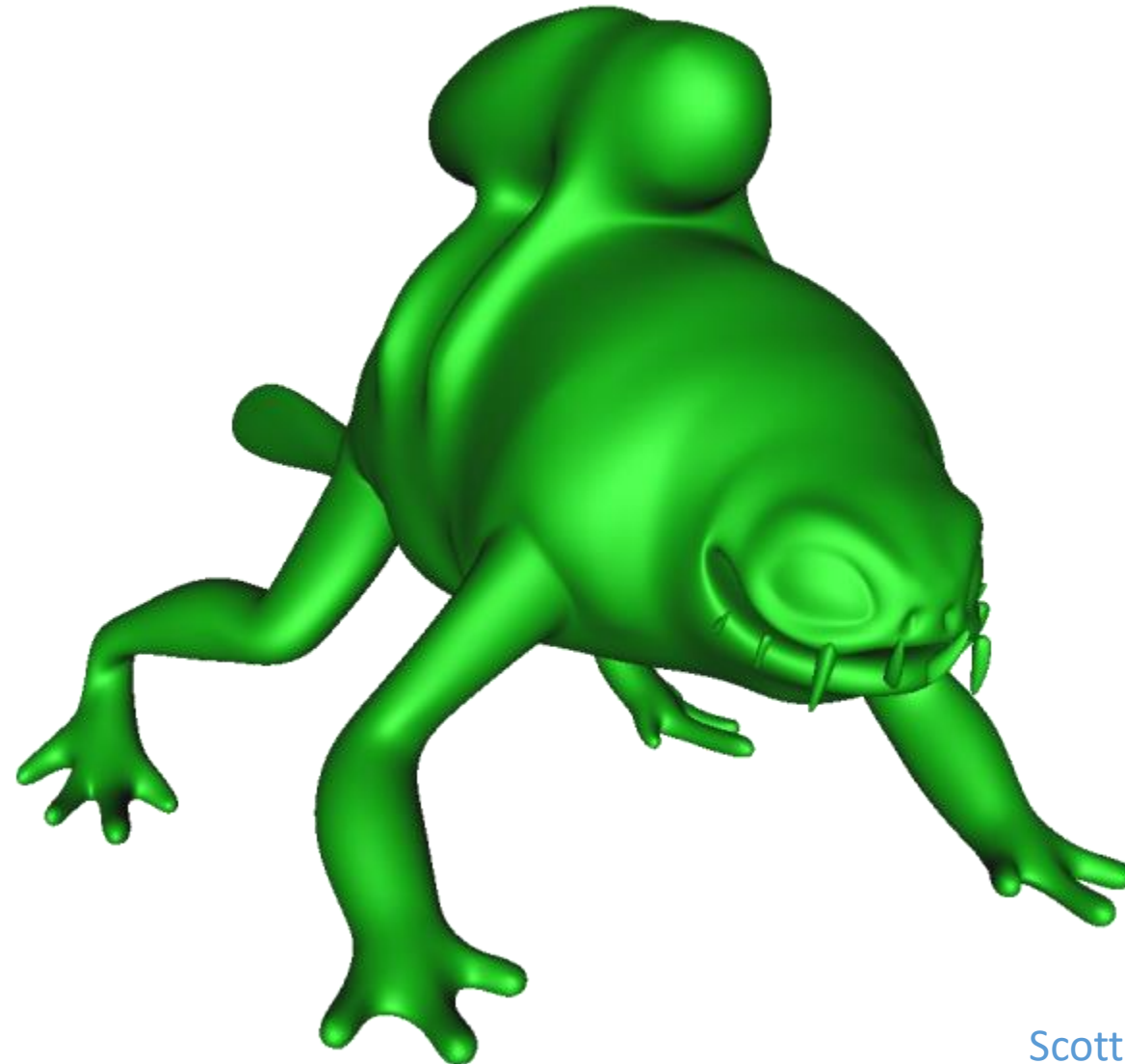


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Subdivision Surfaces – Examples



Limit surface

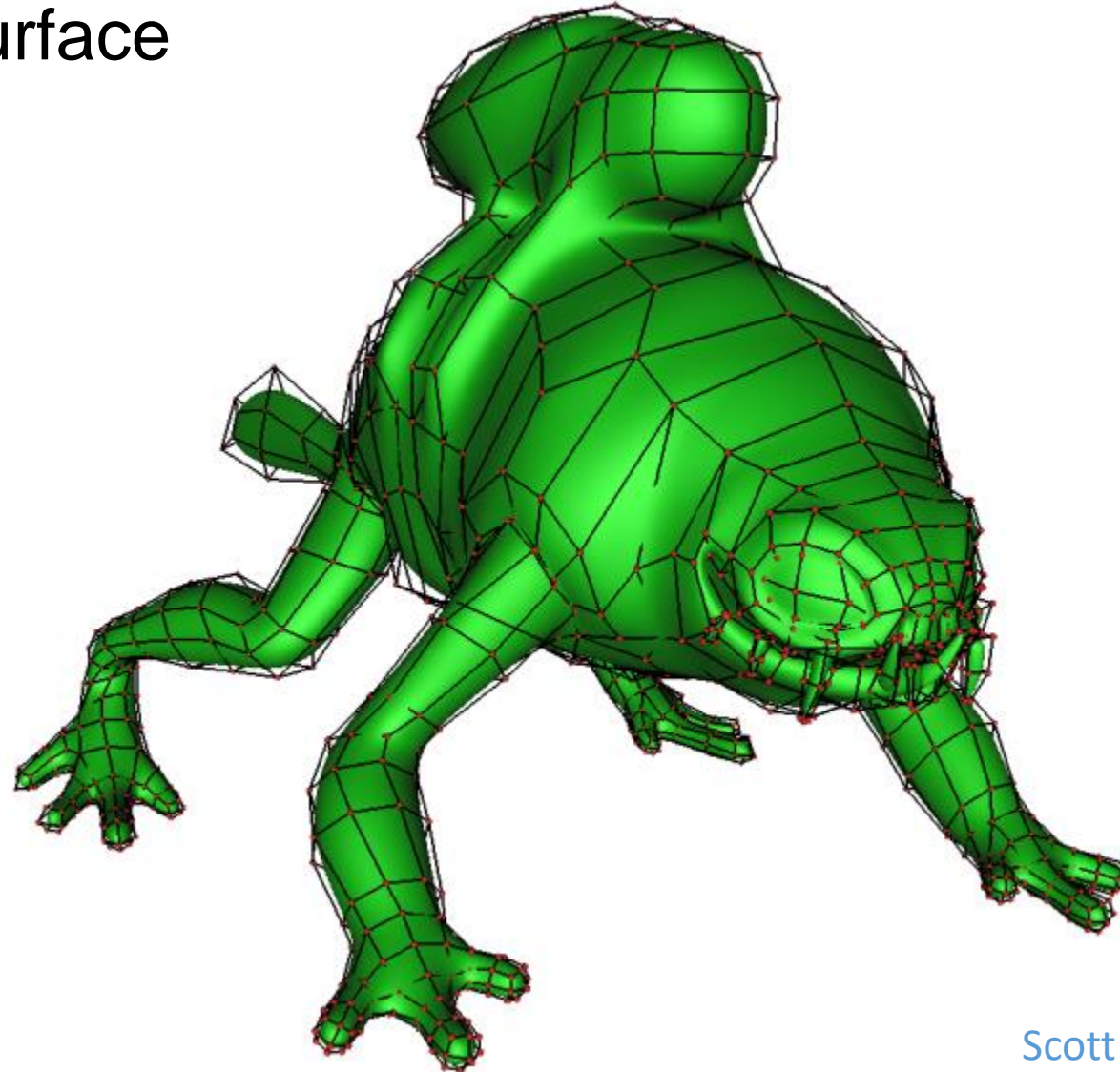


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Subdivision Surfaces – Examples



Base mesh + limit surface



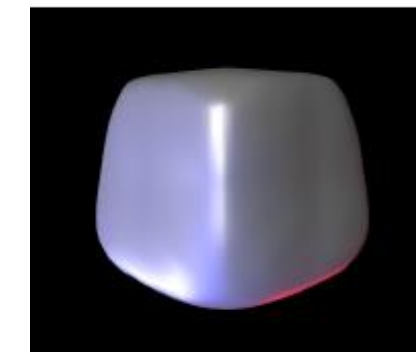
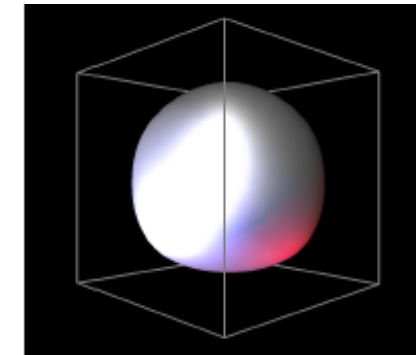
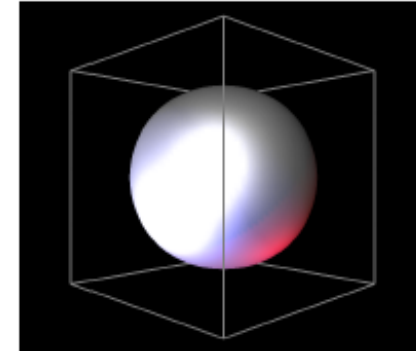
Meshlab demo



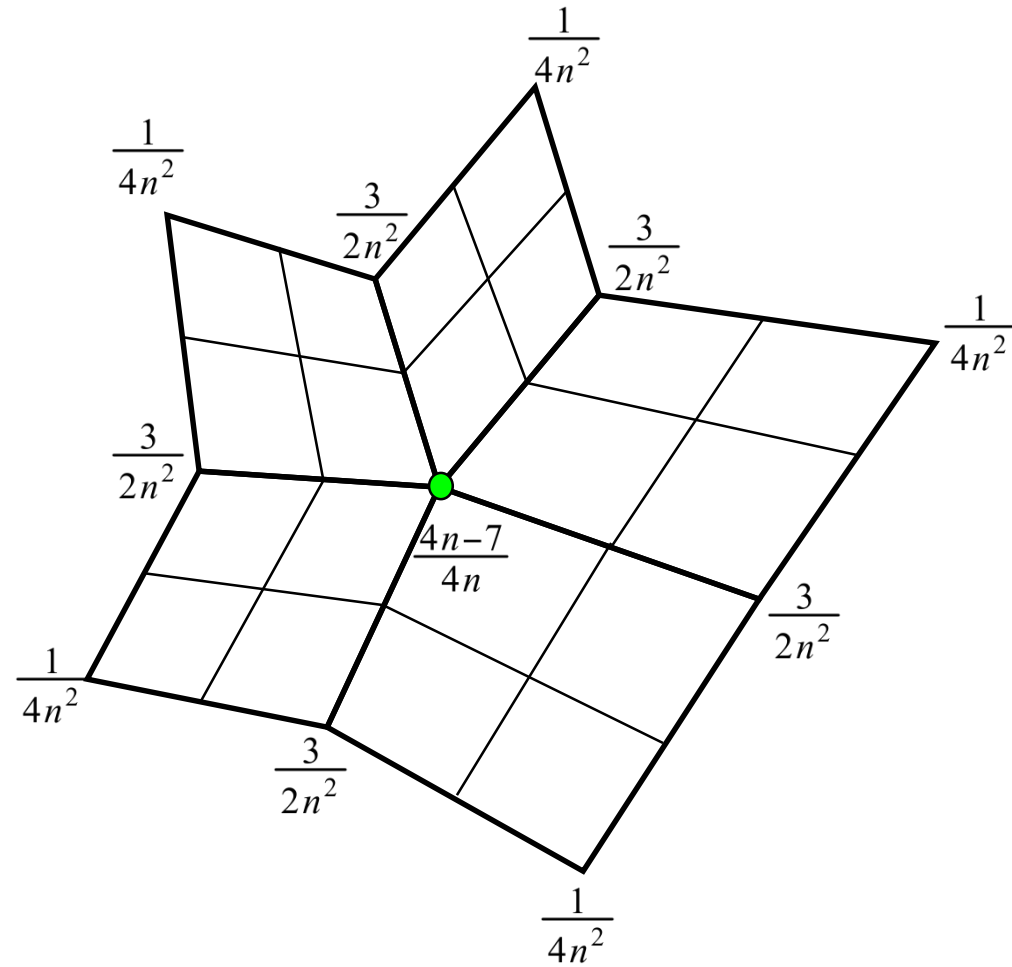
Subdivision Schemes



- Common subdivision schemes
 - Catmull-Clark
 - Loop
 - Many others
- Differ in ...
 - Input topology
 - How refine topology
 - How refine geometry
- ... which makes differences in ...
 - Provable properties



Catmull-Clark Subdivision

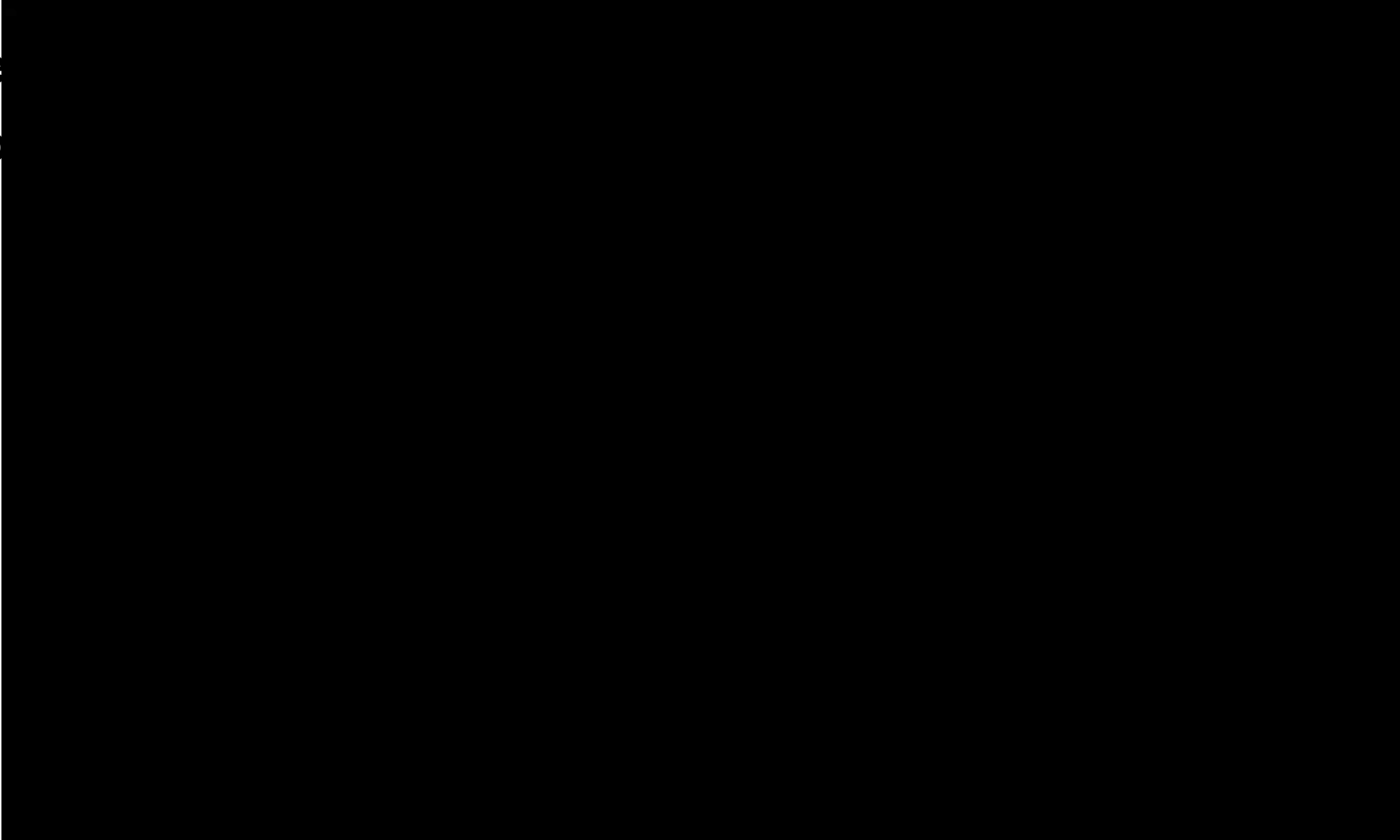


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Subdivision Surfaces



- Use
- Sup



Gerl's Game



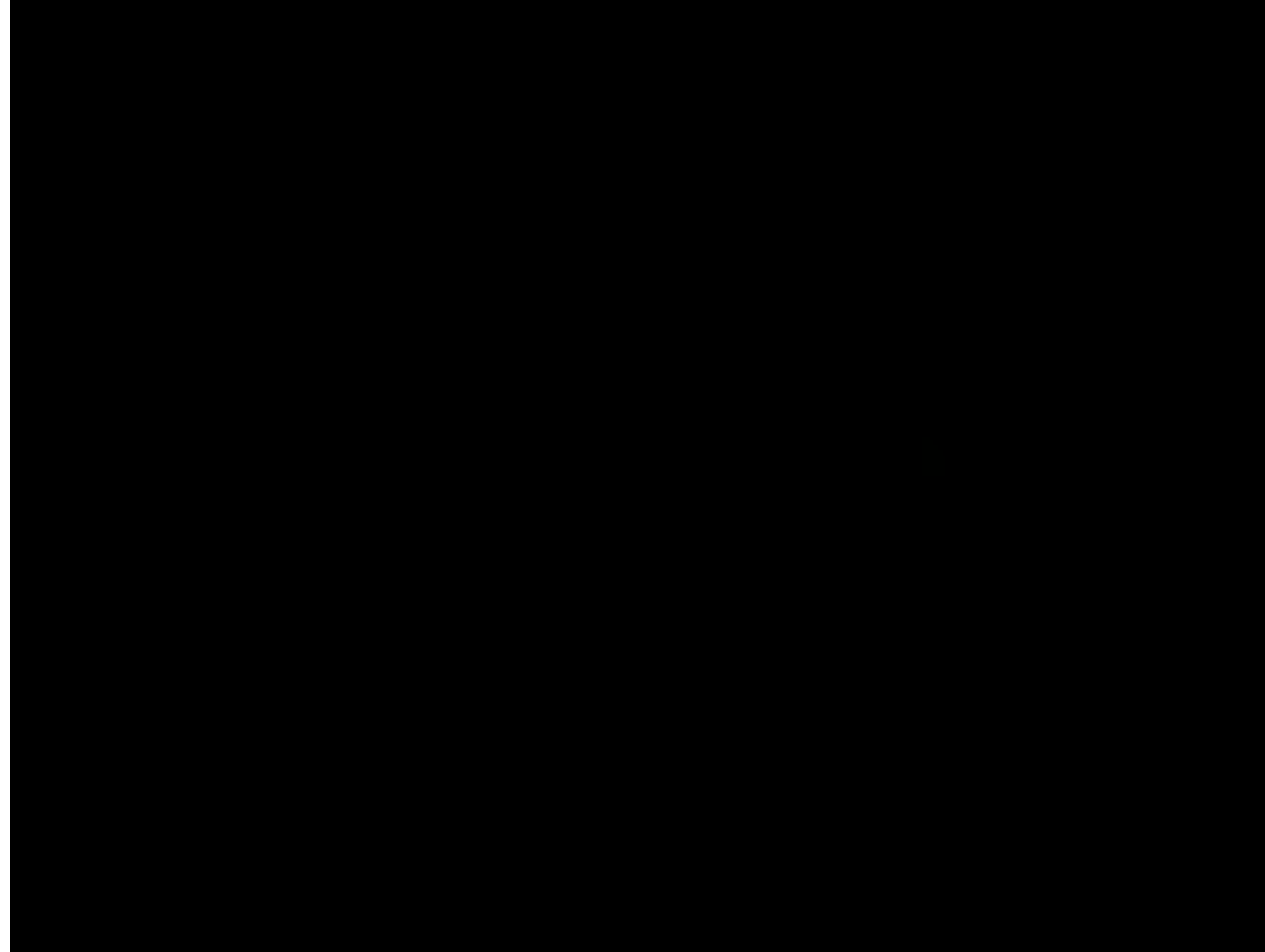
- “served as a demonstration of a new animation tool called subdivision surfaces” (Wikipedia)
- Subdivision used for head, hands & some clothing
- Academy Award winner



Geri's Game



- Guest performance in Toy Story 2



Toy Story 2 © Pixar Animation Studios

Subdivision Surfaces

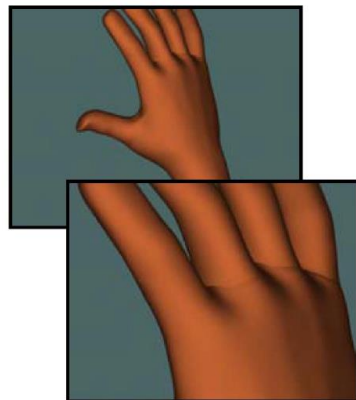


- An alternative to NURBS, overcoming:
 - Many patches
 - Difficult to mark sharp features

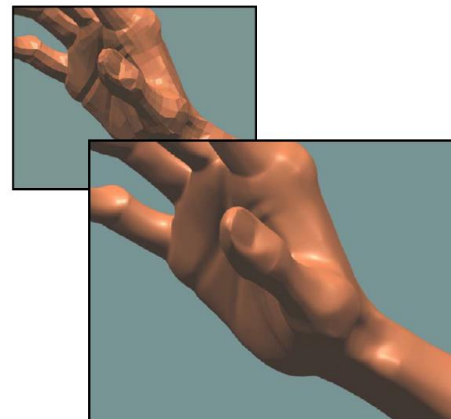


- Irregularities after deformation

Woody's hand (NURBS)



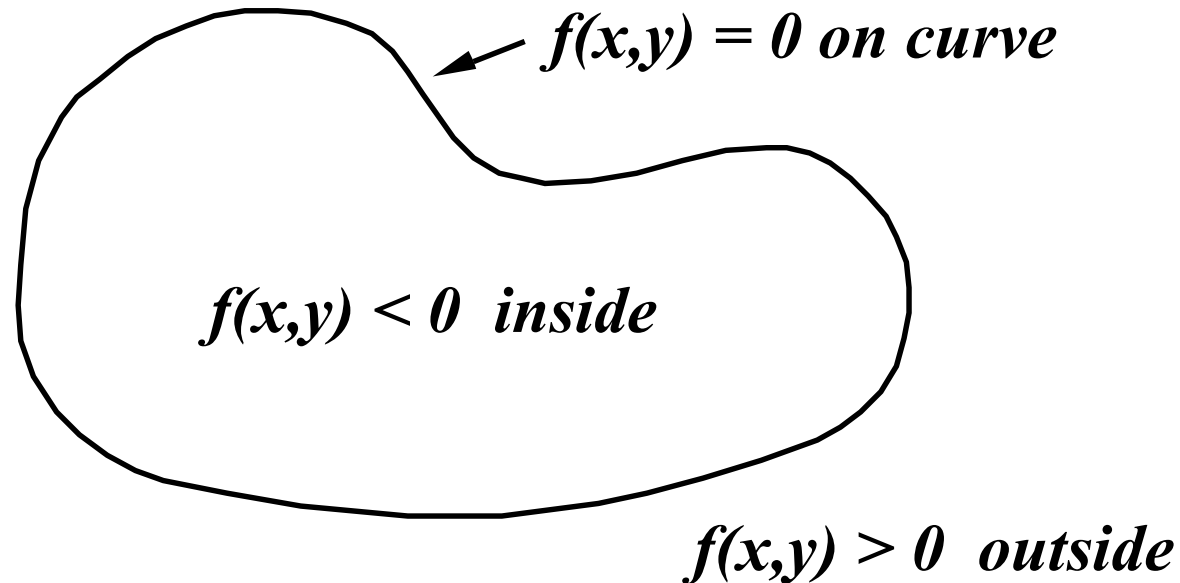
Geri's hand (subdivision)



Implicit Surfaces



- Surface defined implicitly by function:
 - $f(x, y, z) = 0$ (on surface)
 - $f(x, y, z) < 0$ (inside)
 - $f(x, y, z) > 0$ (outside)



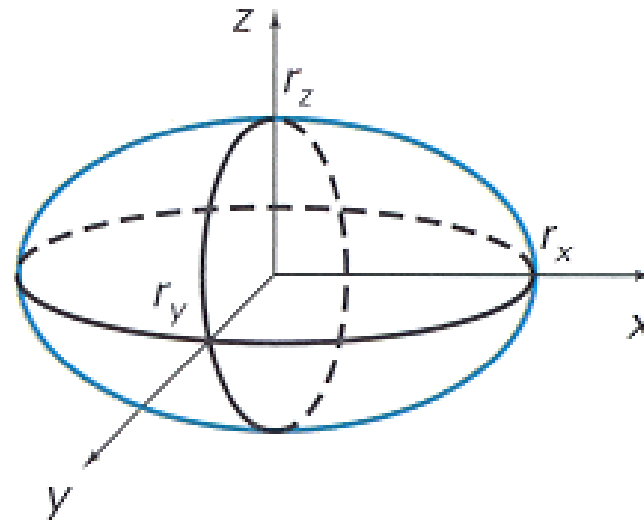
Implicit Surface Properties



Efficient check for whether point is inside

- Evaluate $f(x,y,z)$ to see if point is inside/outside/on
- Example: ellipsoid

$$f(x, y, z) = \left(\frac{x}{r_x}\right)^2 + \left(\frac{y}{r_y}\right)^2 + \left(\frac{z}{r_z}\right)^2 - 1$$

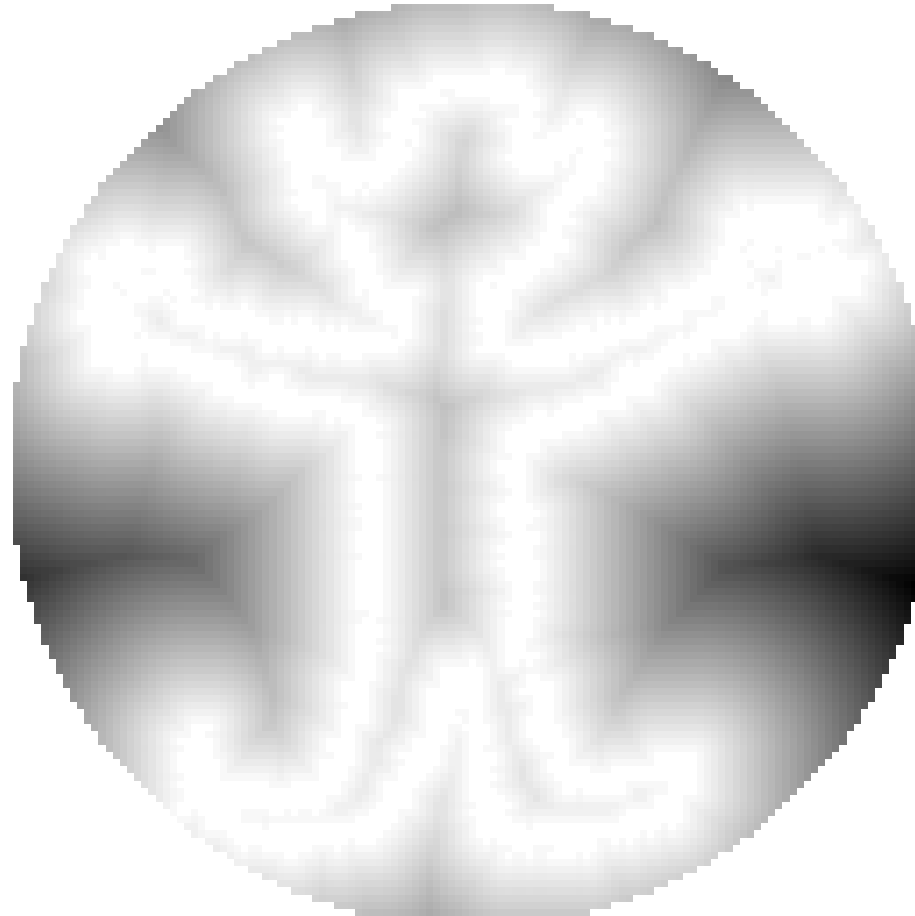


H&B Figure 10.10

Implicit Surfaces



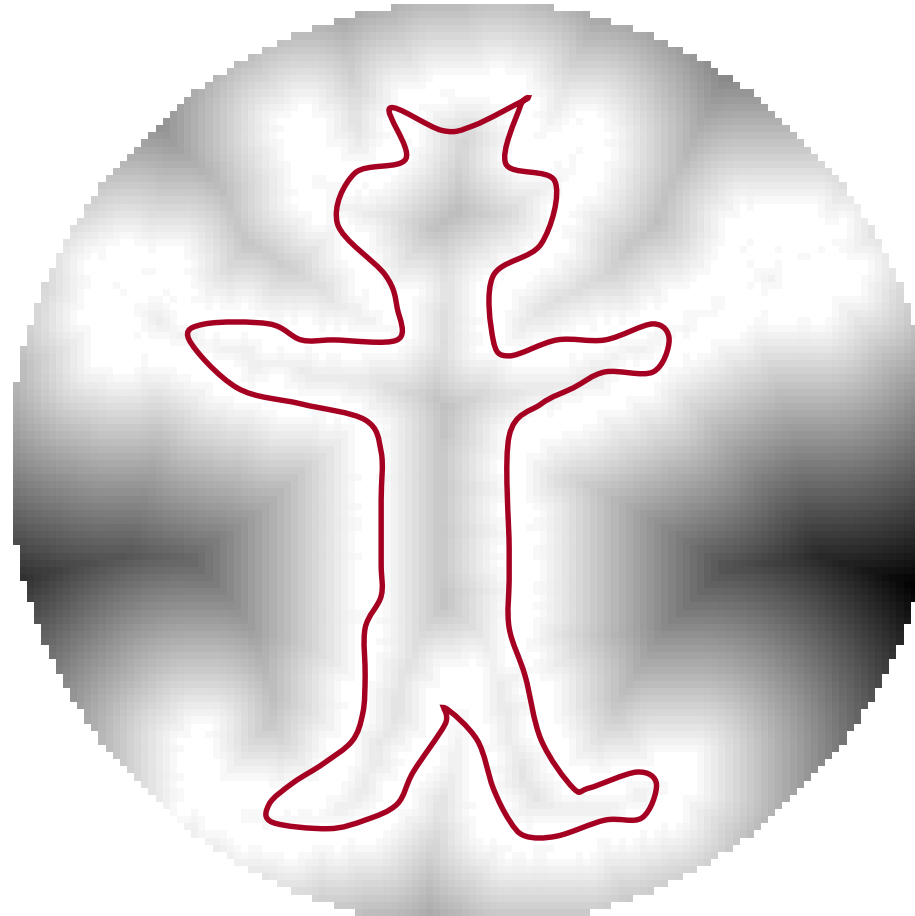
- Represent surface with function over all space



Implicit Surfaces



- Surface defined implicitly by function



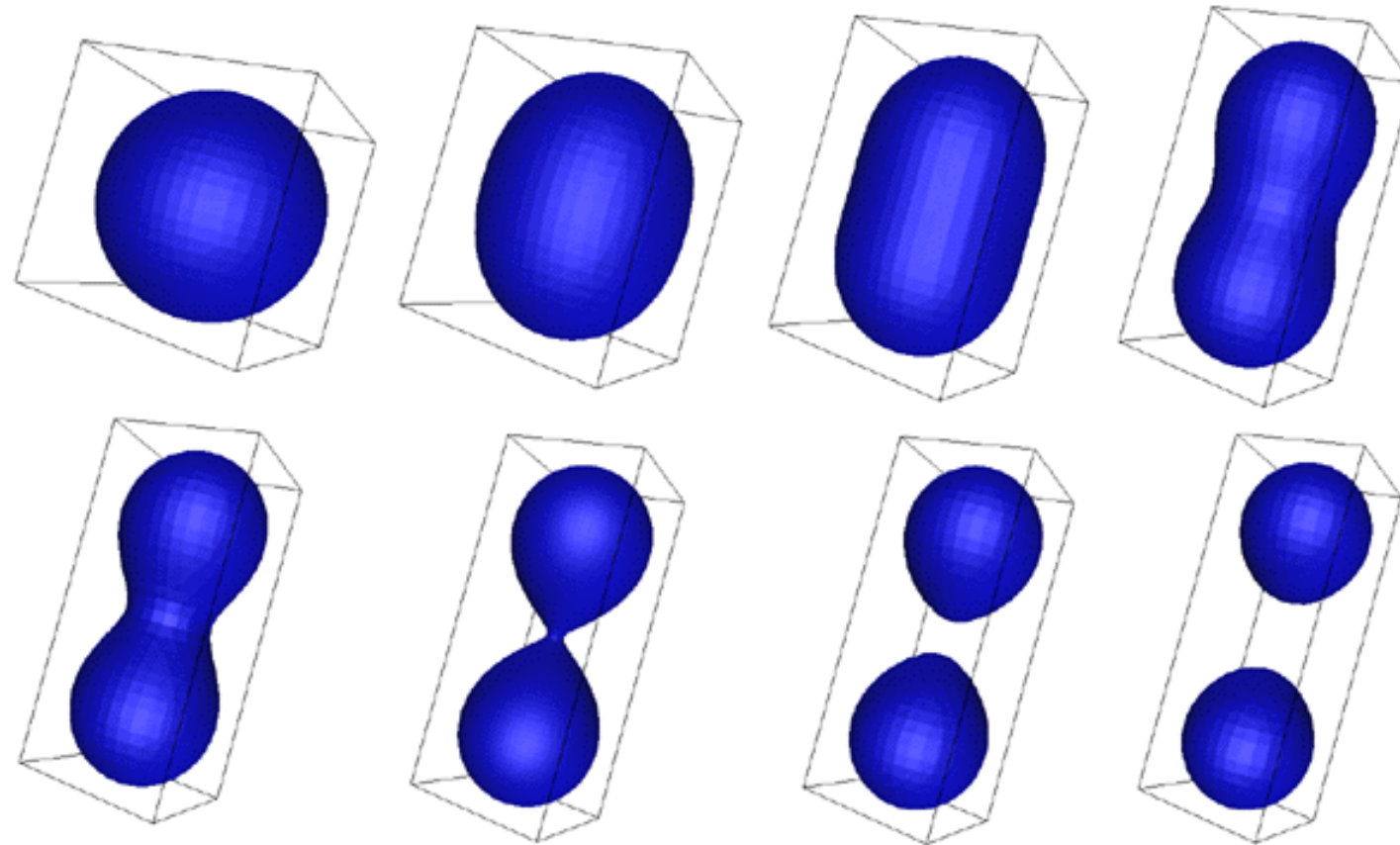
Kazhdan

Implicit Surface Properties



Efficient topology changes

- Surface is not represented explicitly!



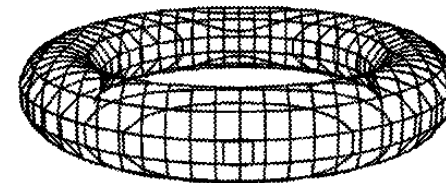
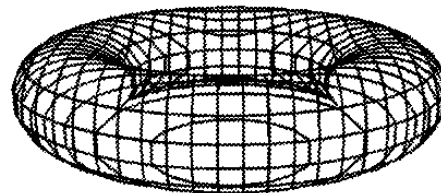
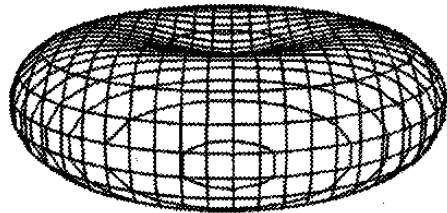
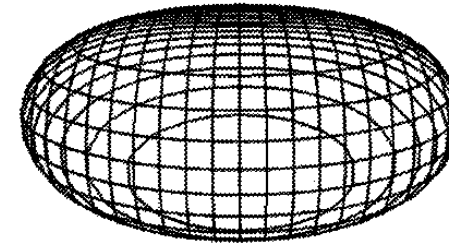
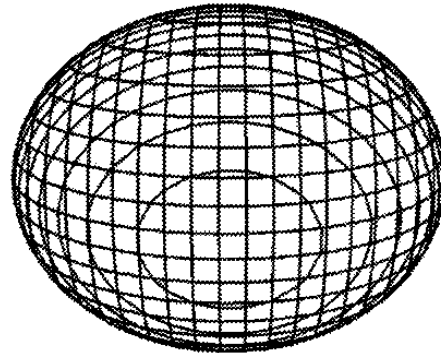
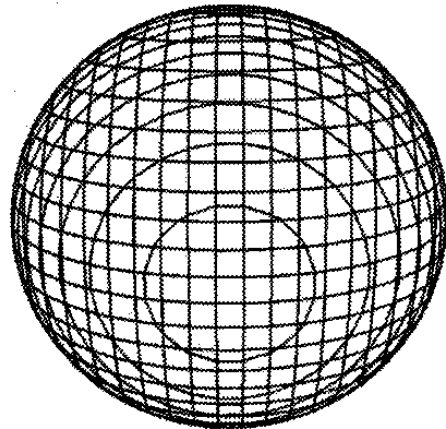
Bourke

Implicit Surface Properties



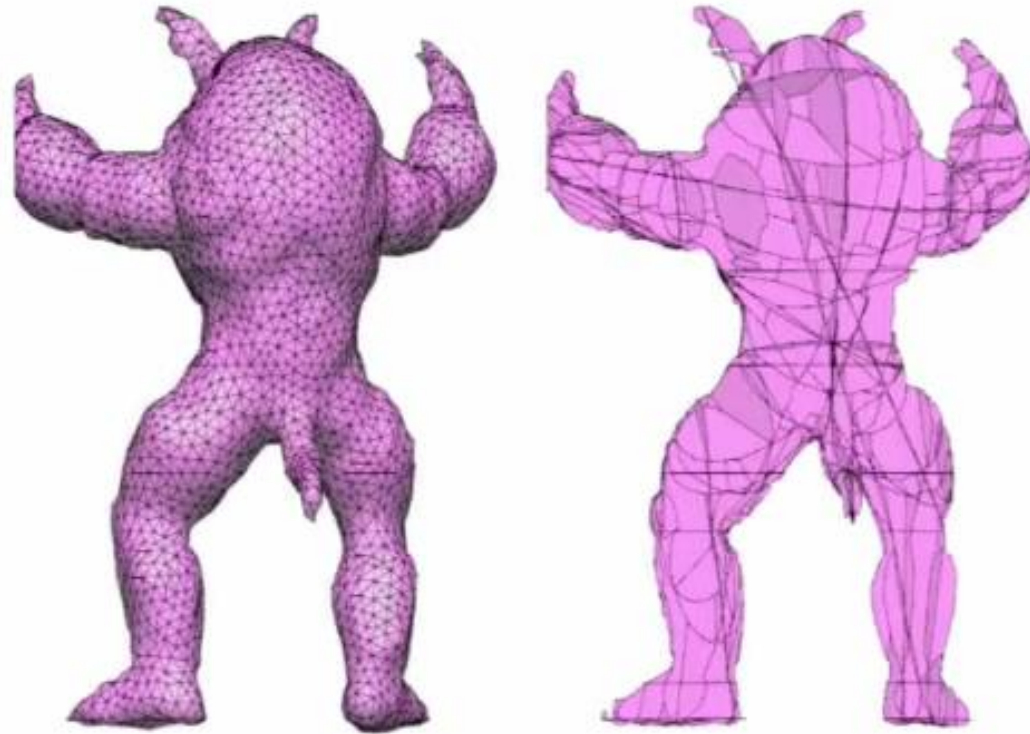
Efficient topology changes

- Surface is not represented explicitly!



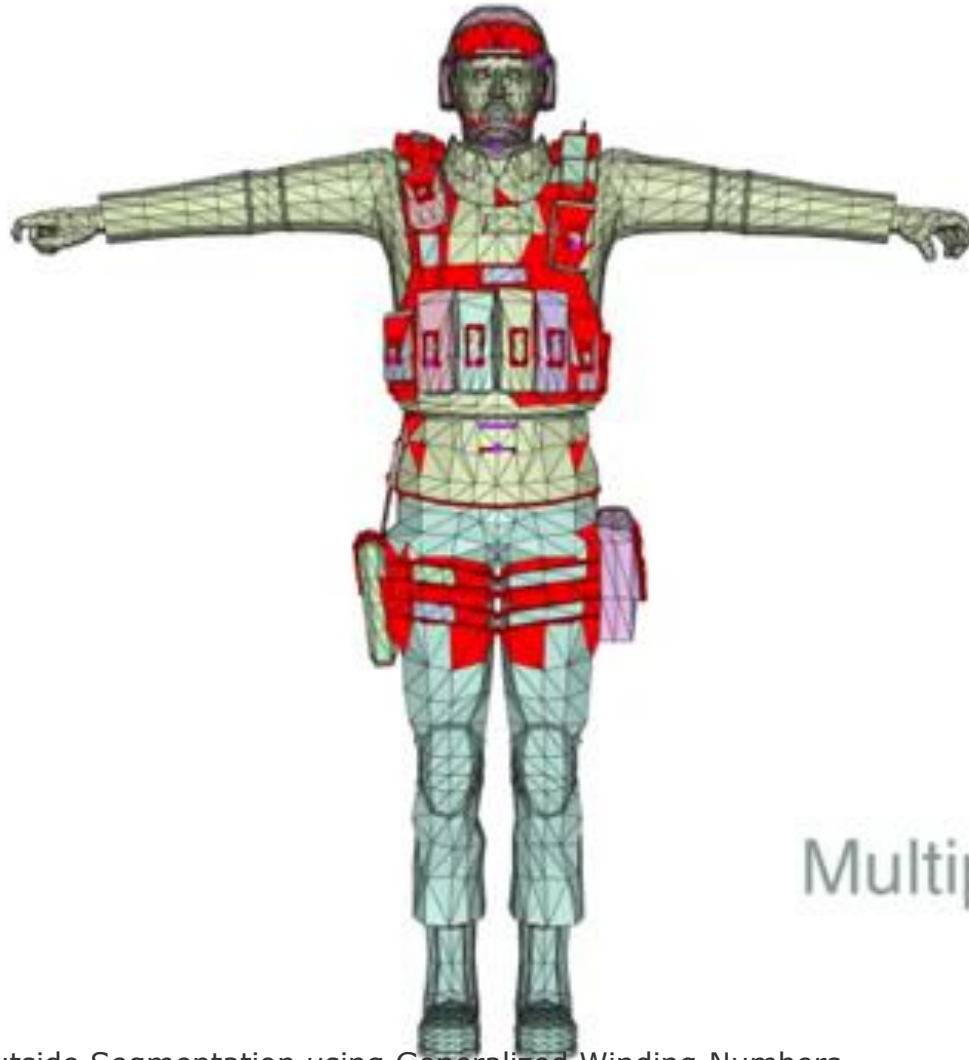
Bloomenthal

Applications



Online Reconstruction of 3D Objects from Arbitrary Cross-Sections
[Bermano et al. 2011]

Applications



Multiple connected components

3D Object Representations

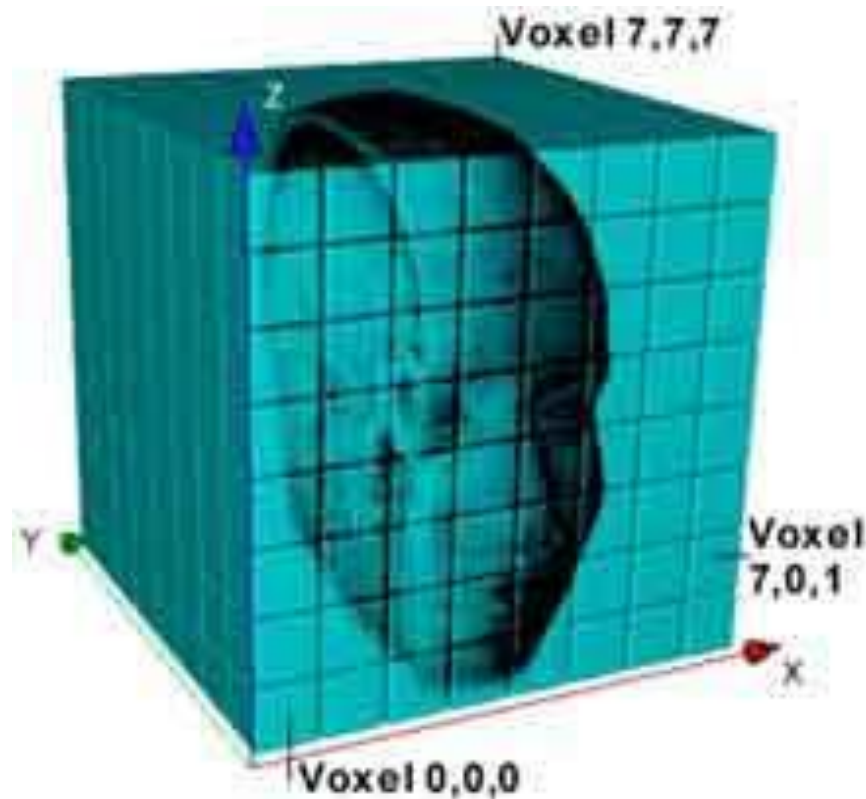


- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Voxels



- Regular array of 3D samples (like image)
 - Samples are called *voxels* (“**v**olume **pix**els”)



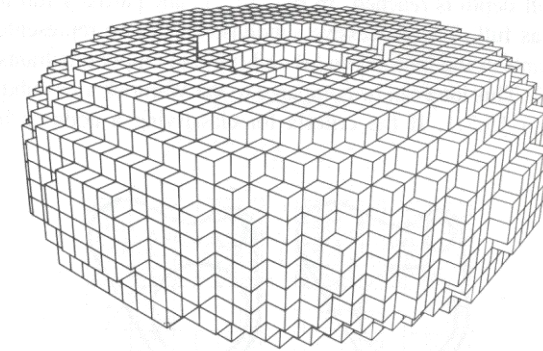
Voxel grid



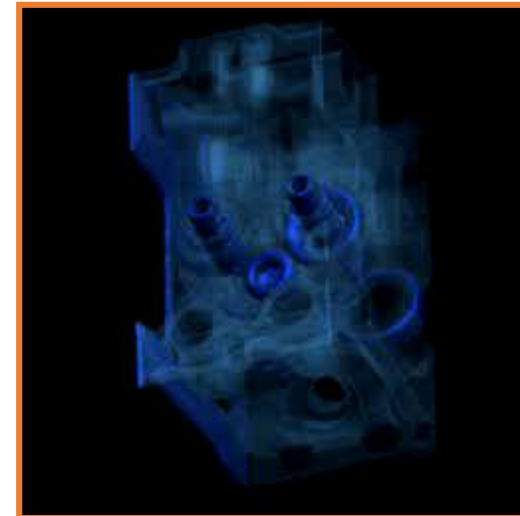
Uniform volumetric grid of samples:

- Occupancy
(object vs. empty space)
- Density
- Color
- Other function
(speed, temperature, etc.)

- Often acquired via
simulation or from
CAT, MRI, etc.



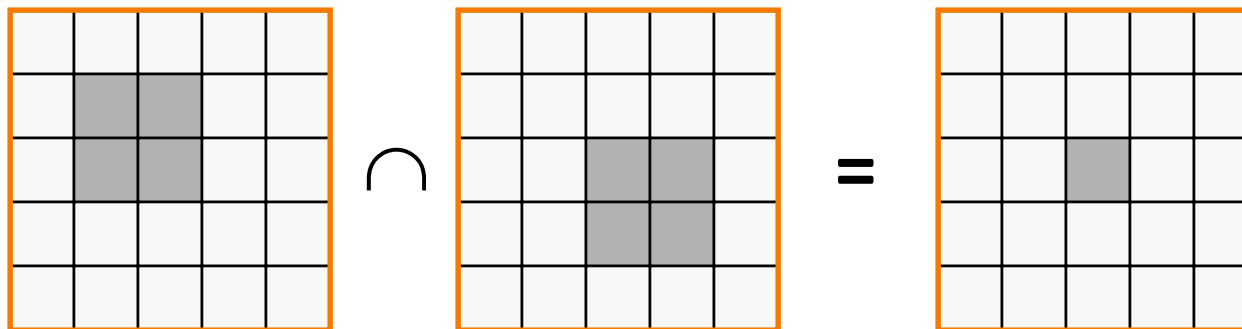
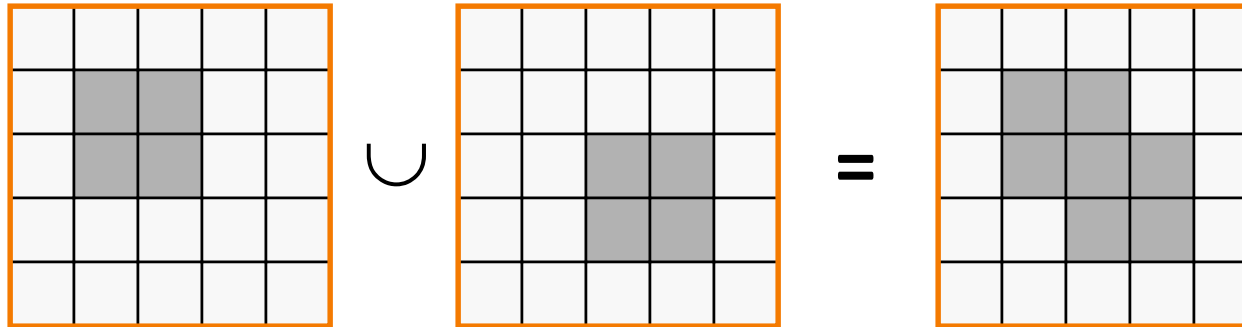
FvDFH Figure 12.20



Voxel Boolean Operations



- Compare objects voxel by voxel
 - Trivial

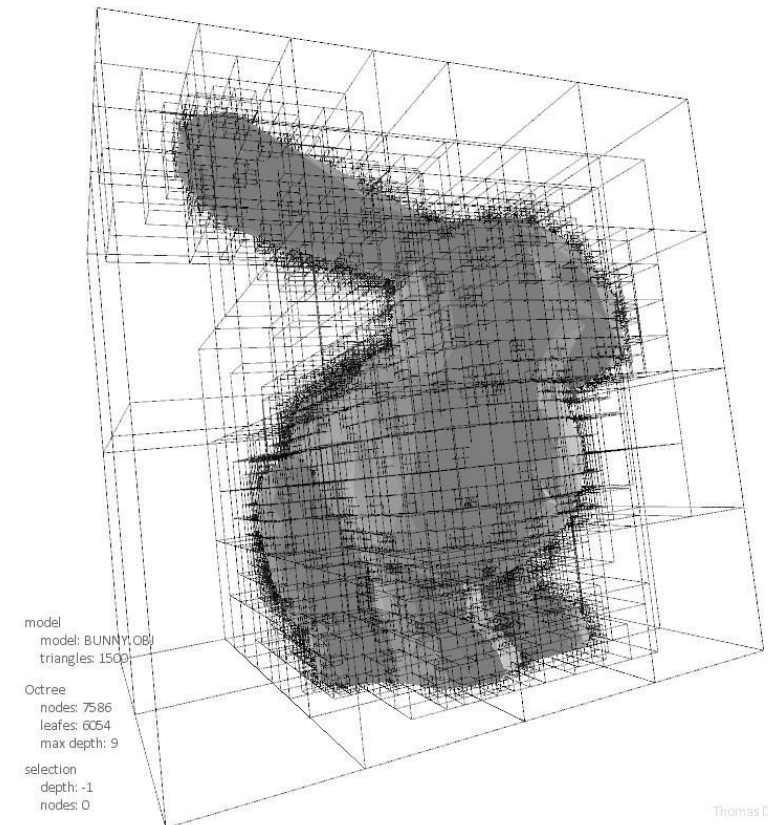
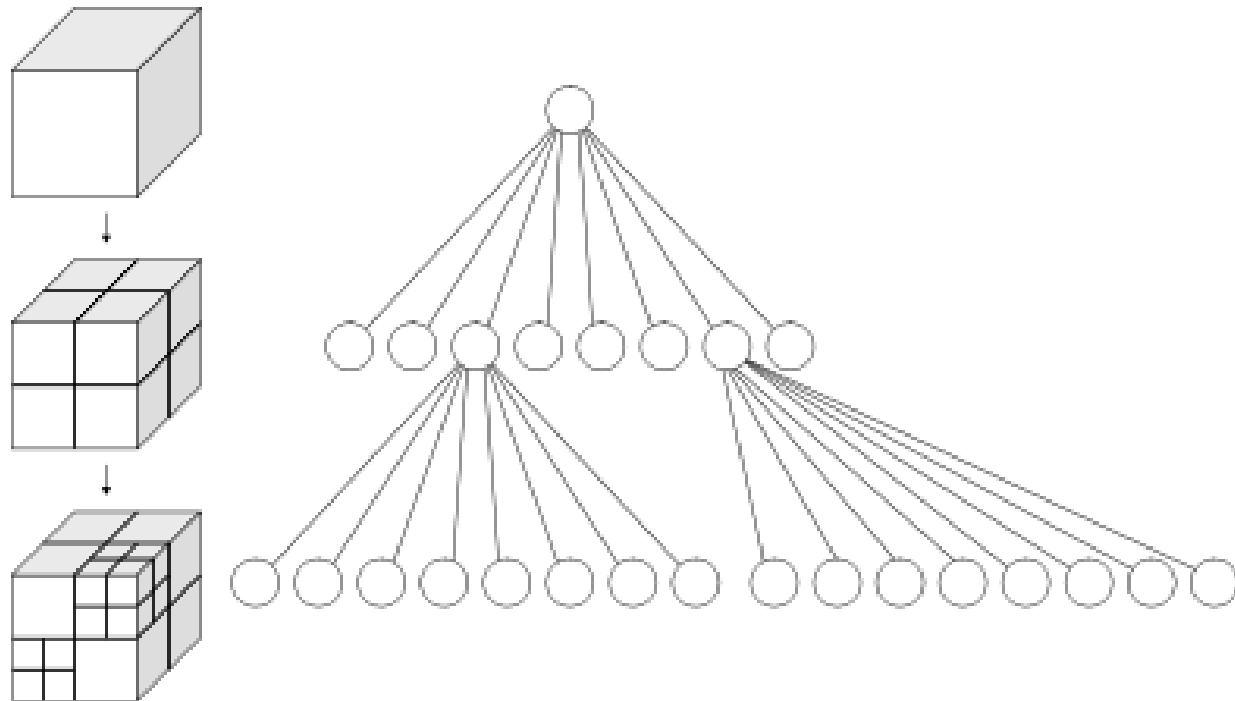


Octree



The adaptive version of the voxel grid

- Significantly more space efficient
- Makes operations more cumbersome

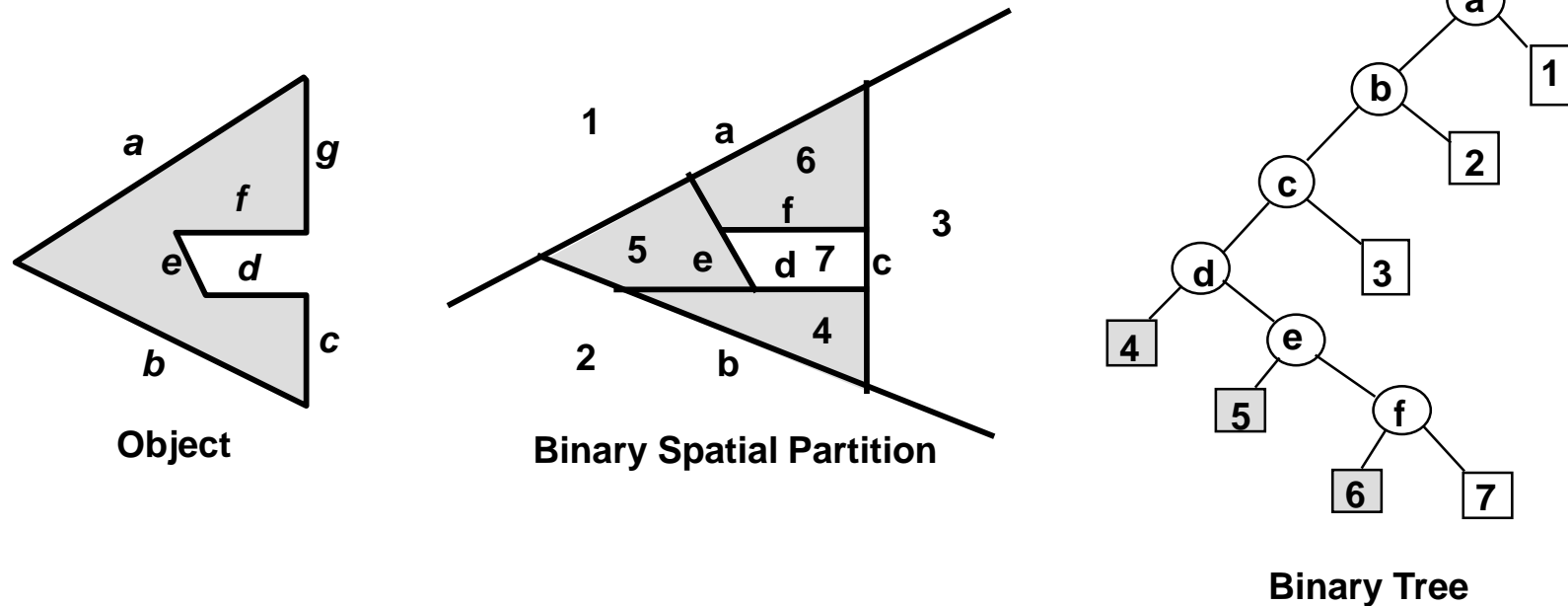


BSP Tree



Hierarchical **B**inary **S**pace **P**artition with solid/empty cells labeled

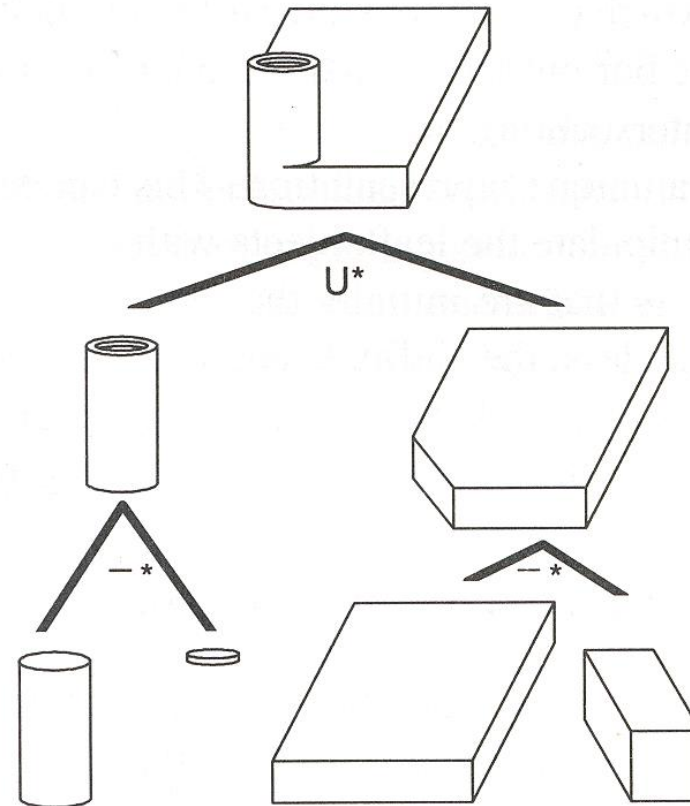
- Constructed from polygonal representations



Constructive Solid Geometry (CSG)



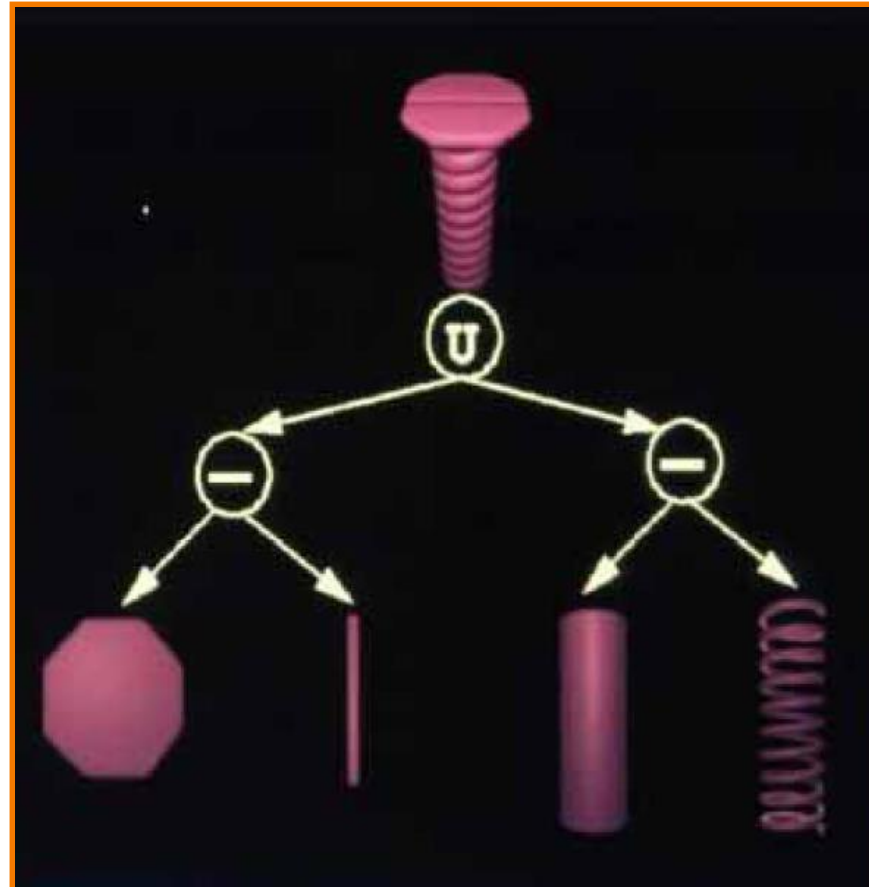
- Represent solid object as hierarchy of boolean operations
 - Union
 - Intersection
 - Difference



FvDFH Figure 12.27

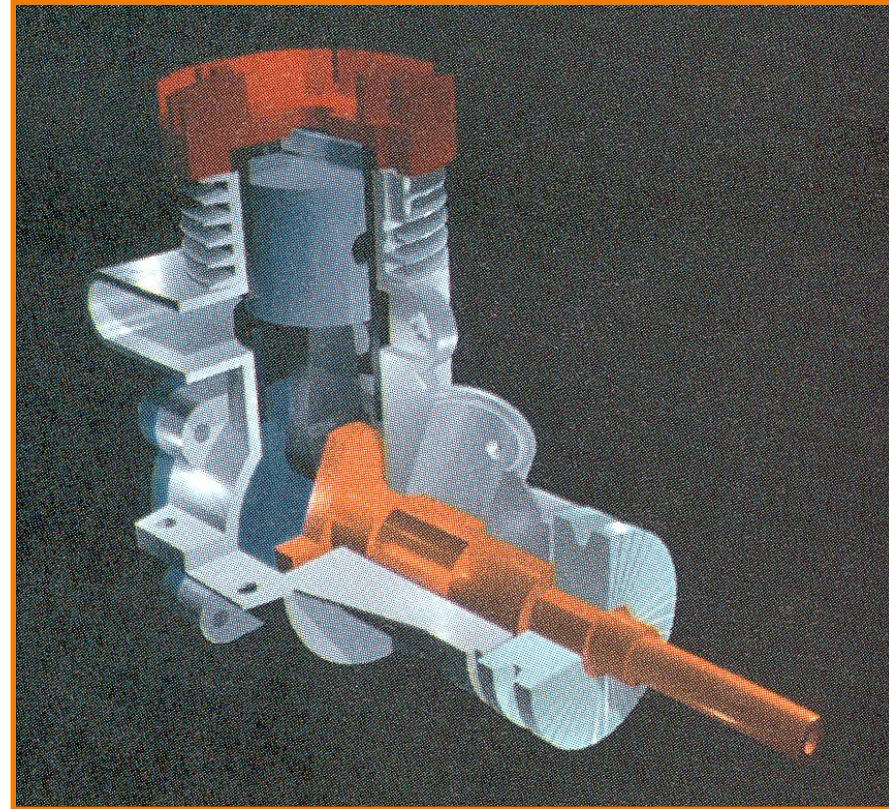


- Interactive modeling programs
 - Intuitive way to design objects



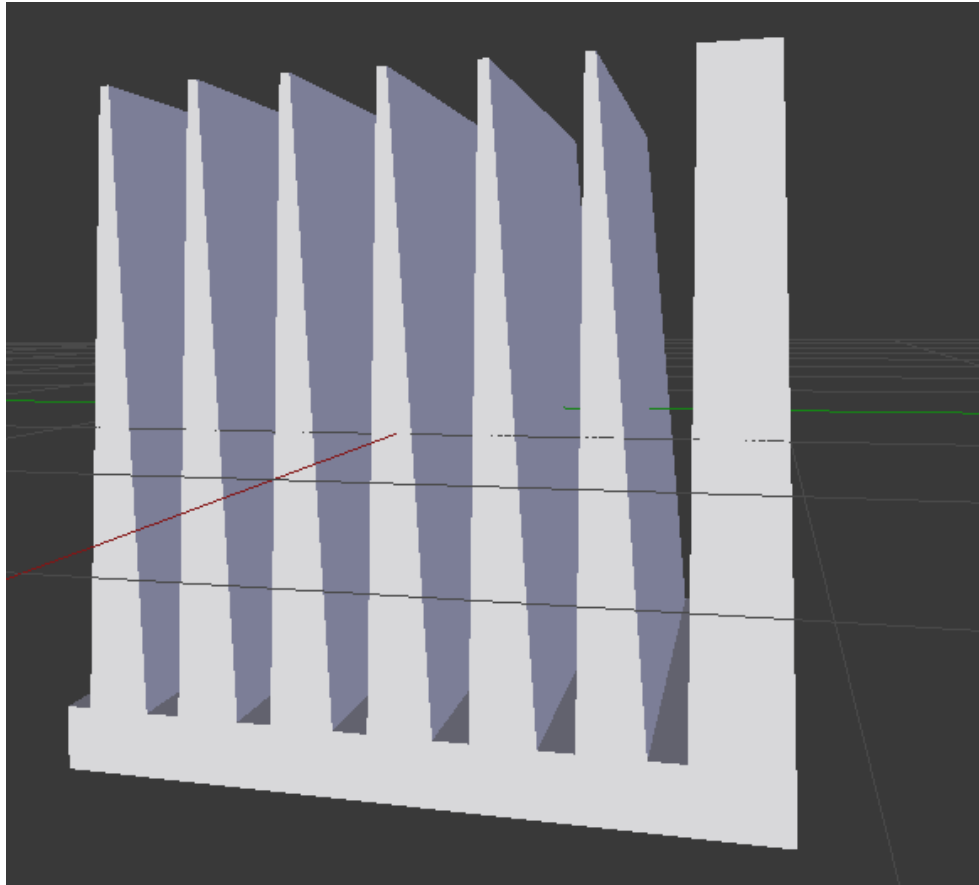


- Interactive modeling programs
 - Intuitive way to design objects



H&B Figure 9.9

CSG



3D Object Representations



- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific

Scene Graph



Union of objects at leaf nodes

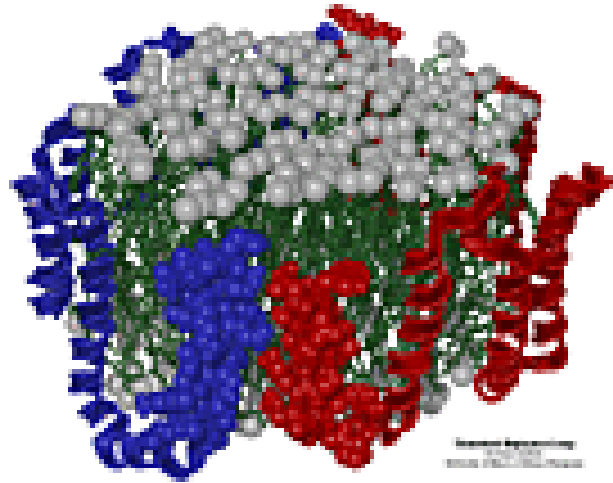


Bell Laboratories

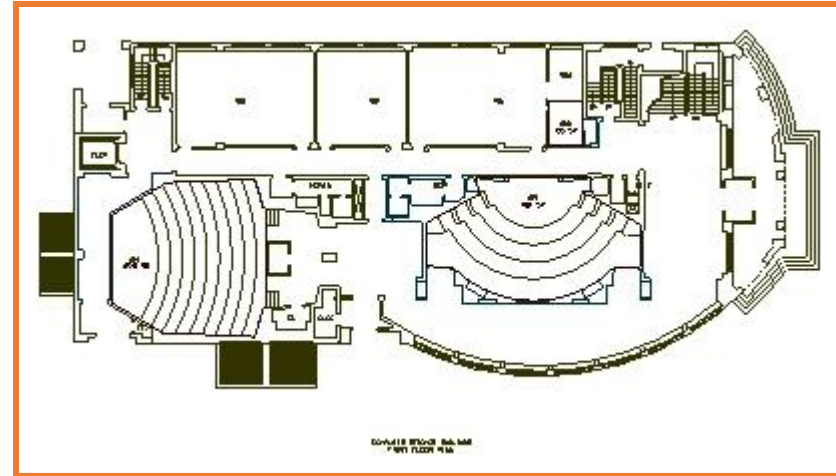


avalon.viewpoint.com

Application Specific



Apo A-1
*(Theoretical Biophysics Group,
University of Illinois at Urbana-Champaign)*



Architectural Floorplan
(CS Building, Princeton University)

Computational Differences



- Efficiency
 - Representational complexity (e.g. surface vs. volume)
 - Computational complexity (e.g. $O(n^2)$ vs $O(n^3)$)
 - Space/time trade-offs (e.g. tree data structures)
 - Numerical accuracy/stability (e.g. degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine