Do the magic properties of the Benjamini-Hochberg procedure hold in the context of multiple regression?

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Benjamini and Hochberg procedure [2] is a widely applied tool for multiple testing. It is now known that apart from controlling FDR is has some asymptotic optimality properties in the context of parameter estimation and minimizing the Bayes risk in sparse mixtures ([1],[3],[4]). These known results will be briefly summarized and then we will concentrate on the related problem of identifying „causal“ regressors in a high dimensional sparse regression. Inherent limitations with respect to FDR control in the context of multiple regression will be presented, which however still allow to control this parameter under very low sparsity and when the columns of the design matrix are only weakly correlated. A new convex optimization procedure, SLOPE ([5],[6]), will be presented, which uses BH idea and has been empirically shown to control FDR in the context of multiple regression with weakly correlated regressors. We will also present simulation results illustrating very promising predictive properties of SLOPE, which suggest that the asymptotic optimality results of [1] carry over into the context of sparse high dimensional regression.

References