

List of publications by Eugenii Shustin

BOOKS

- [1] (jointly with G.-M. Greuel and C. Lossen) *Introduction to singularities and deformations*. Springer-Verlag, Berlin, Heidelberg, 2007.
- [2] (jointly with I. Itenberg and G. Mikhalkin) *Tropical algebraic geometry/ Oberwolfach seminars*, vol. **35**. Birkhauser, 2007.
- [3] (jointly with G.-M. Greuel and C. Lossen) *Singular Algebraic Curves*. Springer, Cham 2018.

ARTICLES

- [1] (jointly with D.A. Gudkov) Classification of non-singular 8th order curves on ellipsoid. In: *Methods of Qualitative Theory*, Gorky University Press, Gorky, 1980, pp. 104–107 (Russian).
- [2] On invariants of algebraic curve singular points. *Math. Notes of Acad. Sci. USSR* **34** (1983), 962–963.
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- [16] Hyperbolic and minimal smoothings of singular points. *Selecta Math. Sov.* **10** (1991), no. 1, 19–25.
- [17] Dynamical systems in \mathbf{C}^2 and real curves of 8th degree. In: *Methods of Qualitative Theory*, N.-Novgorod University Press, N.-Novgorod, 1991, pp. 120–129 (Russian).
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